

1 Article

## 2 Synergetic Evaluation of Project Portfolio Configuration Based 3 on Data Envelopment Analysis

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12 **Abstract:** Project portfolio configuration (PPC) is an important approach to maintain the sustainable  
13 development of enterprises and achieve organizations' strategy. However, the synergetic efficacy  
14 of PPC which determines the degree of the project's strategic objectives achieved is a fuzzy problem  
15 and hard to be measured. To solve this problem, this paper takes the data envelopment analysis  
16 (DEA) as the tool to measure the efficacy of PPC under deterministic conditions. First, a portfolio  
17 evaluation index system which takes financial indicators and non-financial indicators into  
18 consideration is developed based on the review of the literature; Second, an evaluation model based  
19 on DEA is built to reduce the number of decision making-unit with the perspective of synergetic  
20 theory; Then, a computational experiment is studied to verify the feasibility of this proposed model.  
21 The results of this computational experiment show that this model can effectively narrow scope of  
22 decision-making, improve the decision-making level and provide a reference to decide the DEA  
23 effective project portfolio decision-making unit. To our knowledge, this study is the first time to  
24 apply the notion of synergetic efficacy and DEA to the PPC domain. It is hoped that this paper may  
25 shed lights on any further study about PPC and enterprise competitiveness of sustainable  
26 development.

27 **Keywords:** project portfolio configuration; synergetic management; data envelopment analysis;  
28 efficiency evaluation.  
29

### 30 1. Introduction

31 Sustainable development is a new management paradigm, one whose principles can be used to  
32 improve how practitioners of all levels manage the complexity and dynamics of projects [1-3].  
33 Following rapid economic development and growth, multi-projects executed in parallel has become  
34 the new norm for corporate business operations in a market of limited resources. The ability to  
35 reasonably combine and implement multiple projects simultaneously in order to strike a balance  
36 between efficiency and quality has become an increasingly important issue for enterprises adapting  
37 to market demand and sharpening its competitive edge. Project Portfolio Management (PPM) refers  
38 to methods and patterns that combine different components to achieve strategic objectives under  
39 certain constraints [4] (such as limited resource constraints and possible target conflicts between  
40 different projects) in order to maximize the effectiveness and profitability for the said organization.  
41 One of the most challenging tasks in project portfolio management is PPC, which is a guiding  
42 philosophy that aims to implement synergistic configuration and dynamic optimization for project  
43 components that ultimately delivers strategic organizational impact [5]. PPC is not only affected by  
44 various resource distribution constraints and internal conflicts between project objectives [6], but also  
45 a combination of factors such as post-benefit correlations and the relevance of the results [7].

46 Since early 2001, both domestic and overseas scholars have paid more and more effort into the  
47 study of PPC, which focused not only on theoretical research but also on a wide range of business  
48 practices [8-10]. Based on a review of the literature, many studies have been reported on the methods  
49 of maintaining a high degree of correlation between PPC and strategy, resources allocation across  
50 different projects and schedule optimization of the PPC [11], providing a basis for decision making  
51 when managers implement portfolio management [12-14]. Sascha [15] and his fellow scholars  
52 constructed a comprehensive conceptual model to ensure the realization of strategic organizational  
53 objectives which takes into account factors such as business strategy, the structure of project  
54 components, etc; these then further clarified the influence of synergetic effects of the project  
55 components on the organizational strategy. From the perspective of the dynamic environment, Petit  
56 [16] studied how uncertainties may effect project portfolio management, and then summarized the  
57 sources and distribution of uncertainties, thus contributing ideas to the study of uncertainties in  
58 project portfolio management [17-19].

