

1 Article

2 Classifying induced superconductivity in atomically 3 thin Dirac-cone materials

4 Evgueni F. Talantsev^{1,2,*}5 ¹ M. N. Miheev Institute of Metal Physics, Ural Branch, Russian Academy of Sciences, 18, S. Kovalevskoy St.,
6 Ekaterinburg, 620108, Russia; evgeny.talantsev@imp.uran.ru7 ² NANOTECH Centre, Ural Federal University, 19 Mira St., Ekaterinburg, 620002, Russia;
8 evgeny.talantsev@urfu.ru

9 * Correspondence: evgeny.talantsev@imp.uran.ru; Tel.: +007-912-676-0374

10

11 **Abstract:** Recently, Kayyalha *et al.* (*Phys. Rev. Lett.*, **2019**, 122, 047003) reported on anomalous
12 enhancement of the self-field critical currents, $I_c(sf, T)$, at low temperatures in Nb/BiSbTeSe₂-
13 nanoribbon/Nb Josephson junctions. The enhancement was attributed to the low-energy Andreev
14 bound states arising from winding of the electronic wave function around the circumference of the
15 topological insulator BiSbTeSe₂ nanoribbon. In this paper, we show that identical enhancement in
16 $I_c(sf, T)$ and in the upper critical field, $B_{c2}(T)$, at approximately same reduced temperatures, were
17 reported by several research groups in atomically thin junctions based on a variety of Dirac-cone
18 materials (DCM) earlier. Our analysis shows that in all these S/DCM/S systems the enhancement is
19 due to a new superconducting band opening. Taking in account that several intrinsic
20 superconductors also exhibit the effect of new superconducting band(s) opening when sample
21 thickness becomes thinner than the out-of-plane coherence length, $\xi_c(0)$, we strength our previous
22 proposal that there is a new phenomenon of additional superconducting band(s) opening in
23 atomically thin films.

24 **Keywords:** superconductivity enhancement in atomically thin films; Dirac-cone materials; single
25 layer graphene; Josephson junctions; multiple-band superconductivity

26

27

1. Introduction

28 Intrinsic superconductors can be grouped in 32 classes under “conventional”, “possibly
29 unconventional” and “unconventional” categories according to the mechanism believed to give rise
30 to superconductivity [1]. Despite some differences, all intrinsic superconductors can induce
31 superconducting state in non-superconducting materials by the Holm-Meissner effect [2] (also
32 designates as the proximity effect [3,4]). As direct consequence of this, non-dissipative transport
33 current can flow through the non-superconducting material in superconductor/non-
34 superconductor/superconductor (S/N/S) junctions. The amplitude of this non-dissipative transport
35 current at self-field conditions (when no external magnetic field is applied), $I_c(sf, T)$, was given by
36 Ambegaokar and Baratoff (AB) [5,6]:

$$I_c(sf, T) = \frac{\pi \Delta(T)}{2e \cdot R_n} \cdot \tanh\left(\frac{\Delta(T)}{2k_B T}\right), \quad (1)$$

37 where $\Delta(T)$ is the temperature-dependent superconducting gap, e is the electron charge, R_n is the
38 normal-state tunneling resistance in the junction, and k_B is the Boltzmann constant.

39 Many interesting physical effects are expected if non-superconducting part of S/N/S junction
40 will be made of single-layer graphene (SLG) [7], multiple-layer graphene (MLG) [8], graphene-like
41 materials [9], and many other new 2D- and nano-DCMs which are under on-going
42 discover/invent/exploration stage now [10-39]. One certainly interesting class of S/N/S junctions is
43 when non-superconducting part of the device made of topological insulators (TI) [40-47].

44 Temperature dependent self-field critical currents, $I_c(sf, T)$ in this class of junctions were first reported
 45 by Veldhorst *et al.* in Nb/Bi₂Te₃/Nb [18], and later by Kurter *et al.* in Nb/Bi₂Se₃/Nb [19], by Charpentier
 46 *et al.* in Al/Bi₂Te₃/Al [42], and by other research groups in different systems (extended reference list
 47 for studied S/TI/S junctions can be found in Refs. 45,46).

48 Recently, Kayyalha *et al.* [48] report on anomalous enhancement of $I_c(sf, T)$ in Nb/BiSbTeSe₂-
 49 nanoribbon/Nb junction at temperatures of $T \leq 0.25 \cdot T_c$. They confirmed the effect in all five studied
 50 junctions [48], for which TI parts were made of BiSbTeSe₂ flakes with thicknesses, $2b$, varied from 30
 51 nm to 50 nm, and flakes widths, $2a$, varied from 266 nm to 390 nm. We note, that in all these S/TI/S
 52 junctions, BiSbTeSe₂-nanoribbons thicknesses and widths were smaller than the ground state
 53 superconducting coherence length, $2b \ll 2a < \xi_c(0) \sim 600$ nm in these devices [48]. For one junction,
 54 made of wider BiSbTeSe₂-nanoribbon, $2a = 4 \mu\text{m}$ (Fig. S4 of Supplementary Information of Ref. [48]),
 55 measurements were performed only at low temperatures, $T < 2$ K, which is about $T < 0.2 \cdot T_c$ (if we take in
 56 account, that Nb has $T_c = 8.9\text{-}9.6$ K [49]), and, thus, more experimental studies are required for this 4-
 57 μm wide Nb/BiSbTeSe₂-nanoribbon/Nb junction to see the $I_c(sf, T)$ enhancement.

58 Here we need to stress, that identical $I_c(sf, T)$ enhancement (or, in another words, $I_c(sf, T)$ upturn
 59 [12]) at approximately the same reduced temperature of $T \leq 0.25 \cdot T_c$ in atomically-thin S/N/S junction
 60 was first reported by Calado *et al.* [12] in MoRe/SLG/MoRe junction in 2015. One years later, less
 61 prominent $I_c(sf, T)$ enhancement (however, which is still very clearly visible in raw experimental data
 62 [50]), in nominally the same MoRe/SLG/MoRe junctions at $T \leq 0.25 \cdot T_c$ was reported by Borzenets *et al.*
 63 [15]. Based on this, it will be incorrect to attribute the $I_c(sf, T)$ enhancement at low reduced
 64 temperatures in Nb/BiSbTeSe₂-nanoribbon/Nb [48] to unique property of S/TI/S junctions.

65 In addition, this is important to mention that Kurter *et al.* [19] were the first who reported $I_c(sf, T)$
 66 enhancement in S/TI/S junction at reduced temperature of $T \leq 0.25 \cdot T_c$. In their Nb/Bi₂Se₃/Nb junctions,
 67 Bi₂Se₃ flake has thickness of $2b = 9$ nm, and, thus, the condition of $2b < \xi_c(0)$ was also satisfied.

68 In overall, as S/TI/S [19,48], as S/SLG/S [12,15], studied junctions, for which the effect of the low-
 69 temperature $I_c(sf, T)$ enhancement was observed have non-superconducting parts thinner than the
 70 ground state out-of-plane coherence lengths, $\xi_c(0)$. Truly, SLG thickness is $2b = 0.4\text{-}1.7$ nm [50] and
 71 thus the condition of $2b \ll \xi_c(0)$ satisfies for any SLG-based junctions.

72 We have to note that several intrinsic superconductors exhibit multiple-band superconducting
 73 gapping [50,52] and the enhancement of the transition temperature [52-59] when the condition of $2b$
 74 $< \xi_c(0)$ [52] is satisfied. The first discovered material in this class of superconductors is atomically thin
 75 FeSe [53-55] in which 13-fold increase (i.e., 100 K vs 7.5 K) was experimentally registered to date.
 76 Another milestone experimental finding in this field was reported by Liao *et al.* [9] who observed the
 77 effect of new superconducting band opening and T_c enhancement in few layer stanene (which is the
 78 closest counterpart of graphene) by tuning the films thicknesses. To date, maximal T_c increase due to
 79 the effect [52], stands with another single-atomic layer superconductor, $T_d\text{-MoTe}_2$, for which Rhodes
 80 *et al.* [59] reported 30-fold T_c increase when samples were thinning down to single atomic layer.

81 In this paper we report results of our analysis of temperature dependent self-field critical
 82 currents, $I_c(sf, T)$, in Nb/BiSbTeSe₂-nanoribbon/Nb [48] and Nb/(Bi_{0.06}Sb_{0.94})₂Te₃/Nb [60] junctions, and
 83 of the upper critical field, $B_{c2}(T)$, in Sn/SLG/Sn junctions [61] and show that a new superconducting
 84 band opening phenomenon in atomically thin superconductors, which we proposed earlier [50,52],
 85 has got further experimental supports.

