

1 Article

2 Active Prior Tactile Knowledge Transfer for Learning 3 Tactual Properties of New Objects

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8
9 **Abstract:** Reusing the tactile knowledge of some previously-explored objects helps us to easily
10 recognize the tactual properties of new objects. In this paper, we enable a robotic arm equipped
11 with multi-modal artificial skin, like humans, to actively transfer the prior tactile exploratory action
12 experiences when it learns the detailed physical properties of new objects. These experiences, or prior
13 tactile knowledge, are built by the feature observations that the robot perceives from multiple sensory
14 modalities, when it applies the pressing, sliding, and static contact movements on objects with
15 different action parameters. We call our method Active Prior Tactile Knowledge Transfer (APTKT),
16 and systematically evaluated its performance by several experiments. Results show that the robot
17 improved the discrimination accuracy by around 10% when it used only one training sample plus
18 the feature observations of prior objects. By incorporating the auxiliary features, the transfer learning
19 improved the discrimination accuracy by over 20%. The results also show that the proposed method
20 is robust against transferring irrelevant prior tactile knowledge (negative knowledge transfer).

21 **Keywords:** tactile sensing; artificial robotic skin; active tactile object perception; active tactile object
22 learning; active tactile transfer learning

23 1. Introduction

24 1.1. Motivation

25 We humans perceive tactual properties of an object (e.g. stiffness, textures, temperature, weight)
26 by applying exploratory actions (e.g. pressing, sliding, static contact, lifting). After applying different
27 exploratory actions on an object, we can attain its different tactile information. Conversely, making
28 the same exploratory action on different objects will produce different tactile observations. Therefore,
29 when we learn about an object, we always link its physical properties with the exploratory actions that
30 we apply on it.

31 Besides different kinds of exploratory actions, the tactile information we perceive from an object is
32 also dependent on how we apply an action. Consider an example of pressing on two objects. The object
33 1 is made of soft sponge, and the object 2 is made by covering a soft sponge surface on a solid metal.
34 When pressing our fingertips on both objects with a small normal force, we can recognize similar
35 object deformations. However, if we press with a larger normal force, object 1 deforms much more
36 than object 2, since we have reached the metal part in object 2. A similar situation can also be found
37 when we apply the sliding movement on the object surfaces with different forces and velocities. As a
38 result, by applying different exploratory actions in different ways, we can build a *detailed* knowledge
39 of the object tactual properties which we call tactile exploratory action experiences.

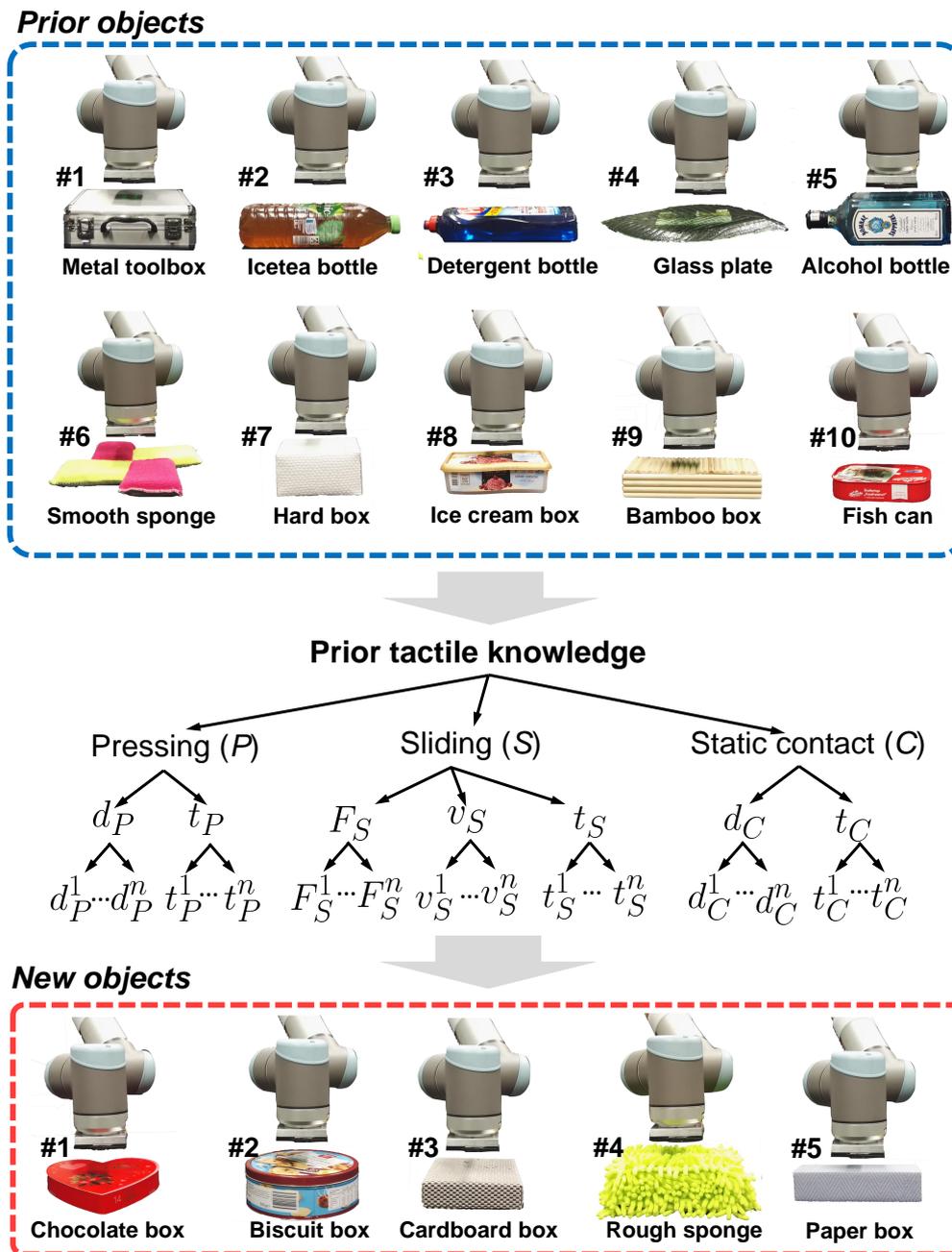


Figure 1. The robot leverages the prior tactile exploratory action experiences built by applying the pressing, sliding, and static contact movements with different action parameters on the old objects (with index #1 - #10) to learn about new objects (with index #1 - #5) physical properties. The feature observations of prior objects (prior tactile instance knowledge) were used to transfer the action experiences.

40 We humans learn about new objects in an active and incremental way. We actively select the most
 41 informative exploratory actions to interact with them. More importantly, we relate these new objects
 42 with the experiences of exploring the objects that we have previously encountered. By transferring
 43 the prior tactile knowledge, or prior tactile exploratory action experiences, we can largely reduce the
 44 amount of exploratory actions required to discriminate among new objects. In this way, we humans
 45 save a lot of time and energy, and recognize new objects with high accuracy.

46 Can robotic systems with a sense of touch also performs like humans to actively transfer the past
47 tactile exploratory action experiences when learning about new objects (transfer learning)?

48 1.2. Background

49 Over the past decades, researchers have developed various tactile sensors and mounted them on
50 robotic systems (e.g. [1–6]). In this way, the robots with a sense of touch can perceive different object
51 tactual properties by applying exploratory actions. For example, a robot can slide its sensory parts on
52 objects to sense their textural properties [7–9], build a static contact to perceive the temperature [10], or
53 lift objects to obtain their center of mass [11]. Furthermore, several methods has been proposed for the
54 active object exploration problem, in which the robot actively applies multiple exploratory actions to
55 discriminate among objects (e.g. [12–17]).