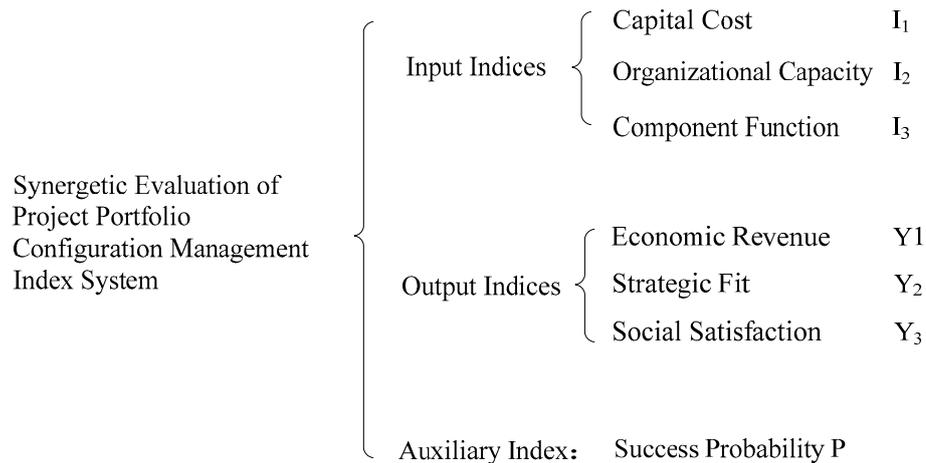
59 The PPC co-management refers to the method and mode of synergistic management of different  
60 resource components, the resource constraints, the mutual influence of the multi-project objectives,  
61 the synergistic sharing of the project resources, etc., in order to achieve benefits that are greater than  
62 the sum of individual projects [20]. However, as mentioned above, there are many factors to be  
63 considered in the project portfolio management, complicated cooperative relations among the factors  
64 [21], and difficulties in quantifying synergistic effects. Hence, there are relatively few research results  
65 from the field of studying project portfolio management.

66 DEA is an effective and objective method for evaluating production efficiency from the same  
67 type of decision-making unit [22]. Wang et al. [23] established an integrated approach that combines  
68 the grey forecasting model GM and DEA to evaluate the comparative efficiencies of 16 Green  
69 Logistics Providers and select the righter partner for sustainable development of enterprise that will  
70 lead to improved business performance and reduce carbon dioxide (CO<sub>2</sub>) emissions. From the  
71 prospect of sustainable development of real estate industry, DEA has been successfully used for  
72 predicting one company bankruptcy and the operation efficiency which emphasized on the levels of  
73 several financial indexes and the effect the strict regulating policies [24]. Both domestic and foreign  
74 research have documented different forms of DEA evaluation models that have been widely used in  
75 various fields of study [25-27], which further proved its importance of sustainable development of  
76 enterprises and its effectiveness in analyzing the technological and scale efficiency for the multi-  
77 inputs and multi-outputs. Hence this paper intends to establish a synergistic evaluation index system  
78 and model of PPC to analyze, evaluate and select the best project portfolio.

79 This paper is structured as follows: Section 2 establishes a scientific and rational evaluation index  
80 system of PPC which takes both financial and non-financial objectives into consideration, via an  
81 extensive literature review. Section 3 evaluates the value of the index and Section 4 proposes a  
82 synergetic evaluation model of the PPC based on the DEA. Section 5 verifies the effectiveness and  
83 feasibility of the model using a computational experiment. Section 6 draws conclusions.

## 84 2. Construction of Synergetic Evaluation Index System of the PPC

85 The success of a project's implementation is affected by not only the amount of capital  
86 investment but also the decision-maker's maturity, managerial skill-sets within the organization, as  
87 well as the components of the project itself. The organization will benefit from financial gains, further  
88 development promotions as well as positive social influence. On the basis of a review of the existing  
89 literature, this paper puts forward the synergetic evaluation of the PPC management index system,  
90 shown as Fig. 1 [10, 11][25-27]:



**Figure 1** Synergetic Evaluation of the PPC Index System

91  
92  
93 PPC synergistic management evaluation index system consists of input indices, output Indices  
94 and auxiliary Indices. By considering the uncertainties both within the organization and the external  
95 social environment, it is too difficult to be absolutely sure about the success of any projects. Therefore,  
96 this paper introduces supporting Indices in the evaluation index system that will indicate the  
97 probability of a project's success under the influence of such uncertainties. The figures of the  
98 supporting Indices were based on the experts' review as well as conclusions from their years of  
99 experience.

100 The organization currently has  $n$  available projects to choose from, which is noted as project set  
101  $E$ ,  $E = \{i_1, i_2, \dots, i_n\}$ , randomly taking  $z$  ( $2 \leq z \leq n$ ) projects from project set  $E$  will forms a new  
102 project portfolio  $K$ . The explanations to the indices and the interaction between the indices under  
103 the synergies are as follows.