86 2. Models description

87 In our previous work [50], we proposed to substitute $\Delta(T)$ in Eq. 1 by analytical expression
 88 proposed by Gross *et al.* [62]:

$$\Delta(T) = \Delta(0) \tanh\left(\frac{\pi k_B T_c}{\Delta(0)} \sqrt{\eta \left(\frac{\Delta C}{C}\right) \left(\frac{T_c}{T} - 1\right)}\right), \quad (2)$$

89 where $\Delta(0)$ is the ground-state amplitude of the superconducting band, $\Delta C/C$ is the relative jump in
 90 electronic specific heat at the transition temperature, T_c , and $\eta = 2/3$ for s-wave superconductors [62].

91 In result, T_c , $\Delta C/C$, $\Delta(0)$, and normal-state tunneling resistance, R_n , of the S/N/S junction can be
 92 deduced by fitting experimental $I_c(sf, T)$ dataset to Eq. 1 (full expression for Eq. 1 is given in Ref. 50).

93 In Ref. 50 we showed that S/SLG/S and S/Bi₂Se₃/S junctions exhibit two-decoupled band
 94 superconducting state, for which, for general case of multiple-decoupled bands, temperature-
 95 dependent self-field critical current, $I_c(sf, T)$, can be described by the equation:

$$I_c(sf, T) = \sum_{i=1}^N \frac{\pi \Delta_i(T)}{2eR_{n,i}} \cdot \theta(T_{c,i} - T) \cdot \tanh\left(\frac{\Delta_i(T)}{2k_B T}\right), \quad (3)$$

96 where the subscript i refers to the i -band, $\theta(x)$ is the Heaviside step function, and each band has its
 97 own independent parameters of $T_{c,i}$, $\Delta C_i/C_i$, $\Delta_i(0)$, and $R_{n,i}$.

98 We should note that multiple-band induced superconductivity in junctions should be detectable
 99 by any technique which is sensitive to additional bands crossing the Fermi surface, for instance
 100 multiple distinct gaps should be evident in the temperature-dependence of the upper critical field,
 101 $B_{c2}(T)$, for which general equation is:

$$B_{c2}(T) = \sum_{i=1}^N B_{c2,i}(T) \cdot \theta(T_{c,i} - T), \quad (4)$$

102 where, within each i -band, the upper critical field can be described by known model. In our study,
 103 we utilize four $B_{c2}(T)$ model to show that main result is model-independent. For instance, we use:

104 1. Two-fluid Gorter-Casimir (GC) model [63,64]:

$$B_{c2}(T) = \sum_{i=1}^N \left[B_{c2,i}(0) \cdot \left(1 - \left(\frac{T}{T_{c,i}}\right)^2\right) \cdot \theta(T_{c,i} - T) \right] = \frac{\phi_0}{2\pi} \cdot \sum_{i=1}^N \left[\frac{\theta(T_{c,i} - T)}{\xi_i^2(0)} \cdot \left(1 - \left(\frac{T}{T_{c,i}}\right)^2\right) \right], \quad (5)$$

105 where $\phi_0 = 2.068 \cdot 10^{-15}$ Wb is flux quantum, $\xi_i(0)$ is the ground state in-plane coherence length of the i -
 106 band. This model is a wide use for single-band superconductors ranging from 3D near-room-
 107 temperature superconducting hydrides [65-68] to 2D superconductors [54,55,61,69].

108 2. Jones-Hulm-Chandrasekhar (JHC) model [70]:

$$B_{c2}(T) = \frac{\phi_0}{2\pi} \cdot \sum_{i=1}^N \frac{\theta(T_{c,i} - T)}{\xi_i^2(0)} \cdot \left(\frac{1 - \left(\frac{T}{T_{c,i}}\right)^2}{1 + \left(\frac{T}{T_{c,i}}\right)^2} \right), \quad (6)$$

109 3. Werthamer-Helfand-Hohenberg model [71,72], for which we use analytical expression given by
 110 Baumgartner *et al.* [73] (we will designate this model as B-WHH herein):

$$B_{c2}(T) = \frac{\phi_0}{2\pi} \cdot \sum_{i=1}^N \frac{\theta(T_{c,i} - T)}{\xi_i^2(0)} \cdot \left(\frac{\left(1 - \frac{T}{T_{c,i}}\right)^{-0.153} \cdot \left(1 - \frac{T}{T_{c,i}}\right)^2 - 0.152 \cdot \left(1 - \frac{T}{T_{c,i}}\right)^4}{0.693} \right), \quad (7)$$

111 4. Gor'kov model [74], for which simple analytical expression was given by Jones *et al.* [70]:

$$B_{c2}(T) = \frac{\phi_0}{2\pi} \cdot \sum_{i=1}^N \frac{\theta(T_{c,i} - T)}{\xi_i^2(0)} \cdot \left(\left(\frac{1.77 - 0.43 \cdot \left(\frac{T}{T_{c,i}}\right)^2 + 0.07 \cdot \left(\frac{T}{T_{c,i}}\right)^4}{1.77} \right) \cdot \left[1 - \left(\frac{T}{T_{c,i}}\right)^2 \right] \right), \quad (8)$$

112 3. Results

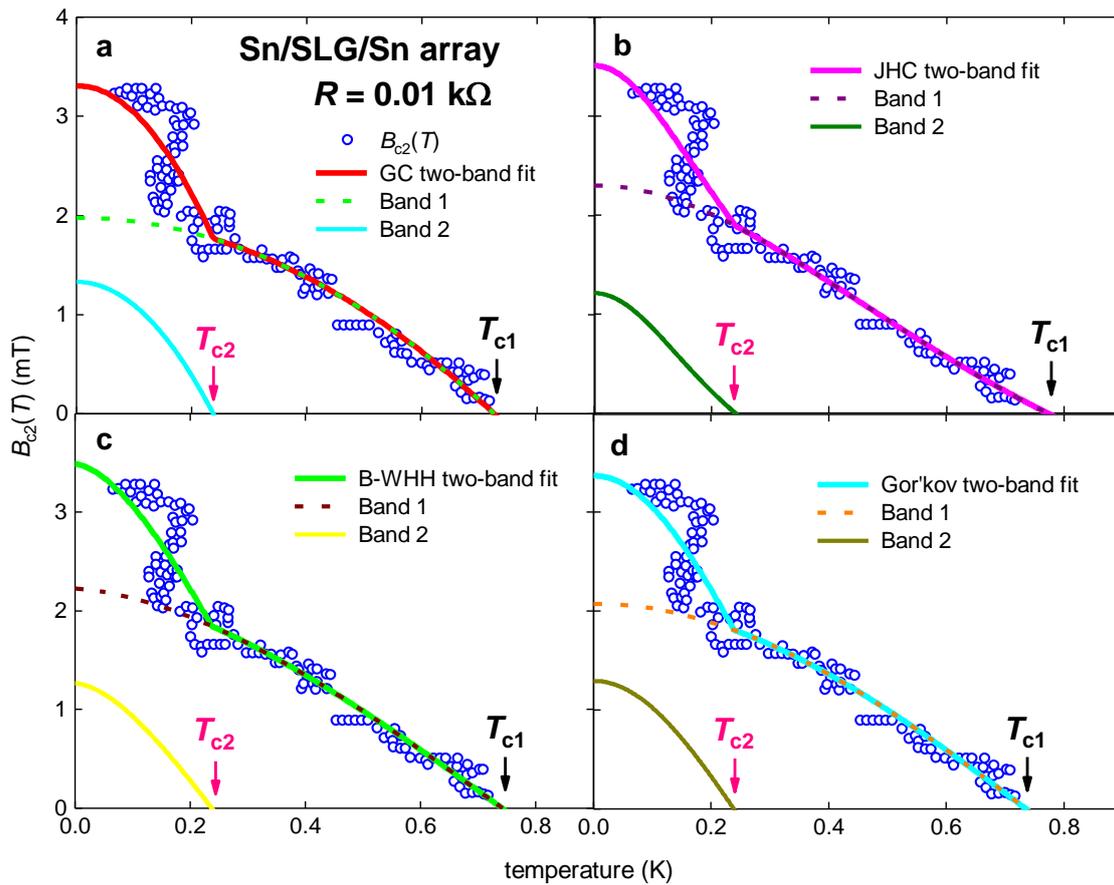
113 3.1. Planar Sn/SLG/Sn array

114 Superconductivity in planar graphene junctions is varying by the change of the charge carrier
 115 density by moving away from the Dirac point in the dispersion [12,13,17]. This change is usually
 116 controlled by the gate voltage, V_g , applying to the junction. Han *et al* [61] reported on a proximity-
 117 coupled array of Sn discs with diameter of 400 nm on SLG which were placed in a hexagonal lattice
 118 separated by 1 μ m between disks centers.