56 However, The problem of transferring the robotic prior tactile knowledge has been rarely
57 investigated. Even though many transfer learning techniques has been successfully applied to various
58 areas (e.g. Natural Language Processing: [18]; WiFi-based localization: [19]; Computer Vision: [20–22];
59 Bio-informatics: [23]), it was our works that introduced tactile transfer learning. Previously, Kaboli
60 *et al.* [24] developed a novel textural descriptor. Using the descriptor, a ShadowHand dexterous
61 robotic hand equipped with BioTac sensors on its fingertips could efficiently discriminate among object
62 surface textures. Later, we designed a transfer learning method [25] so that the robotic hand could
63 reuse the prior texture models from 12 objects to learn 10 new object textures. However, since only the
64 sliding movement was applied, the robot could only transfer the object textural properties. In a later
65 work [26], we proposed an active learning method that an UR10 robotic arm with an artificial skin
66 on its end-effector could not only apply sliding movement, but also apply pressing and static contact
67 movements on objects to learn about their different physical properties (surface texture, stiffness, and
68 thermal conductivity). Even though our active learning method enables the robot to efficiently learn
69 about objects, the robot still needs to learn from scratch given a new set of objects. In this regard,
70 recently we proposed an algorithm called Active Tactile Transfer Learning (ATTL) [27] to actively
71 transfer the knowledge of multiple physical properties from prior objects. Using ATTL, the UR10
72 robotic arm could actively select prior knowledge of different object physical properties (surface texture,
73 stiffness, and thermal conductivity by applying sliding, pressing, and static contact movements) to
74 transfer. As a result, the robot could use less training samples to achieve higher recognition rate, when
75 it learned about new objects.

76 The robotic systems in the above-mentioned works only applied exploratory actions with fixed
77 action parameters, e.g. sliding with a fixed velocity to perceive surface textures. Therefore, the robots
78 can only transfer limited prior tactile knowledge and learn the coarse physical properties of new
79 objects. In order to learn objects' *detailed* physical properties so as to better discriminate among objects,
80 the robots should be able to apply an exploratory action in different ways, similar to us humans.

81 1.3. Contribution

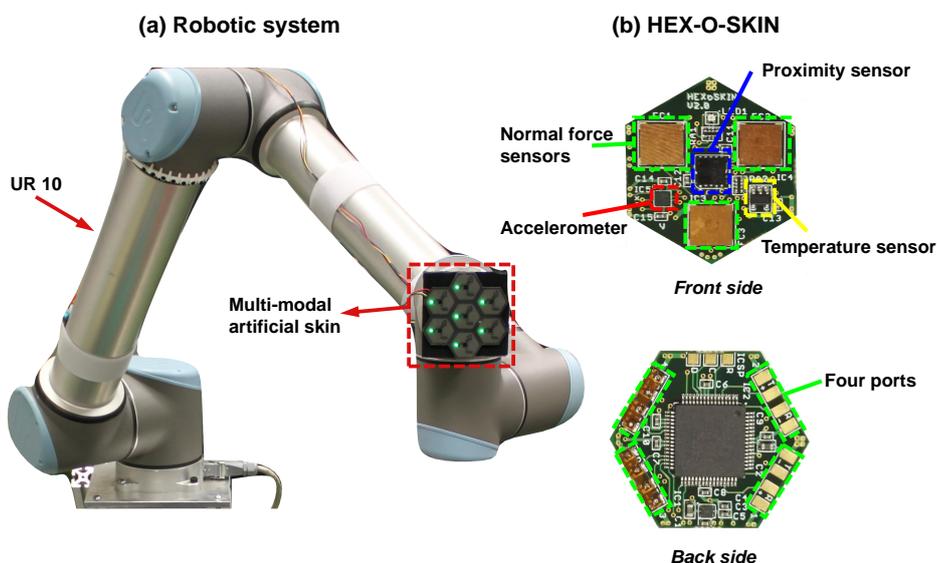
82 In this paper, we focus on actively transferring the prior tactile exploratory action experiences to
83 learn the detailed physical properties of new objects. Our contributions are two-folds:

- 84 • We enable a robot to apply more exploratory actions with various action parameters. In this way,
85 the robot gains a more detailed object tactile knowledge.
- 86 • We propose a tactile transfer learning algorithm so that the robot actively leverages the detailed
87 tactile knowledge of some previously-explored objects (i.e. prior tactile exploratory action
88 experiences), when it learns about new objects. The feature observations of prior objects are
89 transferred, which are perceived from multiple sensory modalities.

90 In the sequel, we first introduce the robotic system (Sec. 2). Then, we illustrate how the robot
91 applies exploratory actions and obtain the physical properties of objects (Sec. 3). Afterwards, we
92 illustrate our proposed tactile transfer learning in detail (Sec. 4), followed by a systematic evaluation

Table 1. Technical information of sensors in the artificial skin ([7]).

Type	Sensor	Range	Accuracy	Resolution
Proximity	VCNL4010	200mm	N.A.	0.25lx
Acceleration	BMA250	$\pm 2g$	256LSB/g	3.91 mg
Temperature	LM71	$-40 - 150^{\circ}C$	$\pm 1.5^{\circ}C$	$31.25m^{\circ}C$
Normal force	customized	$> 10N$	0.05N	N.A.

**Figure 2.** (a): The UR10 robotic arm equipped with a multi-modal artificial skin. (b): The HEX-O-SKIN (skincell) in the artificial skin.

93 of the method (Sec. 5). We finalize this paper with a conclusion and a discussion about future works
 94 (Sec. 6).

95 2. System Description

96 2.1. Multi-modal Artificial Skin

97 To enable the robot to perform more human-like behaviours with different tactile sensing
 98 modalities, we designed and manufactured multi-modal artificial skin (Fig. 2 (a)) made by seven
 99 active tactile modules called "HEX-O-SKIN" (Fig. 2 (b)) [1]. Each module is a small hexagonal printed
 100 circuit board equipped with off-the-shelf sensors (one temperature sensor, one accelerometer, three
 101 normal force sensors, and one proximity sensor). In this way, robots equipped with this artificial skin
 102 with seven temperature sensors, seven accelerometers, 21 normal force sensors, and seven proximity
 103 sensors can emulate the human tactile sensing about temperature, vibrations, force, and light touch.
 104 Their technical information is summarized in Tab. 1.

105 2.2. UR10 Robotic Arm

106 We mounted the multi-modal artificial skin on the end-effector of an Universal Robotic Arm
 107 (UR10) with six DoF (Fig. 2 (a)). The UR10 was controlled in collaboration with the artificial skin in
 108 order to apply different exploratory actions on objects.

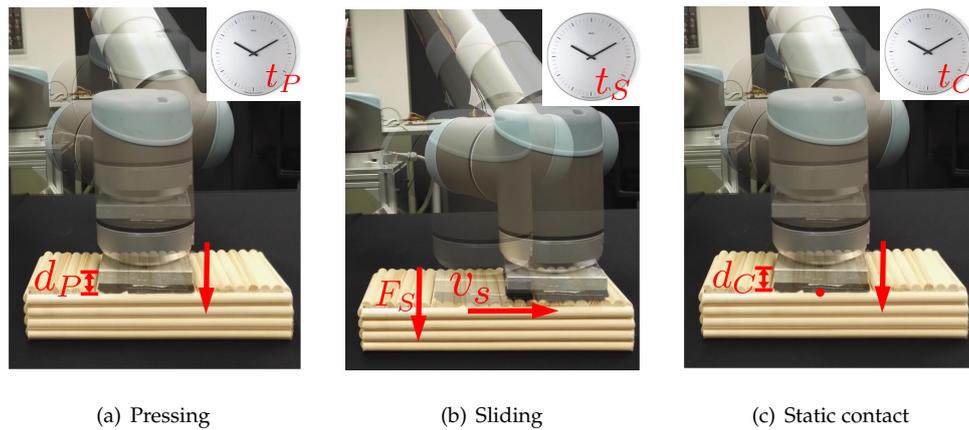


Figure 3. Visualization of the exploratory actions. **(a):** The pressing movement defined by the action parameters d_P and t_P . **(b):** The sliding movement with action parameters v_S , F_S , and t_S . **(c):** The static contact movement defined by d_C and t_C .