## 104 2.1 Input Indices

### 105 2.1.1 Capital Cost

106 Investment funds play the most important role in the implementation of any project. Due to the  
107 synergies between the resources of the project, the capital costs ( $X_1$ ) of the project portfolio is not  
108 equal to the sum cost of each individual project. Under the management of project portfolio  
109 synergistic configuration, the cost of capital formula is shown as below:

$$110 \quad x_{1j_1} + x_{1j_2} + \dots + x_{1j_z} + V_1^K = X_1^K \quad (1)$$

111 Equation (1) shows that under the influence of synergies, by carrying out each project  $z$   
112 separately, project portfolio  $K$  demands less capital  $X_1$  towards the aggregate capital cost  $X_1^K$ . In  
113 the formula,  $x_{1j_z}$  represents the amount of investment capital for investing project  $j_z$  which is part of  
114 the project portfolio  $K$ .  $X_1^K$  represents the total amount of capital cost for investing project portfolio  
115  $K$ ,  $V_1^K$  (negative value) represents the synergistic effect of the cost of capital under the PPC synergistic  
116 management.

### 117 2.1.2 Organizational Capacity

118 Organizational management is the most direct and effective management model within project  
119 management. Organizational capacity ( $X_2$ ) refers to the project manager's management skill which  
120 includes management of funds, manpower, and machinery, etc.

$$121 \quad x_{2j_1} + x_{2j_2} + \dots + x_{2j_z} + V_2^K = X_2^K \quad (2)$$

122 Equation (2) shows that due to the synergistic effect, rather than carrying out each project  $Z$   
123 separately, project portfolio  $K$  requires less organizational capacity ( $X_2$ ) towards aggregate  
124 organizational capacity ( $X_2^K$ ). In the formula,  $x_{2j_z}$  represents the effort of organizational capacity for  
125 investing project  $j_z$  which is part of the project portfolio  $K$ .  $X_2^K$  means the total amount of capital

126 cost for investing project portfolio  $K$ ,  $V_2^K$  (negative values) represents the synergistic effect of the  
 127 organizational capacity under the synergistic management of the PPC.

### 128 2.1.3 Component Function

129 While there are strategic objectives for the organization, the objectives of different projects are  
 130 not always the same. For instance, some projects are for financial gains, while others are for obtaining  
 131 market share. Component function ( $X_3$ ) refers to project component's contribution to the overall  
 132 strategic target of the organization.

$$133 \quad x_{3j_1} + x_{3j_2} + \dots x_{3j_z} + V_3^K = X_3^K \quad (3)$$

134 Equation (3) shows that due to the synergistic effect, rather than carry out each project  $Z$   
 135 separately, project portfolio  $K$  requires less organizational capacity  $X_3$  towards aggregate  
 136 organizational capacity ( $X_3^K$ ).  $x_{3j_z}$  represents the amount of component function involved in  
 137 investing project  $j_z$  which is part of the project portfolio  $K$ .  $X_3^K$  means the total amount of  
 138 component function required for investing project portfolio  $K$ ,  $V_3^K$  (negative values) represents the  
 139 synergistic effect of the organizational capacity under the synergistic management of the PPC.

## 140 2.2 Output Indices

### 141 2.2.1 Economic revenue

142 Economic revenue ( $Y_1$ ) refers to the net present value of the project, which is the core for  
 143 organization development and smooth implementation of projects. The basic requirement for the  
 144 PPC is to achieve higher profits from the synergies of the project portfolio rather than from the profits  
 145 of individual projects.

$$146 \quad y_{1j_1} + y_{1j_2} + \dots y_{1j_z} + U_1^K = Y_1^K \quad (4)$$

147 Equation (4) shows that due to the synergistic effect, the increase in the total economic revenue  
 148  $Y_1^K$  generated by the  $Z$  projects in the form of project portfolio  $K$ .  $y_{1j_z}$  represents the revenue  
 149 generated by the  $j_z$  project in the project portfolio  $K$ ,  $Y_1^K$  refers to the total revenue generated by  
 150 project portfolio  $K$ .  $U_1^K$  (positive value) means the synergistic effect of the value of economic revenue  
 151 under the influence of the PPC synergies.