119 In Figs. 1 and 2 we show reported $B_{c2}(T)$ for Sn/SLG/Sn array by Han *et al.* [61] in their Figs. 4,5
 120 at gate voltage of $V_g = 30$ V. We defined $B_{c2}(T)$ by two criteria of $R = 0.01$ k Ω (Fig. 1) and $R = 0.2$ k Ω

121 (Fig. 2). It can be seen that there is an obvious upturn in $B_{c2}(T)$ at $T \leq 0.4 \cdot T_c$ independent of the upper
 122 critical field definition criterion. We note, that the upturn occurs at practically the same reduced
 123 temperature at which Borzenets *et al.* [15] observed the $I_c(sf, T)$ enhancement in MoRe/SLG/MoRe
 124 junctions.

125 Accordingly, we fit these $B_{c2}(T)$ datasets to four two-band models (Eqs. 5-8) and ones are shown
 126 in Figs. 1,2. Deduced parameters, including the ratio of transition temperatures for two bands, $\frac{T_{c2}}{T_{c1}} =$
 127 0.32 ± 0.02 for $R = 0.01 \text{ k}\Omega$ criterion (Fig. 1), and $\frac{T_{c2}}{T_{c1}} = 0.38 \pm 0.01$ for $R = 0.2 \text{ k}\Omega$ criterion (Fig. 2),
 128 are well agreed with each other despite a fact that experimental $B_{c2}(T)$ data were processed by four
 129 different models.



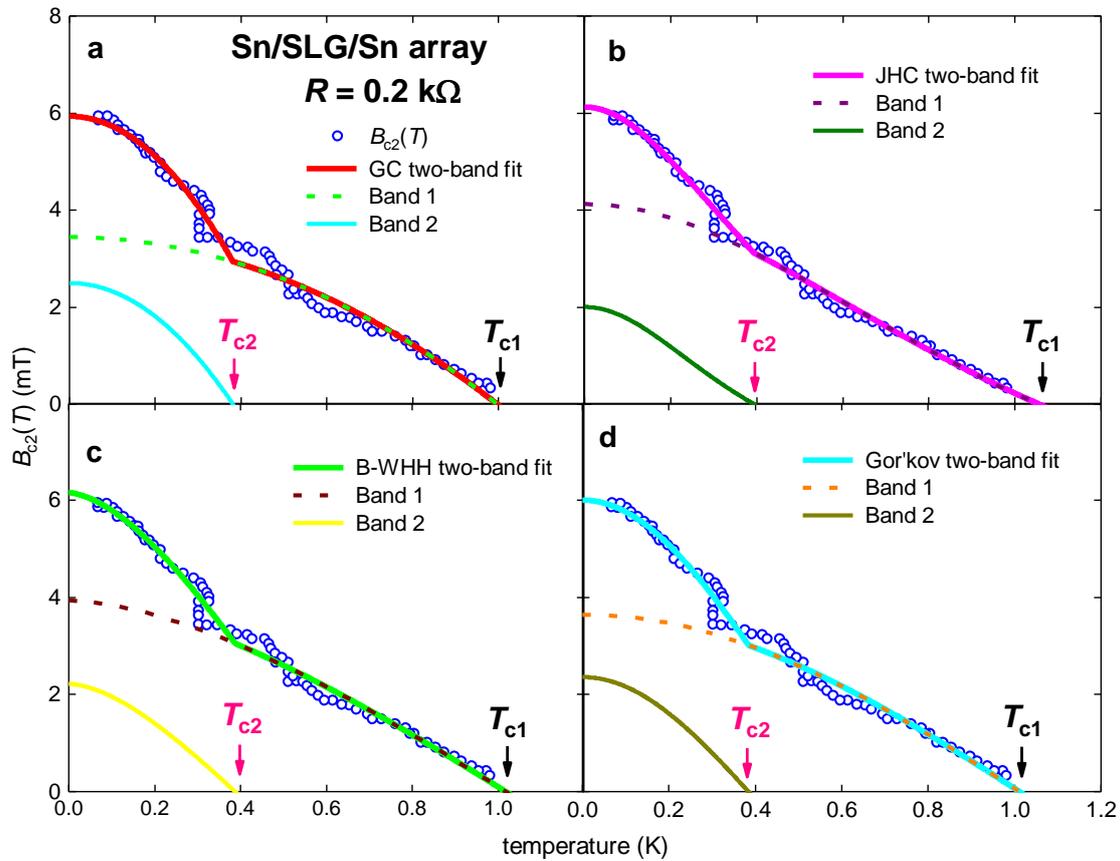
130

131 **Figure 1.** Experimental $B_{c2}(T)$ for Sn/SLG/Sn array at gate voltage of $V_g = 30 \text{ V}$ [61] and data fits to Eqs.
 132 5-8. B_{c2} criterion is $R = 0.01 \text{ k}\Omega$. (a) GC model. Derived parameters: $T_{c1} = 0.72 \pm 0.01 \text{ K}$, $\xi_1(0) = 408 \pm 7$
 133 nm , $T_{c2} = 0.24 \pm 0.01 \text{ K}$, $\xi_2(0) = 497 \pm 22 \text{ nm}$, $\frac{T_{c2}}{T_{c1}} = 0.33 \pm 0.02$, fit quality is $R = 0.9059$; (b) JHC model.
 134 Derived parameters: $T_{c1} = 0.77 \pm 0.02 \text{ K}$, $\xi_1(0) = 378 \pm 8 \text{ nm}$, $T_{c2} = 0.24 \pm 0.02 \text{ K}$, $\xi_2(0) = 521 \pm 34 \text{ nm}$, $\frac{T_{c2}}{T_{c1}} =$
 135 0.31 ± 0.04 , fit quality is $R = 0.9101$; (c) B-WHH model. Derived parameters: $T_{c1} = 0.74 \pm 0.02 \text{ K}$, $\xi_1(0) =$
 136 $385 \pm 7 \text{ nm}$, $T_{c2} = 0.24 \pm 0.01 \text{ K}$, $\xi_2(0) = 510 \pm 28 \text{ nm}$, $\frac{T_{c2}}{T_{c1}} = 0.32 \pm 0.02$, fit quality is $R = 0.9093$. (d) Gor'kov
 137 model. Derived parameters: $T_{c1} = 0.74 \pm 0.02 \text{ K}$, $\xi_1(0) = 398 \pm 7 \text{ nm}$, $T_{c2} = 0.24 \pm 0.01 \text{ K}$, $\xi_2(0) = 504 \pm 25$
 138 nm , $\frac{T_{c2}}{T_{c1}} = 0.32 \pm 0.02$, fit quality is $R = 0.9082$.

139 We also need to note that experimental data of Han *et al.* [61] have an evidence that there is the
 140 third upturn in $B_{c2}(T)$ which can be seen at lowest experimentally available temperatures of $T < 0.1 \text{ K}$
 141 and applied fields of about $B \sim 4.5 \text{ mT}$ in Fig. 4,5 [61], if the criterion of $R \sim 0.05 \text{ k}\Omega$ (for the $B_{c2}(T)$
 142 definition) will be applied.

143 Despite a fact that authors [61] did not mention the presence of these two upturns in raw
 144 experimental $B_{c2}(T)$ data and more detailed measurements of $B_{c2}(T)$ requires to reveal more accurately
 145 the position and parameters for the third band, there is already enough experimental evidences that
 146 Sn/SLG/Sn array exhibits at least two-superconducting bands gapping, and thus, the report of Han

147 *et al.* [61] supports our primary idea that atomically thin films exhibits multiple-band
 148 superconducting gapping phenomenon [50,52].
 149