109 3. Exploratory Actions and Perception

110 3.1. Exploratory Actions Definition

111 By applying exploratory actions on objects with different action parameters, the robot can attain
 112 different feature observations. In this work, we consider three types of exploratory actions: *pressing*
 113 (denoted as P), *sliding* (denoted as S), and *static contact* (denoted as C). Formally, we define N_a number
 114 of exploratory actions as $A = \{\alpha_n^{\theta_n}\}_{n=1}^{N_a}$, where θ_n is the action parameters that define “how” the robot
 115 can apply the exploratory action. We further define $\theta_n \in \{\theta_P, \theta_S, \theta_C\}$, where θ_P , θ_S , and θ_C represent
 116 the action parameters for the pressing, sliding, and static contact movements respectively.

117 3.1.1. Pressing

118 The robotic system presses its sensory part on the object surfaces in order to perceive its stiffness.
 119 The pressing movement consists of pressing until a depth of d_P and holding the artificial skin for t_P
 120 seconds, i.e. $\theta_P = [d_P, t_P]$. During the pressing, the multi-modal artificial skin can record the normal
 121 force feedbacks from each normal force sensor: $\mathbf{F}_{n_f, n_s} = \{F_{n_f, n_s}^m\}_{m=1}^{t_P \cdot f_s}$ in order to measure the object
 122 stiffness, where N_f is the number of normal force sensors in one skincell (in our case $N_f = 3$), and
 123 N_s is the number of skincells in the artificial skin (in our case $N_s = 7$). Moreover, it can record the
 124 temperature feedbacks from each temperature sensor for the purpose of attaining the object thermal
 125 conductivity: $\mathbf{T}_{n_t, n_s} = \{T_{n_t, n_s}^m\}_{m=1}^{t_P \cdot f_s}$, $n_t = 1, \dots, N_t$, with N_t being the number of temperature sensors in
 126 one skincell (in our case $N_t = 1$). f_s is the sampling rate of the artificial skin, and m the sampling time
 127 step.

128 3.1.2. Sliding

129 The robot slides the artificial skin on the object surface and perceives its textural properties.
 130 To do this, the robot first builds a contact with objects with the normal force of F_S , then it linearly
 131 slides on the objects with a speed of v_S for t_S seconds, $\theta_S = [F_S, v_S, t_S]$. During sliding, the robot
 132 collects the outputs of accelerometers (in three axes: x, y, z): $\mathbf{a}_{n_a, n_s}^{(x)} = \{a_{n_a, n_s}^{(x), m}\}_{m=1}^{t_S \cdot f_s}$, $\mathbf{a}_{n_a, n_s}^{(y)} = \{a_{n_a, n_s}^{(y), m}\}_{m=1}^{t_S \cdot f_s}$,
 133 $\mathbf{a}_{n_a, n_s}^{(z)} = \{a_{n_a, n_s}^{(z), m}\}_{m=1}^{t_S \cdot f_s}$. Then the robot combines these signals together: $\mathbf{a} = \{\mathbf{a}_{n_a, n_s}\}_{n_a=1, n_s=1}^{N_a, N_s}$; $\mathbf{a}_{n_a, n_s} =$
 134 $[\mathbf{a}_{n_a, n_s}^{(x)}, \mathbf{a}_{n_a, n_s}^{(y)}, \mathbf{a}_{n_a, n_s}^{(z)}]$, $n_a = 1, \dots, N_a$, where N_a is the number of accelerometers in one skincell (in our case
 135 $N_a = 1$). Besides, the change of temperature during sliding is also collected as an extra information
 136 $\mathbf{T}_{n_t, n_s} = \{T_{n_t, n_s}^m\}_{m=1}^{t_S \cdot f_s}$.

Table 2. Exploratory actions And Perception

Exploratory actions	Action Parameters (θ)	Sensory feedbacks	Features
Pressing	d_P, t_P	\mathbf{F}, \mathbf{T}	$\bar{F}, [\bar{\mathbf{T}}, \nabla \bar{\mathbf{T}}]$
Sliding	F_S, t_S, v_S	\mathbf{a}, \mathbf{T}	$TD, [\bar{\mathbf{T}}, \nabla \bar{\mathbf{T}}]$
Static contact	d_C, t_C	\mathbf{F}, \mathbf{T}	$\bar{F}, [\bar{\mathbf{T}}, \nabla \bar{\mathbf{T}}]$

137 3.1.3. Static Contact

138 The object thermal cues can be attained by the robotic system by applying static contact movement:
 139 the robot presses its sensory part against the object surface until a depth of d_C and maintains the
 140 contact for t_C seconds, i.e. $\theta_C = [d_C, t_C]$. The normal force feedbacks and temperature feedbacks are
 141 recorded: $\mathbf{F}_{n_f, n_s} = \{F_{n_f, n_s}^m\}_{m=1}^{t_C \cdot f_s}$, $\mathbf{T}_{n_t, n_s} = \{T_{n_t, n_s}^m\}_{m=1}^{t_C \cdot f_s}$.

142 3.2. Object Physical Properties Perception

143 3.2.1. Stiffness

144 We use the normal force averaged over all normal force sensors and time steps as an indicator for
 145 the object stiffness. For the pressing movement with pressing time steps $t_P \cdot f_s$, object stiffness can be
 146 estimated by $\bar{F} = \frac{1}{t_P \cdot f_s} \frac{1}{N_f} \frac{1}{N_s} \sum_{m=1}^{t_P \cdot f_s} \sum_{n_f=1}^{N_f} \sum_{n_s=1}^{N_s} F_{n_f, n_s}^m$.

147 3.2.2. Textural Property

148 In this work, we use the same textural feature extraction method in [26]: The vibration signals
 149 \mathbf{a} in the artificial skin are used to calculate the activity, mobility and complexity, denoted as $A(\mathbf{a})$,
 150 $M(\mathbf{a})$, $C(\mathbf{a})$. We also computed the linear correlation of accelerometer signals between different
 151 directions (xy, yz, xz) denoted as $L(\mathbf{a})$. The final descriptor of textural features combines activity,
 152 mobility, complexity and linear correlation together [26]: $TD = [A(\mathbf{a}), M(\mathbf{a}), C(\mathbf{a}), L(\mathbf{a})]$.

153 3.2.3. Thermal Conductivity

154 To extract the features that describe the object thermal cues, we first calculate the average
 155 temperature sequence from all the temperature sensors: $\bar{\mathbf{T}} = \sum_{n_t=1}^{N_t} \sum_{n_s=1}^{N_s} \frac{\mathbf{T}_{n_t, n_s}}{N_t \cdot N_s}$. We then calculate its
 156 gradient at each time step as: $\nabla \bar{\mathbf{T}}$, and combine it with the average temperature sequence: $[\bar{\mathbf{T}}, \nabla \bar{\mathbf{T}}]$.
 157 To avoid curse of dimensionality, we further reduce this combination to ten dimensions via Principle
 158 Component Analysis (PCA) method and use it as the final feature to describe the object thermal
 159 conductivity.