### 152 2.2.2 Strategic fit

153 Strategic management theory can effectively improve the performance of project portfolio  
 154 management[28], Through building conceptual model which is based on the analysis of interaction  
 155 among project portfolio, corporate strategy and business success, Sascha Meskendah[9] [15] proved  
 156 strategy does effect the project portfolio and business success; Corporate strategic fitness has become  
 157 an international important index for evaluating the effectiveness of the project portfolio[25, 26] [29].

$$158 \quad y_{2j_1} + y_{2j_2} + \dots y_{2j_z} + U_2^K = Y_2^K \quad (5)$$

159 Equation (5) shows that due to the influence of synergies, there is improvement of strategic fit  
 160  $Y_2^K$  by undertaking  $Z$  projects in the form of project portfolio  $K$ .  $y_{2j_z}$  shows how  $j_z$  project in the  
 161 project portfolio  $K$  may affect organizational strategic fit,  $Y_2^K$  refers to the aggregate strategic fit that  
 162 project portfolio  $K$  may generate.  $U_2^K$  (positive value) represents the synergistic effect of strategic fit  
 163 under the influence of the PPC synergistic.

### 164 2.2.3 Social Satisfaction

165 Social satisfaction ( $Y_3$ ) has a direct influence on the long-term development of project portfolio  
 166 and the corporate social image. Those projects that pursue social satisfaction can help achieve or even  
 167 exceed customer expectations, and this may further improve social recognition for current and future  
 168 projects. By establishing customer loyalty and by improving consumer expectations for future  
 169 projects, there will not only be increases in economic revenue as well as benefits to strategic fit, but  
 170 will also garner the support of government and other organizations.

$$171 \quad y_{3j_1} + y_{3j_2} + \dots y_{3j_z} + U_3^K = Y_3^K \quad (6)$$

172 The equation (6) shows that due to the influence of synergies, there will be improvement of social  
 173 satisfaction  $Y_3^K$  by undertaking the  $Z$  projects in the form of project portfolio  $K$ .  $y_{3j_z}$  indicates how  
 174  $j_z$  project in the project portfolio  $K$  may affect social satisfaction,  $Y_3^K$  refers to the aggregate social  
 175 satisfaction that project portfolio  $K$  may bring.  $U_3^K$  (positive value) represents the synergistic effect  
 176 of social satisfaction under the influence of the PPC synergies.

### 177 3. Determination the value of evaluation index

178 Since the evaluation indexes have different characteristics, the data of the six indexes cannot be  
 179 in the same numerical range. Normalization is a simplified method that can eliminate the difference  
 180 of the numerical differences between the different evaluation indexes. Based on data normalization  
 181 method such as linear normalization, energy normalization and component whitening, this paper  
 182 adopts the improved energy normalization method to deal with the index value.

183 Numbers 1 to 6 are respectively assigned to capital cost, organizational capacity, component  
 184 function, economic revenue, strategic fit, and social satisfaction. As mentioned above, project  
 185 portfolio  $K$  has  $z$  projects, each project has 6 indices,  $\alpha_j^K$  represents the value index of  $J$  ( $1 \leq J \leq$   
 186  $6$ ) project from project portfolio  $K$ .  $\alpha_j^{K'}$  stands for the index value of  $J$  from project portfolio  $K$  after  
 187 normalized. The energy normalization can be calculated by the following equation 7 [30]:

$$188 \alpha_j^{K'} = \frac{\alpha_j^K}{\|\alpha_j\|} \quad (7)$$

189 Where  $K$  has  $z$  projects and  $J$  is one of the indicators. In equation (7),  $\|\alpha_j\|$  is the vector norm of  
 190  $J$ , and  $\|\alpha_j\| = \alpha_{j_1} + \alpha_{j_2} + \dots + \alpha_{j_z}$ , where  $\alpha_{j_z}$  represents the value index of  $J$  ( $1 \leq J \leq 6$ ) for project  
 191  $Z$ . As the traditional energy normalization method ignores the actual situation of the corporation and  
 192 their reasonable expectations of the project, equation 7 cannot be directly applied to the DEA  
 193 efficiency evaluation of project portfolio. To take the capital cost as an example, according to equation  
 194 7,  $\|\alpha_1\|$  represents the total investment of project portfolio  $K$ . The traditional energy normalization  
 195 method ignores the financial affordability of the enterprise; in other words, by assuming the  
 196 enterprise's highest capital investment is  $\hat{\alpha}_j$ . When the project portfolio  $K$ 's capital investment is  
 197 greater than  $\hat{\alpha}_j$ , the data processing is meaningless. Therefore, the synergetic evaluation of the PPC  
 198 should always consider the organization's situation in reality as well as its reasonable expectations  
 199 of the project.