150

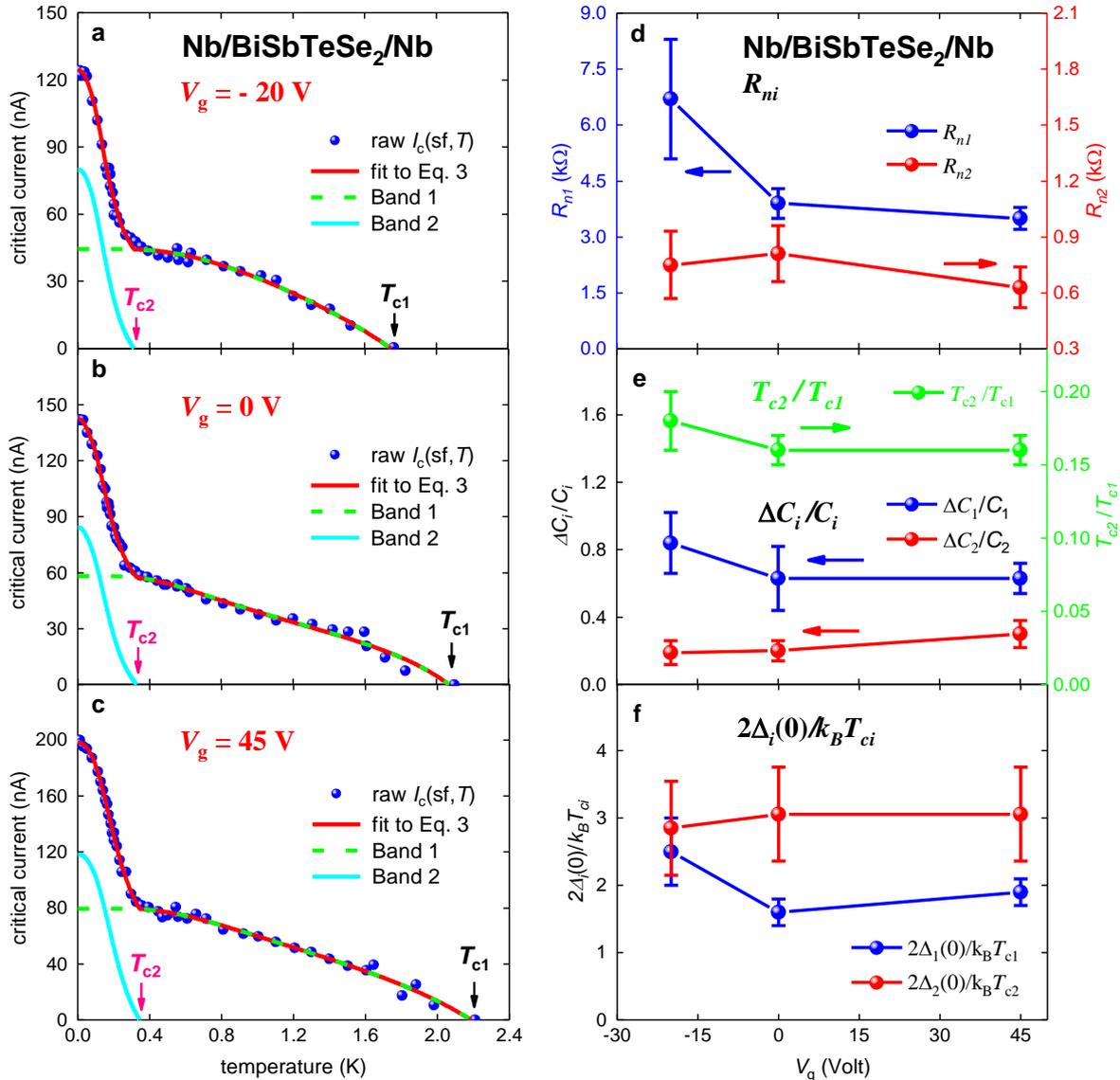
151 **Figure 2.** Experimental $B_{c2}(T)$ for Sn/SLG/Sn array at gate voltage of $V_g = 30$ V [61] and data fits to Eqs.
 152 5-8. B_{c2} criterion is $R = 0.2$ k Ω . (a) GC model. Derived parameters: $T_{c1} = 1.00 \pm 0.01$ K, $\xi_1(0) = 309 \pm 3$
 153 nm, $T_{c2} = 0.38 \pm 0.01$ K, $\xi_2(0) = 363 \pm 7$ nm, $\frac{T_{c2}}{T_{c1}} = 0.38 \pm 0.01$, fit quality is $R = 0.9847$; (b) JHC model.
 154 Derived parameters: $T_{c1} = 1.06 \pm 0.01$ K, $\xi_1(0) = 283 \pm 3$ nm, $T_{c2} = 0.39 \pm 0.01$ K, $\xi_2(0) = 405 \pm 11$ nm, $\frac{T_{c2}}{T_{c1}} =$
 155 0.37 ± 0.01 , fit quality is $R = 0.9903$; (c) B-WHH model. Derived parameters: $T_{c1} = 1.02 \pm 0.01$ K, $\xi_1(0) =$
 156 289 ± 3 nm, $T_{c2} = 0.39 \pm 0.01$ K, $\xi_2(0) = 385 \pm 9$ nm, $\frac{T_{c2}}{T_{c1}} = 0.38 \pm 0.01$, fit quality is $R = 0.9885$. (d) Gor'kov
 157 model. Derived parameters: $T_{c1} = 1.01 \pm 0.01$ K, $\xi_1(0) = 300 \pm 3$ nm, $T_{c2} = 0.38 \pm 0.01$ K, $\xi_2(0) = 374 \pm 7$ nm,
 158 $\frac{T_{c2}}{T_{c1}} = 0.38 \pm 0.01$, fit quality is $R = 0.9873$.

159 3.2. Planar Nb/BiSbTeSe₂-nanoribbon/Nb junctions

160 There is a wide accepted view that the superconducting state in S/TI/S junctions, similarly to the
 161 case of S/SLG/S junctions, controls by the gate voltage, V_g . In this regard, junctions made of the
 162 tetradymite compound, BiSbTeSe₂, one of the most bulk-insulating three-dimensional topological
 163 insulators [47], should follow these expectations. However, our analysis of recent experimental data
 164 reported by Kayyalha *et al.* [48] on Nb/BiSbTeSe₂/Nb junctions, shows that superconducting state in
 165 BiSbTeSe₂-based systems is very robust vs the change in the gate voltage, V_g , and thus, at least, S/TI/S
 166 junctions where TI thickness is less than the ground state of the coherence length, $\xi(0)$, have different
 167 physical operation principles than S/SLG/S counterparts. For instance, Kayyalha *et al.* [48] in their
 168 Figs. 2 and S1 reported $I_c(sf, T)$ for five Nb/BiSbTeSe₂-nanoribbon/Nb junctions at different V_g . The
 169 thickness of BiSbTeSe₂ flakes was varied from $2b = 30$ nm to 50 nm, and based on reported $\xi(0) \sim 600$
 170 nm [48], the condition of $2b < \xi(0)$ [50,52] is satisfied for all junctions.

171 3.2.1. Nb/BiSbTeSe₂-nanoribbon/Nb junctions (Sample 1 [48])

172 In Fig. 3 we show experimental $I_c(sf, T)$ datasets for Sample 1 [48] reported for three gate voltages,
 173 $V_g = -20$ V (Fig. 3,a), 0 V (Fig. 3,b), and +45 V (Fig. 3,c). $I_c(sf, T)$ fits to Eq. 3 were performed for all
 174 parameters to be free as experimental raw datasets were rich enough to carry out this sort of fits.



175

176 **Figure 3.** Experimental $I_c(sf, T)$ for Nb/BiSbTeSe₂-nanoribbon/Nb junction (Sample 1 [48]), data fits to
 177 Eq. 3, and major deduced parameters. (a) Gate voltage $V_g = -20$ V. Derived parameters: $T_{c1} = 1.74 \pm$
 178 0.04 K, $\Delta_1(0) = 190 \pm 40$ μ eV, $\Delta C_1/C_1 = 0.84 \pm 0.18$, $2\Delta_1(0)/k_B T_{c1} = 2.5 \pm 0.5$, $R_{n1} = 6.7 \pm 1.6$ k Ω , $T_{c2} = 0.31 \pm$
 179 0.02 K, $\Delta_2(0) = 38.2 \pm 9.7$ μ eV, $\Delta C_2/C_2 = 0.19 \pm 0.07$, $2\Delta_2(0)/k_B T_{c2} = 2.85 \pm 0.70$, $R_{n2} = 0.75 \pm 0.18$ k Ω , $\frac{T_{c2}}{T_{c1}} =$
 180 0.18 ± 0.02 , fit quality is $R = 0.9953$; (b) Gate voltage $V_g = 0$ V. Derived parameters: $T_{c1} = 2.07 \pm 0.03$ K,
 181 $\Delta_1(0) = 144 \pm 11$ μ eV, $\Delta C_1/C_1 = 0.63 \pm 0.19$, $2\Delta_1(0)/k_B T_{c1} = 1.6 \pm 0.2$, $R_{n1} = 3.9 \pm 0.4$ k Ω , $T_{c2} = 0.33 \pm 0.02$ K,
 182 $\Delta_2(0) = 43.5 \pm 8.4$ μ eV, $\Delta C_2/C_2 = 0.20 \pm 0.06$, $2\Delta_2(0)/k_B T_{c2} = 3.06 \pm 0.70$, $R_{n2} = 0.81 \pm 0.15$ k Ω , $\frac{T_{c2}}{T_{c1}} = 0.16 \pm$
 183 0.01 , fit quality is $R = 0.9965$; (c) Gate voltage $V_g = 45$ V. Derived parameters: $T_{c1} = 2.19 \pm 0.03$ K, $\Delta_1(0) =$
 184 176 ± 13 μ eV, $\Delta C_1/C_1 = 0.63 \pm 0.09$, $2\Delta_1(0)/k_B T_{c1} = 1.9 \pm 0.2$, $R_{n1} = 3.5 \pm 0.3$ k Ω , $T_{c2} = 0.34 \pm 0.01$ K, $\Delta_2(0) =$
 185 47.6 ± 8.7 μ eV, $\Delta C_2/C_2 = 0.30 \pm 0.08$, $2\Delta_2(0)/k_B T_{c2} = 3.06 \pm 0.70$, $R_{n2} = 0.63 \pm 0.11$ k Ω , $\frac{T_{c2}}{T_{c1}} = 0.16 \pm 0.01$, fit
 186 quality is $R = 0.9977$; (d) Derived R_{ni} as function of gate voltage V_g ; (e) Derived $\frac{T_{c2}}{T_{c1}}$ and $\Delta C_i/C_i$ as
 187 function of gate voltage V_g ; (f) Derived $2\Delta_i(0)/k_B T_{c_i}$ as function of gate voltage V_g .