160 Tab 2. summarizes the exploratory actions, the sensory feedbacks and the corresponding tactile
 161 features.

162 4. Transferring Prior Tactile Exploratory Action Experiences

163 This section describes our proposed transfer learning method (APTKT) in detail. First, we
 164 formulate our problem in Sec. 4.1. Then, we illustrate our transfer learning method, including its
 165 process (Sec. 4.3), what to transfer (Sec. 4.4), how to transfer (Sec. 4.5), from where to transfer, and how
 166 much to transfer (Sec. 4.6). The motivation of our method is demonstrated in Fig. 1.

167 4.1. Problem Formulation

168 Assume that a robotic system has gained prior tactile knowledge of some *old* objects, on which
 169 the robot has previously applied different exploratory actions with different action parameters. These
 170 prior exploratory action experiences consist of the feature observations perceived by the multiple

171 sensors and observation models from the old objects. Now, the robot is tasked to learn about a set of
 172 *new* objects. Since the old objects might share some similar physical properties with the new objects,
 173 by leveraging the related tactile exploratory action experiences, the robot can learn about new objects
 174 more efficiently.

175 We define N_{new} number of new objects ($C^{\text{new}} = \{c_j^{\text{new}}\}_{j=1}^{N_{\text{new}}}$) the robot is tasked to efficiently
 176 learn about through different exploratory actions $A = \{\alpha_n^{\theta_n}\}_{n=1}^{N_\alpha}$ (For simplicity, we will denote α as
 177 an exploratory action in the rest of the paper). In other words, the robot should actively attain object
 178 feature observations ($V_\alpha^{\text{new}} = \{V_{c_1}^{\text{new}}, V_{c_2}^{\text{new}}, \dots, V_{c_{N_{\text{new}}}}^{\text{new}}\}$) for each exploratory action α and construct
 179 reliable observation models $V_\alpha^{\text{new}} \xrightarrow{f_\alpha^{\text{new}}} C^{\text{new}}$. We further define the robot prior tactile experience for
 180 an exploratory action α for N_{old} number of prior objects ($C^{\text{old}} = \{c_i^{\text{old}}\}_{i=1}^{N_{\text{old}}}$) as the prior object feature
 181 observations ($V_\alpha^{\text{old}} = \{v_{c_1}^{\text{old}}, v_{c_2}^{\text{old}}, \dots, v_{c_{N_{\text{old}}}}^{\text{old}}\}$) and the observation models of old objects $V_\alpha^{\text{old}} \xrightarrow{f_\alpha^{\text{old}}} C^{\text{old}}$.
 182 These feature observations are collected by the multiple tactile sensors from the artificial robotic skin.

183 We formulate our problem as the transfer learning in the Gaussian Process Classification (GPC)
 184 framework [28], where each object is regarded as a class, and for each exploratory action, a GPC model
 185 is built as the observation model. The robot iteratively applies the exploratory actions and leverages
 186 prior tactile knowledge to improve the GPC observation models of new objects.

187

188 4.2. Gaussian Process Classification

189 The Gaussian Process Classification (GPC) model describes the mapping between the observation
 190 set X and the output set Y by: $X \xrightarrow{f} Y$. The latent function $g(\mathbf{x})$ in the GPC model is assumed
 191 to be sampled from a high-dimensional gaussian distribution called GP prior [28]: $g(\mathbf{x}) \sim$
 192 $\mathcal{GP}(m(\mathbf{x}), K(\mathbf{x}, \mathbf{x}'))$, where each sample $g(\mathbf{x}_i)$ is a random variable. In this work, we use one-vs-all
 193 multi-class classification. For each object class, a binary GPC whose output label is converted to
 194 $\{-1, +1\}$ is trained for each of the N labels: $f_n(\cdot)$. Given a new sample \mathbf{x}^* , each binary classifier
 195 predicts the observation probability of its label $p(y_n|\mathbf{x}^*)$. The sample is assigned to the class with the
 196 largest prediction probability $y^* = \arg \max_{y_n \in Y} p(y_n|\mathbf{x}^*)$.

197 4.3. Process

198 The robot following our proposed method first applies each exploratory action one time on each
 199 new object, in order to collect a small number of feature observations $V^{\text{new}} = \{V_{\alpha_n}^{\text{new}}\}_{n=1}^{N_\alpha}$ (Initial
 200 data collection). Then, the robot reuses its prior tactile exploratory action experiences to improve the
 201 observation models for *each* new object (Initial prior knowledge transfer). During this process, the
 202 robot compares the relatedness between its prior tactile exploratory action experiences and the new
 203 objects (Sec. 4.6), and chooses the most related one to transfer the old object feature observations V^{old}
 204 (Sec. 4.5). Afterwards, the robot begins to iteratively collect and combine the feature observations and
 205 update the prior tactile knowledge in order to improve the observation models. At each iteration of
 206 prior tactile knowledge updating, the robot (1) actively selects the next object and the next exploratory
 207 action in order to attain a new feature observation, and (2) updates the prior tactile knowledge *only*
 208 for the selected exploratory action. The iteration terminates when there is no improvement in the
 209 observation models of new objects. Our algorithm is demonstrated by Fig. 4.

210 4.4. What to Transfer

211 When the robotic system applies an exploratory action on objects, it perceives multiple feature
 212 observations (e.g. by the pressing movement, the robot can perceive the object stiffness and thermal
 213 conductivity). The prior tactile exploratory action experiences are built using the prior objects feature
 214 observations from multiple sensory modalities that are combined together and the corresponding GPC
 215 observation models of prior objects.

Algorithm 1 multiple feature observations combination

Input : $C = \{c_j\}_{j=1}^{N_c}$ $\triangleright N_c$ number of objects, each object is regarded as a class.
 $A = \{\alpha_n\}_{n=1}^{N_\alpha}$ $\triangleright N_\alpha$ number of exploratory actions with different action parameters
 $V = \{V_{\alpha_n, c_j}\}_{n=1, j=1}^{N_\alpha, N_c}$ \triangleright feature observations

Output: $\gamma = \{\gamma_{\alpha_n, c_j}^{(m_\alpha)}\}_{\alpha_n=1, m_\alpha=1, j=1}^{N_\alpha, M_\alpha, N_c}$ \triangleright Estimated sensory feedback weights.

- 1 **for** $j = 1 : N_c$ **do**
- 2 **for** $n = 1 : N_\alpha$ **do**
- 3 $K'_{\alpha_n} \leftarrow \gamma_{\alpha_n}^{(1)} K^{(1)} + \dots + \gamma_{\alpha_n}^{(M_{\alpha_n})} K^{(M_{\alpha_n})}$ \triangleright Linear kernel combination.
- 4 $\{\gamma_{\alpha_n, c_j}^{(m_\alpha)}\}_{m_\alpha=1}^{M_{\alpha_n}} \leftarrow \text{optimizeGPC}(K'_{\alpha_n}, V_{\alpha_n, c_j})$ \triangleright Finding optimal weights.
- 5 **end**
- 6 **end**