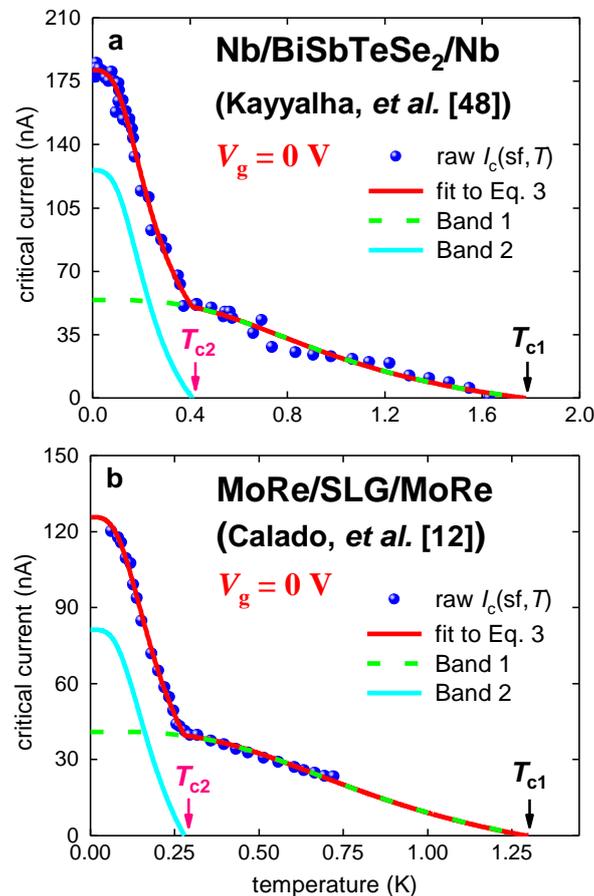
188 As the result, we deduced R_{ni} , $\frac{T_{c1}}{T_{c2}}$, $\Delta C_i/C_i$, $\Delta_i(0)$, and $\frac{2\Delta_i(0)}{k_B T_{c_i}}$ for both superconducting bands as
 189 functions of applied gate voltage, V_g . These deduced parameters are shown in Figs. 3 (e-f).

190 We need to stress, that within the range of uncertainties, deduced R_{n1} values are well agree with
 191 directly measured values by Kayyalha *et al.* [48] (these values reported in Fig. 1 (a) of Ref. 48). More
 192 often measured raw $I_c(sf, T)$ data, and especially at high reduced temperatures, are required to reduce
 193 the uncertainty for R_{n1} values.

194 Most notable outcome of our analysis is that, within uncertainty ranges, fundamental
 195 superconducting parameters for both bands, including the ratio of $\frac{T_{c2}}{T_{c1}}$, are remaining unchanged vs
 196 gate voltage variation in the range from -10 V to 45 V. This means that two-band superconducting
 197 state in Nb/BiSbTeSe₂-nanoribbon/Nb junction is very robust and mostly independent from the
 198 change in the gate voltage, V_g . This is unexpected result, because there is generally accepted view that
 199 because gate voltage, V_g , is determined the electronic state in 2D-systems in the normal state, ones
 200 should also determine the superconducting state. However, our analysis shows that this is not a case
 201 in general view. As we already mentioned above, there is a need for more often measurements of raw
 202 $I_c(sf, T)$ data, which will allows to reduce uncertainties for all deduced parameters.

203 3.2.2. Nb/BiSbTeSe₂-nanoribbon/Nb (Sample 3 [48])

204 In Fig. 4 (a) we show experimental $I_c(sf, T)$ dataset for Nb/BiSbTeSe₂-nanoribbon/Nb (Sample 3)
 205 reported by Kayyalha *et al.* [48].



206

207 **Figure 4.** Experimental $I_c(sf, T)$ for two atomically thin DCM-based junctions and fits to Eqs. 3,9,10. (a)
 208 Nb/BiSbTeSe₂/Nb (Sample 3 [48]). Derived parameters: $T_{c1} = 1.8 \pm 0.1$ K, $\Delta_1(0) = 179 \pm 51$ μ eV, $\Delta C/C =$
 209 0.20 ± 0.04 , $2\Delta(0)/k_B T_c = 2.3 \pm 0.7$, $R_{n1} = 5.2 \pm 1.4$ k Ω , $T_{c2} = 0.41 \pm 0.02$ K, $\Delta_2(0) = 41 \pm 12$ μ eV, $R_{n2} = 0.51 \pm$
 210 0.15 k Ω , $\frac{T_{c2}}{T_{c1}} = 0.23 \pm 0.02$, $R = 0.9954$; (b) MoRe/SLG/MoRe (Sample A [12]). Derived parameters: T_{c1}
 211 $= 1.29 \pm 0.07$ K, $\Delta_1(0) = 139 \pm 36$ μ eV, $\Delta C/C = 0.30 \pm 0.04$, $2\Delta(0)/k_B T_c = 2.5 \pm 0.7$, $R_{n1} = 5.3 \pm 1.4$ k Ω , $T_{c2} =$
 212 0.28 ± 0.01 K, $\Delta_2(0) = 30 \pm 8$ μ eV, $R_{n2} = 0.56 \pm 0.16$ k Ω , $\frac{T_{c2}}{T_{c1}} = 0.22 \pm 0.01$, $R = 0.9981$.

213 Raw experimental $I_c(sf,T)$ dataset for this sample was not reach enough at $T \geq 0.6$ K, and thus
 214 we cannot perform the fit to Eq. 3 for all parameters to be free. To run the model (Eq. 3), we make the
 215 same model restriction, as we did in our previous work [50]:

$$\frac{\Delta C_1}{c_1} = \frac{\Delta C_2}{c_2} = \frac{\Delta C}{c'} \quad (9)$$

$$\frac{2\Delta_1(0)}{k_B \cdot T_1} = \frac{2\Delta_2(0)}{k_B \cdot T_2} = \frac{2\Delta(0)}{k_B \cdot T_c} \quad (10)$$

216 i.e., we forced $\Delta C_i/C_i$ and $\frac{2\Delta_i(0)}{k_B \cdot T_{c,i}}$ values to be the same for both bands. As the result, we deduce R_{ni} ,
 217 $T_{c,i}$, $\frac{T_{c2}}{T_{c1}} \sim \frac{1}{4}$, $\Delta C/C$, $\Delta_i(0)$, and $\frac{2\Delta(0)}{k_B \cdot T_c}$ for this junction and find that these values are very close to ones
 218 deduced for Sample 1 (Fig. 3).

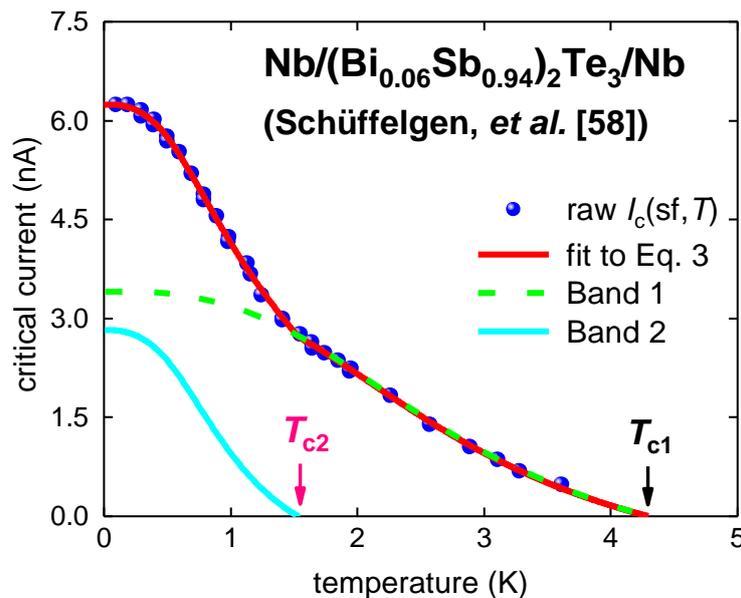
219 3.3. Planar MoRe/SLG/MoRe junction (Device A [12])

220 To demonstrate that our findings in regard of Nb/BiSbTeSe₂-nanoribbon/Nb junctions are
 221 generic for a much wide range of atomically-thin DCM-based Josephson junctions, in Fig. 4 (b) we
 222 show raw $I_c(sf,T)$ dataset and fit to our model (Eq. 3) for MoRe/SLG/MoRe reported by Calado *et al.*
 223 [12] for their Device A [12]. For the $I_c(sf,T)$ fit for this device we used the same parameters restrictions
 224 (Eqs. 9,10), as for Nb/BiSbTeSe₂-nanoribbon/Nb Sample 3 [48].

225 In our previous work [50], we already analyzed this $I_c(sf,T)$ dataset for MoRe/SLG/MoRe Device
 226 A [12]. However, what was a surprise, that there is remarkable and practically undistinguishable
 227 similarity in reduced $I_c(sf,T)$ datasets and fits for Nb/BiSbTeSe₂-nanoribbon/Nb [48] and
 228 MoRe/SLG/MoRe [12] junctions (Fig. 4). In attempt to make further extension for our findings belong
 229 S/DCM/S junctions, in next Section we analyze $I_c(sf,T)$ data for Nb/(Bi_{0.06}Sb_{0.94})₂Te₃-nanoribbon/Nb
 230 junction [58].

231 3.4. Planar Nb/(Bi_{0.06}Sb_{0.94})₂Te₃-nanoribbon/Nb junction

232 In Fig. 5 we show temperature-dependent self-field critical currents, $I_c(sf,T)$, in
 233 Nb/(Bi_{0.06}Sb_{0.94})₂Te₃-nanoribbon/Nb reported by Schüffelgen *et al.* [58], where TI nanoribbon has
 234 thickness of $2b = 10$ nm, and, thus, the condition of $2b < \xi(0)$ [50,52] was satisfied.



235

236 **Figure 5.** Experimental $I_c(sf,T)$ for atomically thin DCM-based junction Nb/(Bi_{0.06}Sb_{0.94})₂Te₃-
 237 nanoribbon/Nb [58] and fit to Eq. 3,9,10. Derived parameters: $T_{c1} = 4.30 \pm 0.07$ K, $\Delta_1(0) = 530 \pm 7$ μ eV,
 238 $\Delta C/C = 0.28 \pm 0.04$, $2\Delta(0)/k_B T_c = 2.87 \pm 0.05$, $R_{n1} = 244 \pm 32$ Ω , $T_{c2} = 1.53 \pm 0.03$ K, $\Delta_2(0) = 189 \pm 3$ μ eV, R_{n2}
 239 $= 105 \pm 16$ Ω , $\frac{T_{c2}}{T_{c1}} = 0.36 \pm 0.01$, $R = 0.9995$.

240 Due to reported $I_c(sf,T)$ dataset was not rich enough at high reduced temperatures, we restrict
241 model by utilizing Eqs. 9,10. In overall, fitted curves and all deduced parameters are very close to
242 one reported by Borzenets *et al.* [15] for MoRe/SLG/MoRe junctions (which we processed and showed
243 in our previous paper [50] in Fig. 7).

244 4. Discussion

245 We should stress that Calado *et al.* [12] in 2015 requested the necessity for a new model to explain
246 the upturn in $I_c(sf,T)$ registered in their MoRe/SLG/MoRe junction (Device A) at $T \sim \frac{1}{4} \cdot T_c$ (which we
247 show in Fig. 4 (a)), because this $I_c(sf,T)$ enhancement was not possible to explain neither by
248 Eilenberger model (which is in use to describe clean S/N/S junctions) [75], nor by Isadel model (which
249 describes diffusive S/N/S junctions) [76].

250 Our explanation for this upturn [52], which is well aligned with the $I_c(sf,T)$ upturn in natural
251 atomically thin superconductors [50], is that this $I_c(sf,T)$ enhancement is due to a new
252 superconducting band opening phenomenon when sample dimensions become smaller than some
253 critical value. For this critical value we proposed to use [52] the out-of-plane coherence length, $\xi_c(0)$,
254 which is still, after expanding our analysis herein, a good choice for the scaling criterion.

255 We need pointed out that this new opening band phenomenon is not necessarily causes the
256 increase in observed transition temperature in comparison with “bulk” material. For instance, in pure
257 Nb films [77], this new “thin film” band has lower transition temperature in comparison with “bulk”
258 band [52]. And when this is the case, there is no warning for the researcher to search more deeply
259 created device/films for new superconducting band.

260 Thus, perhaps, in many atomically thin films, which in fact exhibit a new band opening
261 phenomenon, this effect was not registered yet, because there was no expectation that something
262 important/interesting can be observed at low reduced temperatures, well below “bulk” or observed
263 T_c for given atomically thin film.

264 We also need to note, that the effect of new superconducting band opening [52] in atomically
265 thin films can be detected by any experimental techniques which is sensitive to additional band(s)
266 crossing the Fermi surface. To date, most evident confirmations for the phenomenon are related to
267 the $I_c(sf,T)$ upturn [9,50,52] and $B_{c2}(T)$ upturn [9], however, other techniques also should detect this.

268 In this regard, we want to mention non-ambitiously observation of the $I_c(sf,T)$ upturn reported
269 by Li *et al.* [44] in their Fig. 4 (a) at $T = 2.5$ K in Nb/Cd₃As₂-nanowire/Nb junction. However, raw
270 experimental $I_c(sf,T)$ dataset [44] was limited by measurements at $T < 3.5$ K, and thus, we are not able
271 to perform the analysis for this very interesting atomically-narrow S/TI/S junction at the moment.

272 There are very interesting results reported by Sasaki *et al.* [78] and by Andersen *et al.* [79], who
273 found that temperature-dependent upper critical field, $B_{c2}(T)$, in nanostructures of topological
274 insulators, cannot be explained by single-band WHH model [71,72]. However, reported, to date, raw
275 experimental $B_{c2}(T)$ datasets [77,78] are not reach enough to perform two-band model fit to reveal the
276 presence of additional band at low reduced temperatures in these structures.

277 We also need to mention an interesting research field of interfaced superconductivity [80-82],
278 which is, however, beyond the scope of this paper.

279 5. Conclusions

280 As the result, in this paper we perform analysis of recently reported experimental data on
281 induced superconducting state in atomically thin Dirac-cone films. We show, that the phenomenon
282 of new superconducting band opening in atomically thin films [50,52], when the film thickness
283 becomes thinner than the ground state out-of-plane coherence length, $\xi_c(0)$, can be extended on
284 induced superconducting state in atomically thin DCM, as one was established before for natural
285 superconductors, i.e. pure Nb, exfoliated 2H-TaS₂, double-atomic layer FeSe and few layer stanene
286 [9].

287 In this paper we have focused to analyze induced superconducting state in S/DCM/S junctions,
288 and we report that several S/DCM/S junctions exhibit the phenomenon of new superconducting band
289 opening [50,52] in atomically thin films.

290 **Funding:** This research was funded by the State Assignment of Minobrnauki of Russia, theme "Pressure" No.
291 AAAA-A18-118020190104-3, and by Act 211 Government of the Russian Federation, contract No. 02.A03.21.0006.

292 **Acknowledgments:** Author would like to thank Dr. S. Goswami and Prof. L. M. K. Vandersypen (Kavli Institute
293 of Nanoscience, Delft University of Technology, The Netherlands) for providing raw self-field critical current
294 data for the MoRe/SLG/MoRe devices analyzed in this work.