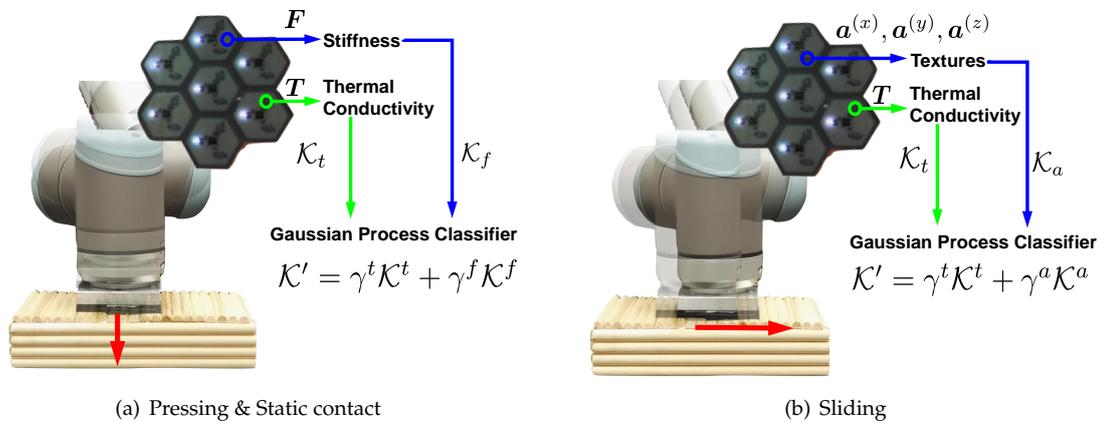


Figure 5. Illustration of multiple feature observations combination method. **(a)** The robotic system combines the normal force sensing and temperature sensing to learn about objects by applying pressing and static contact movements. **(b)** The robot slides on the object surface to sense its textural property and thermal conductivity.

222 4.5. How to Transfer

We now describe how the robotic system transfers the feature observations of a prior object c_i^{old} to learn the GPC observation model of a new object c_j^{new} , based on an exploratory action \mathbf{f} . For simplicity, we hereby refer to i and j as c_i^{old} and c_j^{new} , respectively. We define $\mathbf{g}_i^{\text{old}}$ as the Gaussian Process latent function values [28] for the old object c_i^{old} and $\mathbf{g}_j^{\text{new}}$ for the new object c_j^{new} . We assume that these two function values are not independent from each other, but are sampled together over a dependent Gaussian Prior (GP). This dependent GP is then used to construct the GPC observation model of the new object. The latent function can be modified accordingly: $\mathbf{g}_j^{\text{new}'} \leftarrow [\mathbf{g}_i^{\text{old}}, \mathbf{g}_j^{\text{new}}]$. We further incorporate the relatedness between prior object and new object into the dependent GP model by introducing the following dependent kernel function:

$$K' = \begin{bmatrix} K(V_i^{\text{old}}, V_i^{\text{old}}) & \lambda K(V_i^{\text{old}}, V_j^{\text{new}}) \\ \lambda K(V_j^{\text{new}}, V_i^{\text{old}}) & K(V_j^{\text{new}}, V_j^{\text{new}}) \end{bmatrix} \quad (2)$$

223 $K(\cdot, \cdot)$ serves as the basic kernel function that measures the similarity between two feature
 224 observations that belong to the old object and the new object, respectively. $\lambda K(\cdot, \cdot)$ measures the
 225 feature observations between the old object and the new object. λ controls the relatedness between

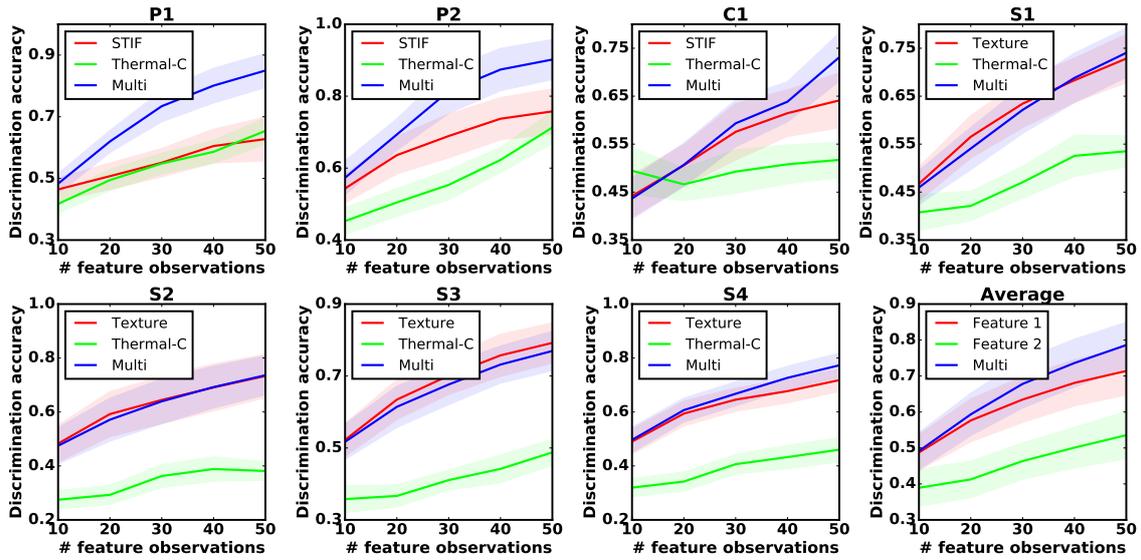


Figure 6. Multiple feature observations combination results for exploratory actions $P1$, $P2$, $C1$, $S1$, $S2$, $S3$, $S4$ and the averaged result. STIF: building the GPC observation model based on object stiffness; Thermal-C: thermal conductivity; Texture: object surface textural properties; Multi: combined feature observations. The horizontal axis represents the number of feature observations. The vertical axis represents the discrimination accuracy of the test dataset.

226 c_i^{old} and c_j^{new} . We constrain its range within $[0, 1]$. As Chai *et al.* [29] evaluated, $\lambda = 0$ indicates that the
 227 old object and the new object are not related, while $\lambda = 1$ indicates that the two objects are the same.

228 4.6. From Where and How Much to Transfer

Sec. 4.5 describes how to transfer the prior tactile knowledge to learn about new objects. This section illustrates how the robotic system selects the most related old object (from where to transfer) and how to determine the relatedness (λ) between two objects (how much to transfer). To do this, we take advantage of the prediction from the GPC observation models of old objects. Let $p(c_i^{\text{old}} | \mathbf{v}_j^{\text{new}})$ be the prediction probability that a feature observation from the new object $\mathbf{v}_j^{\text{new}}$ is assigned to the old object c_i^{old} . We measure the average prediction to all the observations $\mathbf{v}_j^{\text{new}} \in V_j^{\text{new}}$ that belong to the new object: $\bar{p}(c_i^{\text{old}} | V_j^{\text{new}}) = \frac{1}{N_j^{\text{new}}} \sum p(c_i^{\text{old}} | \mathbf{v}_j^{\text{new}})$, with N_j^{new} being the number of new object feature observations. This average prediction value indicates the similarity between the old object c_i^{old} and the new object c_j^{new} . A larger value indicates that these two objects are highly similar. Therefore, we can use it to select the most related old object (denoted as c^{old^*}) for a new object regarding the exploratory action \mathbf{ff} . Furthermore, to avoid transferring irrelevant tactile information, we add a threshold ϵ_{neg} which prevents the robot from selecting any old object when the prediction value is smaller than ϵ_{neg} . The final old object selection criterion is:

$$c^{\text{old}^*} = \begin{cases} \arg \max_{c_i^{\text{old}} \in C^{\text{old}}} \bar{p}(c_i^{\text{old}} | V_j^{\text{new}}), & \text{if } \bar{p}(c^{\text{old}^*} | V_j^{\text{new}}) \geq \epsilon_{\text{neg}} \\ \text{None,} & \text{otherwise} \end{cases} \quad (3)$$

229 Once we select c^{old^*} , we further use the predictions from the observation model of old objects to
 230 determine λ^* : $\lambda^* = \bar{p}(c^{\text{old}^*} | V_j^{\text{new}})$.