295 **Conflicts of Interest:** The funders had no role in the design of the study; in the collection, analyses, or
296 interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

297 References

- 298 1. Hirsch, J.E.; Maple, M.B.; Marsiglio, F. Superconducting materials classes: Introduction and overview.
299 *Physica C* **2015**, *514*, 1-8.
- 300 2. Holm, R.; Meissner, W. Messungen mit Hilfe von flüssigem Helium. XIII. Kontaktwiderstand zwischen
301 Supraleitern und Nichtsupraleitern (Measurements using liquid helium. XIII. Contact resistance between
302 superconductors and non-superconductors). *Zeitschrift für Physik* **1932**, *74*, 715-735.
- 303 3. Natterer, F.D.; Ha, J.; Baek, H.; Zhang, D.; Cullen, W.G.; Zhitenev, N.B.; Kuk, Y.; Strosio, J.A. Scanning
304 tunneling spectroscopy of proximity superconductivity in epitaxial multilayer graphene. *Phys Rev. B* **2016**,
305 *93*, 045406.
- 306 4. Kim, H.; Miyata, Y.; Hasegawa, Y. Superconducting proximity effect on a Rashba-split Pb/Ge(111)- $\sqrt{3} \times \sqrt{3}$
307 surface. *Supercond. Sci. & Technol.* **2016**, *29*, 084006.
- 308 5. Ambegaokar, V.; Baratoff, A. Tunneling between superconductors. *Phys. Rev. Lett.* **1963**, *10*, 486-489.
- 309 6. Ambegaokar, V.; Baratoff, A. Errata: Tunneling between superconductors. *Phys. Rev. Lett.* **1963**, *11*, 104.
- 310 7. Novoselov, K.S.; Geim, A.K.; Morozov, S.V.; Jiang, D.; Zhang, Y.; Dubonos, S.V.; Grigorieva, I.V.; Firsov,
311 A.A. Electric field effect in atomically thin carbon films. *Science* **2004**, *306*, 666-669.
- 312 8. Lee, G.H.; Kim, S.; Jhi, S.-H.; Lee, H.-J. Ultimately short ballistic vertical graphene Josephson junctions. *Nat.*
313 *Comms.* **2015**, *6*, 6181.
- 314 9. Liao, M., *et al.* Superconductivity in few-layer stanene. *Nature Physics* **2018**, *14*, 344-348.
- 315 10. Heersche, H.B.; Jarillo-Herrero, P.; Oostinga, J.B.; Vandersypen, L.M.K.; Morpurgo, A.F. Bipolar
316 supercurrent in graphene. *Nature* **2007**, *446*, 56-59.
- 317 11. Du, X.; Skachko, I.; Andrei, E.Y. Josephson current and multiple Andreev reflections in graphene SNS
318 junctions. *Phys. Rev B* **2008**, *77*, 184507.
- 319 12. Calado, V.E.; *et al.* Ballistic Josephson junctions in edge-contacted graphene. *Nature Nanotech.* **2015**, *10*, 761-
320 764.
- 321 13. Ben Shalom, M.; *et al.* Quantum oscillations of the critical current and high-field superconducting proximity
322 in ballistic graphene. *Nature Phys.* **2016**, *12*, 318-322.
- 323 14. Amet, F.; *et al.* Supercurrent in the quantum Hall regime. *Science* **2016**, *352*, 966-969.
- 324 15. Borzenets, I.V.; *et al.* Ballistic graphene Josephson junctions from the short to the long junction regimes
325 *Phys. Rev. Lett.* **2016**, *117*, 237002.
- 326 16. Island, J.O.; Steele, G.A.; van der Zant, H. S. J.; Castellanos-Gomez, A. Thickness dependent interlayer
327 transport in vertical MoS₂ Josephson. *2D Materials* **2016**, *3*, 031002.
- 328 17. Zhu, M.J.; *et al.* Edge currents shunt the insulating bulk in gapped graphene. *Nat. Comms.* **2017**, *8*, 14552.
- 329 18. Veldhorst, M.; *et al.* Josephson supercurrent through a topological insulator surface state. *Nature Materials*
330 **2012**, *11*, 417-421.
- 331 19. Kurter, C.; Finck, A.D.K.; Hor, Y.S.; Van Harlingen, D.J. Evidence for an anomalous current-phase relation
332 in topological insulator Josephson junctions. *Nature Communications* **2015**, *6*, 7130.
- 333 20. Nanda, G.; *et al.* Current-phase relation of ballistic graphene Josephson junctions. *Nano Lett.* **2017**, *17*,
334 3396-3401.
- 335 21. Yankowitz, M.; Chen, S.; Polshyn, H.; Watanabe, K.; Taniguchi, T.; Graf, D.; Young, A.F.; Dean, C.R. Tuning
336 superconductivity in twisted bilayer graphene. *Science* **2019**, *363*, 1059-1064.
- 337 22. Lucignano, P.; Alfè, D.; Cataudella, V.; Ninno, D.; Cantele, G. The crucial role of atomic corrugation on the
338 flat bands and energy gaps of twisted bilayer graphene at the "magic angle" $\theta \sim 1.08^\circ$. *Phys. Rev. B* **2019**, *99*,
339 195419.
- 340 23. Giubileo, F.; Romeo, F.; Di Bartolomeo, A.; Y. Mizuguchi, Y.; Romano, P. Probing unconventional pairing
341 in LaO_{0.5}F_{0.5}BiS₂ layered superconductor by point contact spectroscopy. *Journal of Physics and Chemistry of*
342 *Solids* **2018**, *118*, 192-199.

- 343 24. Kizilaslan, O.; Truccato, M.; Simsek, Y.; Aksan, M.A.; Koval, Y.; Müller, P. Interlayer tunneling
344 spectroscopy of mixed-phase BSCCO superconducting whiskers. *Supercond. Sci. Technol.* **2016**, *29*, 065013
- 345 25. Fête, A.; Rossi, L.; Augieri, A.; Senatore, C. Ionic liquid gating of ultra-thin YBa₂Cu₃O_{7-x} films. *Appl. Phys.*
346 *Lett.* **2016**, *109*, 192601.
- 347 26. Mueller, P.; Koval, Y.; Lazareva, Y.; Steiner, Ch.; Wurmehl, S.; Buechner, B.; Stuerzer, T.; Johrendt, D. C-
348 axis transport of pnictide superconductors. *Phys. Status Solidi B* **2017**, *254*, 1600157.
- 349 27. Fête, A.; Senatore, C. Strong improvement of the transport characteristics of YBa₂Cu₃O_{7-x} grain boundaries
350 using ionic liquid gating. *Scientific Reports* **2017**, *8*, 17703.
- 351 28. Paradiso, N.; Nguyen, A.-T.; Kloss, K.E.; Strunk, C. Phase slip lines in superconducting few-layer NbSe₂
352 crystals. *2D Materials* **2019**, *6*, 025039.
- 353 29. Wu, Y., *et al.* The transport properties in graphene/single-unit-cell cuprates van der Waals heterostructure.
354 *Supercond. Sci. and Technol.* **2019**, *32*, 085007.
- 355 30. Guo, J.G.; *et al.* Quasi-two-dimensional superconductivity from dimerization of atomically ordered
356 AuTe₂Se_{4/3} cubes. *Nature Communications* **2017**, *8*, 871.
- 357 31. Pan, J.; *et al.* Enhanced superconductivity in restacked TaS₂ nanosheets. *J. Am. Chem. Soc.* **2017**, *139*, 4623.
- 358 32. Ma, Y.; *et al.* Unusual evolution of B_{c2} and T_c with inclined fields in restacked TaS₂ nanosheets. *npj Quantum*
359 *Materials* **2018**, *3*, 34.
- 360 33. Desrat, W.; *et al.* Superconducting Ga/GaSe layers grown by van der Waals epitaxy. *Mater. Res. Express*
361 **2018**, *5*, 045901.
- 362 34. Liu, C.; *et al.* Two-dimensional superconductivity and topological states in PdTe₂ thin films. *Physical Review*
363 *Materials* **2018**, *2*, 094001.
- 364 35. Peng, J.; *et al.* Disorder enhanced superconductivity toward TaS₂ monolayer. *ACS Nano* **2018**, *12*, 9461-9466.
- 365 36. De La Barrera, S.C.; *et al.* Tuning Ising superconductivity with layer and spin-orbit coupling in two-
366 dimensional transition-metal dichalcogenides. *Nature Communications* **2018**, *9*, 1427.
- 367 37. Di Castro, D.; Balestrino, G. Superconductivity in interacting interfaces of cuprate-based heterostructures
368 *Supercond. Sci. Technol.* **2018**, *31*, 073001.
- 369 38. Wu, Y.; *et al.* Dimensional reduction and ionic gating induced enhancement of superconductivity in
370 atomically thin crystals of 2H-TaSe₂. *Nanotechnology* **2019**, *30*, 035702.
- 371 39. Talantsev, E.F. Angular dependence of the upper critical field in randomly restacked 2D superconducting
372 nanosheets. *Supercond. Sci. Technol.* **2019**, *32*, 015013.
- 373 40. Pankratov, O.A., Pakhomov, S.V., Volkov, B.A. Supersymmetry in heterojunctions: Band-inverting contact
374 on the basis of Pb_{1-x}Sn_xTe and Hg_{1-x}Cd_xTe. *Solid State Communications* **1987**, *61*, 93-96.
- 375 41. König, M., *et al.* Quantum spin Hall insulator state in HgTe quantum wells. *Science* **2007**, *318*, 766-770.
- 376 42. Charpentier, S., *et al.* Induced unconventional superconductivity on the surface states of Bi₂Te₃ topological
377 insulator. *Nature Communications* **2017**, *8*, 2019.
- 378 43. Qu, D.-X., *et al.* Onset of a two-dimensional superconducting phase in a topological-insulator – normal-
379 metal Bi_{1-x}Sb_x/Pt junction fabricated by ion-beam techniques. *Phys. Rev. Lett.* **2018**, *121*, 037001.
- 380 44. Li, C.-Z. *et al.* Bulk and surface states carried supercurrent in ballistic Nb-Dirac semimetal Cd₃As₂
381 nanowire-Nb junctions. *Phys. Rev. B* **2018**, *97*, 115446.
- 382 45. Schüffelgen, P. *et al.* Exploiting topological matter for Majorana physics and devices. *Solid State Electronics*
383 **2019**, *155*, 99-104.
- 384 46. Kurter, C., *et al.* Conductance spectroscopy of exfoliated thin flakes of Nb_xBi₂Se₃. *Nano Lett.* **2019**, *19*, 38-45.
- 385 47. German, R, *et al.* Phonon mode calculations and Raman spectroscopy of the bulk-insulating topological
386 insulator BiSbTeSe₂. *Phys. Rev. Materials* **2019**, *3*, 054204.
- 387 48. Kayyalha, M., *et al.* Anomalous low-temperature enhancement of supercurrent in topological-insulator
388 nanoribbon Josephson junctions: Evidence for low-energy Andreev bound states. *Phys. Rev. Lett.* **2019**, *122*,
389 047003.
- 390 49. Miyazaki, A., W Delsolaro, W.V. Determination of the Bardeen–Cooper–Schrieffer material parameters of
391 the HIE-ISOLDE superconducting resonator. *Supercond. Sci. and Technol.* **2019**, *32*, 025002.
- 392 50. Talantsev, E.F.; Crump, W.P.; Tallon, J.L. Two-band induced superconductivity in single-layer graphene
393 and topological insulator bismuth selenide. *Supercond. Sci. & Technol.* **2018**, *31*, 015011.
- 394 51. Shearer, C.J.; Slattery, A.D.; Stapleton, A.J.; Shapter, J.G.; Gibson, C.T. Accurate thickness measurement of
395 graphene. *Nanotechnology* **2016**, *27*, 125704.