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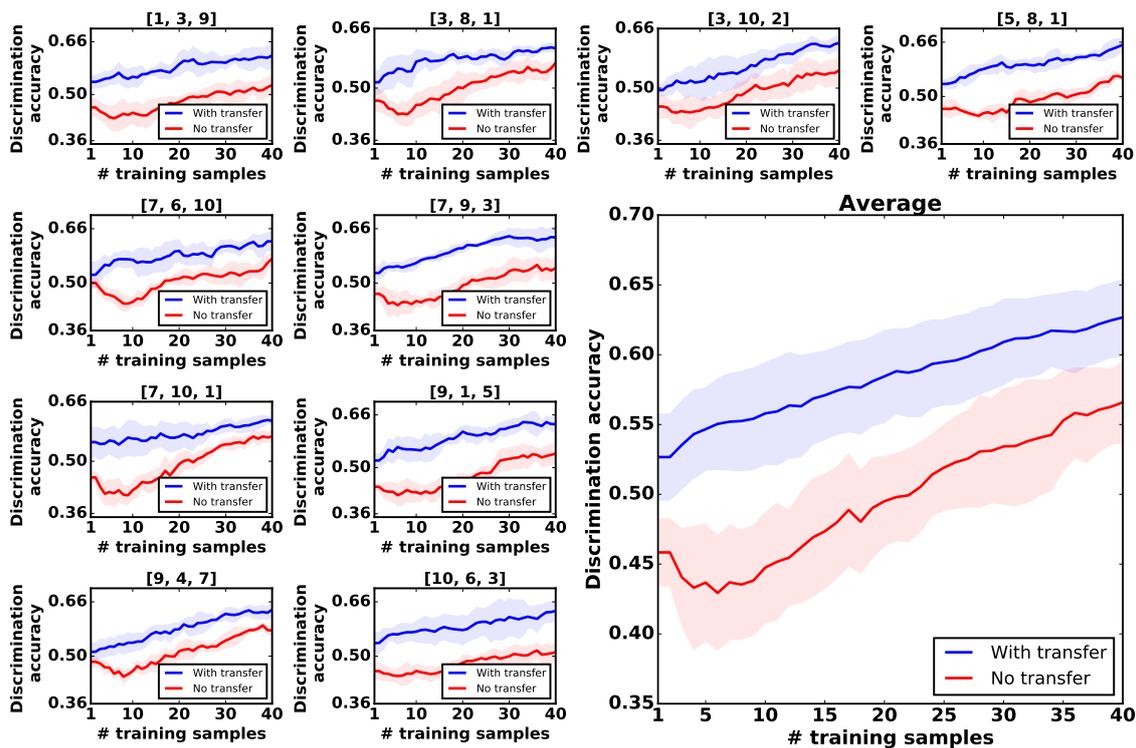


Figure 7. Transferring the exploratory actions experiences from three old objects. The small plots show the learning process from 10 groups of old objects. The large plot on the right shows the averaged results. Horizontal axis: the growing number of feature observations the robot collected. Vertical axis: the discrimination accuracy of the test dataset.

232 4.7. Evaluation of Multiple Feature Observations Combination Method

233 4.8. Prior Exploratory Action Experiences Update

234 When the robot updates its prior exploratory action experiences, it needs to iteratively collect
 235 a new feature observation by applying an exploratory action on an object. We use the Active Touch
 236 for Learning Physical Properties (AT-LPP) algorithm proposed in [26] so that the robot actively
 237 decides which new object to explore next (denoted as c^{new^*}) and which exploratory action to apply
 238 next (denoted as ff^*). Once the robot collects a new feature observation, it updates the prior tactile
 239 exploratory action experiences only from action ff^* . This process includes updating the feature
 240 observation combination, updating the object relatedness λ , and transferring these prior feature
 241 observations to the observation models of new objects.

242 5. Experimental Results

243 5.1. Experimental Objects

244 In order to evaluate the performance of APTKT, we deliberately selected 10 daily objects
 245 with different physical properties which served to build the robotic prior tactile exploratory action
 246 experiences (see Fig. 1 *Prior objects*). Furthermore, we selected five new objects about which the robotic
 247 system was tasked to learn (Fig. 1 *New objects*). For each new object, there existed one or more old
 248 objects that shared similar physical properties. For example, both rough sponge and smooth sponge
 249 are soft; paper box and hard box have similar surface textures; metal toolbox and biscuit box have high

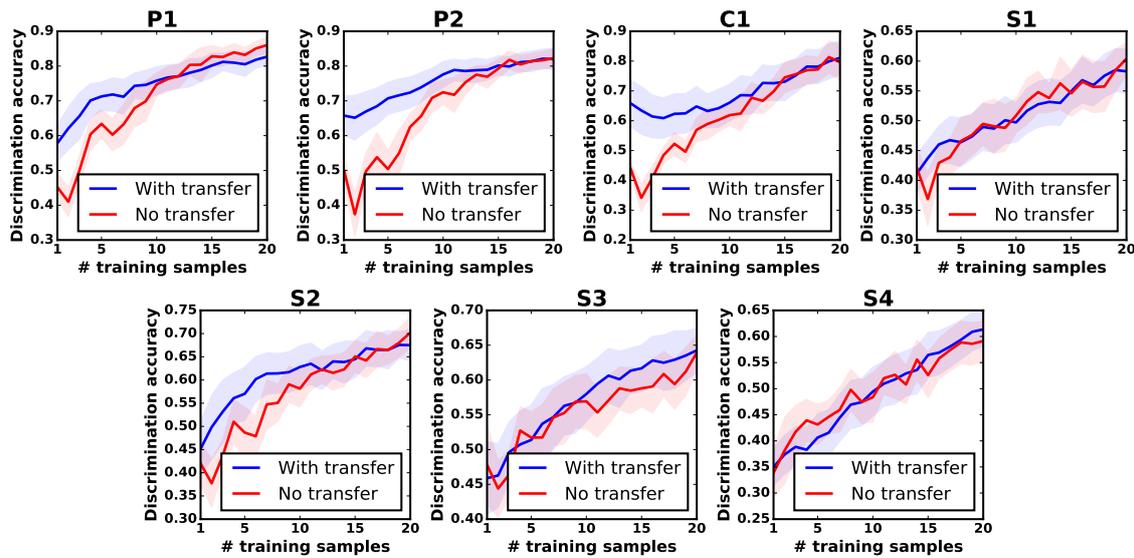


Figure 8. Transfer learning using only one exploratory action.

250 thermal conductivity. In this way, when learning about new objects based on their physical properties,
 251 the robot can leverage the related prior tactile instance knowledge.

252 5.2. Exploratory Action Determination and Test Data Collection

253 In our experiment, we defined seven exploratory actions from the pressing, sliding, and static
 254 contact movements with various action parameters (Pressing: P1, $d_p = 1$ mm, $t_p = 3$ s; P2, $d_p = 2$
 255 mm, $t_p = 3$ s. Sliding: S1, $F_S = 0.1$ N, $t_S = 5$ s, $v_S = 1$ cm/s; S2, $F_S = 0.1$ N, $t_S = 1$ s, $v_S = 5$ cm/s;
 256 S3, $F_S = 0.2$ N, $t_S = 5$ s, $v_S = 1$ cm/s; S4, $F_S = 0.2$ N, $t_S = 1$ s, $v_S = 5$ cm/s. Static Contact: C1,
 257 $d_C = 2$ mm, $t_C = 15$ s). Before applying any of the 7 exploratory actions, the robot established light
 258 contact with the objects which, detected once the total normal force on the the artificial skin increased
 259 above 0.05 N. Furthermore, after applying an exploratory action, the robot was controlled to raise its
 260 end-effector for 30 s such that the temperature sensors could be restored to the ambient temperature.