- 396 52. Talantsev, E.F.; Crump, W.P.; Island, J.O.; Xing, Y.; Sun, Y.; Wang, J.; Tallon, J.L. On the origin of critical
397 temperature enhancement in atomically thin superconductors. *2D Materials* **2017**, *4*, 025072.
- 398 53. Qing-Yan, W.; *et al.* Interface-induced high-temperature superconductivity in single unit-cell FeSe films on
399 SrTiO₃. *Chin. Phys. Lett.* **2012**, *29*, 037402.
- 400 54. Zhang, W.-H.; *et al.* Direct observation of high-temperature superconductivity in one-unit-cell FeSe films.
401 *Chin. Phys. Lett.* **2014**, *31*, 017401.
- 402 55. Ge, J.F.; *et al.* Superconductivity above 100 K in single-layer FeSe films on doped SrTiO₃. *Nature Materials*
403 **2015**, *14*, 285-289.
- 404 56. Zhang, H.M.; *et al.* Detection of a superconducting phase in a two-atom layer of hexagonal Ga film grown
405 on semiconducting GaN(0001). *Phys. Rev. Lett.* **2015**, *114*, 107003.
- 406 57. Xing, Y.; *et al.* Quantum Griffiths singularity of superconductor-metal transition in Ga thin films. *Science*
407 **2015**, *350*, 542-545.
- 408 58. Navarro-Moratalla, E.; *et al.* Enhanced superconductivity in atomically thin TaS₂. *Nat. Comms.* **2016**, *7*,
409 11043.
- 410 59. Rhodes, D.; *et al.* Enhanced superconductivity in monolayer *Td*-MoTe₂ with tilted Ising spin texture. *arXiv:*
411 **2019**, 1905.06508.
- 412 60. Schüffelgen, P. *et al.* Boosting transparency in topological Josephson junctions via stencil lithography.
413 *arXiv:* **2018**, 1711.01665.
- 414 61. Han, Z.; *et al.* Collapse of superconductivity in a hybrid tin-graphene Josephson junction array. *Nature*
415 *Physics* **2014**, *10*, 380-386.
- 416 62. Gross, F.; *et al.* Anomalous temperature dependence of the magnetic field penetration depth in
417 superconducting UBe₁₃. *Zeitschrift für Physik B Condensed Matter* **1986**, *64*, 175-188.
- 418 63. Gorter, C.J.; Casimir, H. On supraconductivity I. *Physica* **1934**, *1*, 306-320.
- 419 64. Poole, P.P.; Farach, H.A.; Creswick, R.J.; Prozorov, R. *Superconductivity*, 2nd ed.; Associated Press: London,
420 UK, 2007; pp. 52-55.
- 421 65. Drozdov, A.P.; Erements, M.I.; Troyan, I.A., Ksenofontov, V.; and Shylin, S.I. Conventional
422 superconductivity at 203 kelvin at high pressures in the sulfur hydride system. *Nature* **2015**, *525*, 73-76.
- 423 66. Talantsev, E.F.; Crump, W.P.; Storey, J.G.; Tallon, J.L. London penetration depth and thermal fluctuations
424 in the sulphur hydride 203 K superconductor. *Annalen der Physics* **2017**, *529*, 1600390.
- 425 67. Mozaffari, S.; *et al.* Superconducting phase-diagram of H₃S under high magnetic fields. *Nature*
426 *Communications* **2019**, *10*, 2522.
- 427 68. Talantsev, E.F. Classifying superconductivity in compressed H₃S. *Modern Physics Letters B* **2019**, *33*, 1950195.
- 428 69. Pal, B.; *et al.* Experimental evidence of a very thin superconducting layer in epitaxial indium nitride.
429 *Supercond. Sci. Technol.* **2019**, *32*, 015009.
- 430 70. Jones, C.K.; Hulm, J.K.; Chandrasekhar, B.S. Upper critical field of solid solution alloys of the transition
431 elements. *Rev. Mod. Phys.* **1964**, *36*, 74-76.
- 432 71. Helfand, E.; Werthamer, N.R. Temperature and purity dependence of the superconducting critical field,
433 *H_{c2}*. II. *Phys. Rev.* **1966**, *147*, 288-294.
- 434 72. Werthamer, N.R.; E. Helfand, E.; Hohenberg, P.C. Temperature and purity dependence of the
435 superconducting critical field, *H_{c2}*. III. Electron spin and spin-orbit effects. *Phys. Rev.* **1966**, *147*, 295-302.
- 436 73. Baumgartner, T.; Eisterer, M.; Weber, H.W.; Fluekiger, R.; Scheuerlein, C.; Bottura, L. Effects of neutron
437 irradiation on pinning force scaling in state-of-the-art Nb₃Sn wires. *Supercond. Sci. Technol.* **2014**, *27*, 015005.
- 438 74. Gor'kov, L.P. The critical supercooling field in superconductivity theory. *Soviet Physics JETP* **1960**, *10*, 593-
439 599.
- 440 75. Eilenberger, G. Transformation of Gorkov's equation for type II superconductors into transport-like
441 equations. *Z. Physik* **1968**, *214*, 195-213.
- 442 76. Usadel, K.D. Generalized diffusion equation for superconducting alloys. *Phys.Rev.Lett.* **1970**, *25*, 507-509.
- 443 77. Rusanov, A.Yu., Hesselberth, M.B.S., and Aarts, J. Depairing currents in superconducting films of Nb and
444 amorphous MoGe. *Phys. Rev. B* **2004**, *70*, 024510.
- 445 78. Sasaki, S., Segawa, K., and Ando, Y. Superconductor derived from a topological insulator heterostructure.
446 *Phys. Rev. B* **2014**, *90*, 220504.
- 447 79. Andersen, L., Wang, Z., Lorenz, T., and Ando, Y. Nematic superconductivity in Cu_{1.5}(PbSe)₅(Bi₂Se₃)₆. *Phys.*
448 *Rev. B* **2018**, *98*, 220512(R).
- 449 80. Reyren, N., *et al.* Superconducting interfaces between insulating oxides. *Science* **2007**, *317*, 1196-1199.

- 450 81. Gozar, A., Logvenov, G., Fitting Kourkoutis, L., Bollinger, A.T., Giannuzzi, L.A., Muller, D.A., and Bozovic,
451 I. High-temperature interface superconductivity between metallic and insulating copper oxides, *Nature*
452 **2008**, *455*, 782-785.
- 453 82. Di Castro D., Balestrino G. Superconductivity in interacting interfaces of cuprate-based heterostructures.
454 *Supercond. Sci. and Technool.* **2018**, *31*, 073001.