261 We evaluated the performance of our proposed method based on a test dataset built by the robot
 262 by applying each actions 20 times on each object. During this process, objects were manually shifted
 263 and rotated so that the data was robust against the variations in the object contact locations with the
 264 artificial skin.

265 We first evaluated the performance of our proposed robotic multiple feature observation
 266 combination algorithm. To do this, the robot selected 10 groups of objects (shown in Fig. 1) to construct
 267 the GPC observation models for each of the seven exploratory actions. Each group contained five
 268 objects that were selected randomly from the old and new object lists, following a uniform distribution.
 269 The algorithm performance was evaluated by the discrimination accuracy of the test dataset predicted
 270 by the GPC models with the growing number of feature observations. We compared our method with
 271 the baseline methods that built the GPC models using only a single sensor modality.

272 The experiments were conducted 10 times for each object group. For a fair comparison, we used
 273 RBF kernel [28] for each sensor modality. Results are plotted in Fig. 6. For all seven exploratory actions,
 274 our proposed algorithm either took advantage of combining different sensor modalities to reach the
 275 best discrimination accuracy (P1, P2, C1, S4 in Fig. 6), or performed the same as the best single-sensor
 276 result (S1, S2, S3 in Fig. 6), indicating that the robot actively selected the most informative sensory
 277 feedback to learn about objects.

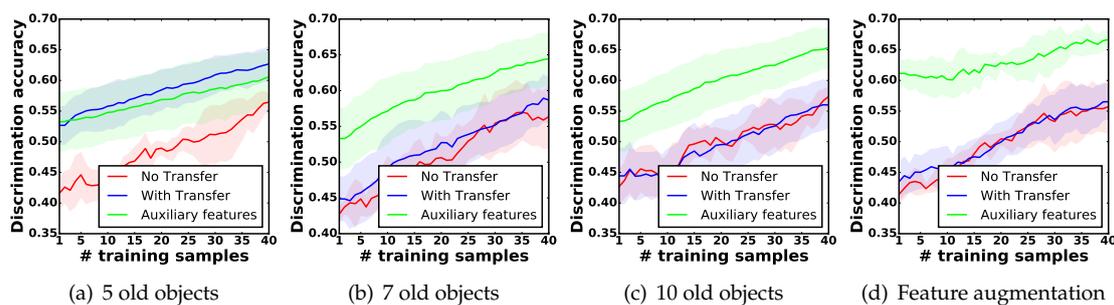


Figure 9. Increasing the number of old objects from 3, 5, 7 to 10, and comparing the performance of different learning methods. Red: baseline method; Blue: APTKT without auxiliary features; Green: APTKT with auxiliary features.

278 5.3. Evaluation of the Transfer Learning Method with Different Groups of Prior Objects

279 In this experiment, we evaluated the performance of APTKT with different groups of prior objects.
 280 To start the learning process, the robot applied each of the seven actions once on each new object.
 281 When the robot iteratively learned the new objects' physical properties, it updated both the multiple
 282 feature observations combination and the prior tactile knowledge built by the dependent GPC models
 283 with all the feature observations collected so far. At each learning iteration, we measured the object
 284 discrimination accuracy of the test dataset. The transfer learning performance was compared with the
 285 learning process without prior knowledge as the baseline method.

286 We randomly shuffled the prior objects into ten groups. Each group consisted of the feature
 287 observations and the observation models from three prior objects. We conducted the experiment
 288 with five trials for each group. In each trial, the robot followed the transfer learning approach and
 289 no-transfer approach to collect 40 feature observations in total, allowing a fair comparison between
 290 different learning strategies to be made. Fig. 7 illustrates that with the help of prior knowledge, the
 291 robot consistently outperformed the learning process without prior knowledge with a discrimination
 292 accuracy of 10%. In order to further evaluate the robustness of APTKT, the robot was tasked to learn
 293 about objects via applying only *one* of the exploratory actions. The experimental procedure was the
 294 same as the one described above. The results are shown in Fig. 8. As can be seen, by actions P1, P2
 295 and C1, The robot had a larger improvement than actions S1, S2, S3 and S4. For example, the robot
 296 increased the discrimination accuracy by 25%, when it reused the prior tactile instance knowledge from
 297 the movement P2. However, when learning about objects by actions S1 and S4, little improvement
 298 was seen. This was due to the fact that different exploratory actions produced different object feature
 299 observations. For action P2, there existed higher related prior tactile knowledge than S1 and S4, and
 300 the robot could benefit more on it.

301 In all scenarios, using our proposed transfer learning algorithm, the robot could achieve a higher
 302 discrimination accuracy than the baseline method with the same number of feature observations.
 303 Therefore, we can conclude that APTKT helps the robot build reliable observation models of new
 304 objects with fewer training samples, even when only one kind of the exploratory action is applied.

305 5.4. Increasing the Number of Prior Objects

306 We further evaluated the performance of our proposed method with an increasing number of
 307 prior tactile experiences. Intuitively, as the number of old objects grows, it is more likely that the robot
 308 can find highly-related prior tactile knowledge, so that the learning performance can continue to be
 309 improved. In this regard, following the same procedure described above, we increased the number
 310 of old objects from 5, 7 to 10 and conducted each experiment five trials. Unexpectedly, as Fig. 9(b),
 311 Fig. 9(c) and Fig. 9(d) shows, the growing number of prior tactile knowledge reduced the transfer

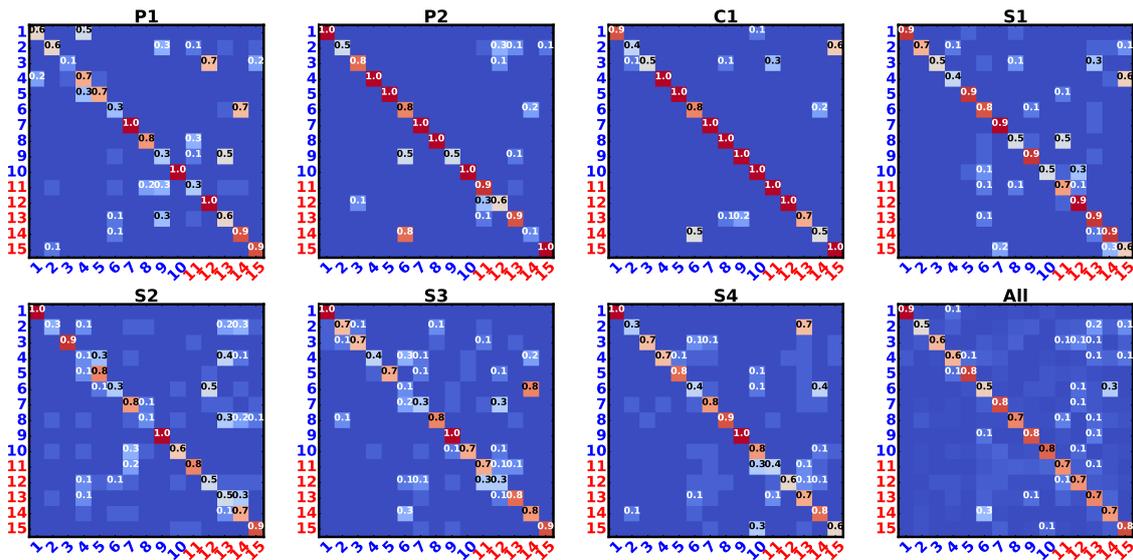


Figure 10. object confusion matrices (value normalized between 0 and 1) for each exploratory action and the average. The blue indices represent the old objects. The red indices represent the new objects, with #11 - #15 indicating new objects #1 - #5. Best viewed in magnification.

312 learning improvement. This was because the object relatedness ρ predicted by the old object GPC
 313 models was underestimated, when there existed many old objects.

To compensate for this, we proposed using a feature augmentation trick that utilized the predictions as auxiliary features to describe the physical properties of the objects. We defined $p(c_i^{\text{old}}|\mathbf{v})$ as the prediction probability that a feature observation from the new object \mathbf{v} is assigned to the old object c_i^{old} . Then we augmented a feature observation \mathbf{v} from a new object as:

$$\mathbf{v}' = \left[\underbrace{\mathbf{v}}_{\text{original features}}, \underbrace{p(c_1^{\text{old}}|\mathbf{v}), \dots, p(c_i^{\text{old}}|\mathbf{v}), \dots, p(c_{N_{\text{old}}}^{\text{old}}|\mathbf{v})}_{\text{predictions from old objects' observation models}} \right]. \quad (4)$$

314 The auxiliary features $[p(c_1^{\text{old}}|\mathbf{x}), \dots, p(c_{N_{\text{old}}}^{\text{old}}|\mathbf{x})]$ can be regarded to be perceived from an auxiliary
 315 sensor. Therefore, we directly employed our proposed multiple feature observation combination
 316 method to the augmented feature observations by casting a weight to its kernel. The augmented
 317 feature observations were then used to build the new object dependent GPC models.

318 We tested our proposed feature augmentation technique when the robot leveraged 3, 5, 7, and 10
 319 prior objects' prior tactile knowledge to learn about new objects via all seven actions. The learning
 320 performance is shown by the green curves in Fig. 9(a) - Fig. 9(d). Clearly, by introducing the probability
 321 predictions as auxiliary features, the robot was able to reuse the prior tactile knowledge again, and
 322 achieved similar improvement of discrimination accuracy for 3 prior objects, and higher improvement
 323 for 5, 7, and 10 prior objects compared to the other methods. Specifically, when reusing 10 prior objects,
 324 the robot achieved 20% higher discrimination accuracy than the baseline method, when only *one* new
 325 feature observation was collected, showing the one-shot learning behaviour. This experiment also
 326 indicates that with a further growing number of prior objects, a further improvement of discrimination
 327 accuracy is achievable.

328 5.5. Negative Prior Tactile Knowledge Transfer Testing

329 When the constructed prior tactile exploratory action experiences are not relevant to the new
 330 objects, a brute-force transfer may degrade the learning performance, resulting in the negative

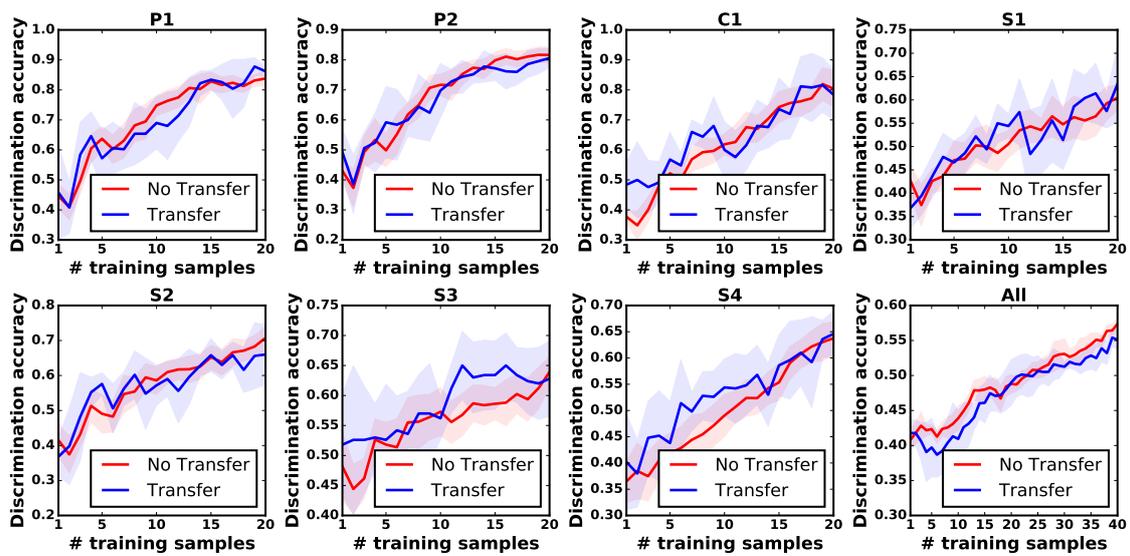


Figure 11. Negative prior tactile knowledge transfer testing. The prior objects were deliberately selected that were unrelated to the new objects.

331 knowledge transfer phenomena. In this case, the transfer learning algorithm should stop leveraging
 332 irrelevant prior knowledge.

333 In order to evaluate APTKT against the negative tactile knowledge transfer, we deliberately
 334 selected irrelevant prior objects and compared the transfer learning performance with the baseline
 335 method, following the same experiment process described in Sec. 5.3. When finding which objects
 336 were relevant (or irrelevant) to each other, we built object confusion matrices to roughly evaluate the
 337 object similarity. To do this, for each of the seven exploratory actions, we trained a Gaussian Mixture
 338 Model (GMM) and calculated the object confusion matrix. We further calculated the confusion matrix
 339 averaged over all exploratory actions. The results are shown in Fig. 10. According to Fig. 10, objects
 340 {1, 5, 7} were dissimilar to the new objects (objects {11 - 15}) regarding the exploratory movement P1,
 341 objects {1, 4, 7} for P2, objects {4, 7, 10} for C1, objects {1, 6, 9} for S1, objects {1, 7, 10} for S2, objects {1,
 342 3, 9} for S3, and objects {1, 3, 8} for S4. We thus used these objects as prior objects to test the transfer
 343 learning performance via the single exploratory action. We further selected objects {1, 5, 10} to test the
 344 learning process via all exploratory actions, since these three objects shared relative small similarity to
 345 the new objects.

346 The results in Fig. 11 illustrate that the discrimination accuracy achieved by APTKT was similar
 347 to the baseline method, when the robot applied either one or all seven exploratory actions. The results
 348 indicate that our proposed algorithm stopped transferring negative prior tactile instance knowledge.

349 6. Conclusions

350 In this work, we proposed a transfer learning method for a robot equipped with multi-modal
 351 artificial skin to actively reuse the prior tactile exploratory action experiences when learning about
 352 the detailed physical properties of new objects. These prior action experiences are built by the
 353 feature observations, when a robotic arm equipped with a multi-modal artificial skin applies the
 354 pressing, sliding and static contact movements with different action parameters on objects. The feature
 355 observations are perceived from multiple sensory modalities. Using our proposed tactile transfer
 356 learning method, the robot has a “warm start” of the learning process. It applies fewer exploratory
 357 actions and gains a more precise tactile knowledge of new objects.

358 In the future, we will extend our method to more exploratory actions (such as tapping and lifting),
 359 so that the robot can transfer more exploratory action experiences to learn more physical properties

360 of an object, such as auditory feedback and center of mass. Furthermore, it would be an interesting
361 topic to research how to transfer the prior tactile knowledge across different exploratory actions, e.g.
362 transferring the tactile knowledge from pressing to static contact movement.

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