#### 200 3.1 Determination the value of quantitative index

201 Capital Cost and Economic revenue are quantitative indices and the values of Capital Cost and  
 202 Economic revenue for the Decision Making Unit can be estimated accurately. The value of the capital  
 203 cost and economic revenue after normalized can be obtained by equation (8)-(9):

$$204 \alpha_1^{K'} = \frac{\alpha_1^K}{\hat{\alpha}_1} \quad (8)$$

$$205 \alpha_4^{K'} = \frac{\alpha_4^K}{\hat{\alpha}_4} \quad (9)$$

206 In equation (8),  $\alpha_1^K$  represents the total number of investments to the project portfolio  $K$ ,  $\hat{\alpha}_1$  is  
 207 the enterprise's highest capital investment,  $\alpha_1^{K'}$  is the value of capital cost after normalized. In  
 208 equation 9,  $\alpha_4^K$  refers to the revenue generated by project portfolio  $K$ ,  $\hat{\alpha}_4$  is the income criterion and  
 209  $\alpha_4^{K'}$  is the economic revenue after normalized. Then, the normalized value of these quantitative  
 210 indices can be calculated accurately.

#### 211 3.2 Determination the value of qualitative index

212 The values of the qualitative indices such as organizational capacity, component function and  
 213 strategic fit are with a very strong sense of uncertainty, it is difficult to get the accurate value for them.  
 214 In order to get them, the peer experts are invited to score the value of the input indices ( $X_2, X_3$ ) and  
 215 output indices ( $Y_2, Y_3$ ) and assess the highest capital investment of ( $X_2, X_3$ ) and the optimum value of  
 216 ( $Y_2, Y_3$ ) by the Likert Scale Method[31,32]. The values of qualitative indices are shown as Table 1:

217

**Table 1.** Values of Qualitative Indices

Indices	Score					Means
	1	3	5	7	9	
Organizational Capacity	$\rho_{21}$	$\rho_{22}$	$\rho_{23}$	$\rho_{24}$	$\rho_{25}$	$\alpha_2^K = (\rho_{21} + 3 \times \rho_{22} + 5 \times \rho_{23} + 7 \times \rho_{24} + 9 \times \rho_{25}) / \sum_{f=1}^5 \rho_{2f}$
Component Function	$\rho_{31}$	$\rho_{32}$	$\rho_{33}$	$\rho_{34}$	$\rho_{35}$	$\alpha_3^K = (\rho_{31} + 3 \times \rho_{32} + 5 \times \rho_{33} + 7 \times \rho_{34} + 9 \times \rho_{35}) / \sum_{f=1}^5 \rho_{3f}$
Strategic Fit	$\rho_{51}$	$\rho_{52}$	$\rho_{53}$	$\rho_{54}$	$\rho_{55}$	$\alpha_5^K = (\rho_{51} + 3 \times \rho_{52} + 5 \times \rho_{53} + 7 \times \rho_{54} + 9 \times \rho_{55}) / \sum_{f=1}^5 \rho_{5f}$
Social Satisfaction	$\rho_{61}$	$\rho_{62}$	$\rho_{63}$	$\rho_{64}$	$\rho_{65}$	$\alpha_6^K = (\rho_{61} + 3 \times \rho_{62} + 5 \times \rho_{63} + 7 \times \rho_{64} + 9 \times \rho_{65}) / \sum_{f=1}^5 \rho_{6f}$

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In Table 1, the  $\rho_{Jf}$  represents the number of times that the index J has be scored, where  $f = (1,2,3,4,5)$ , and the score of this indices are equation to 1 or 3 or 5 or 7 or 9 according to their actual situation. Then, on the basis of equations (8)-(9) , the values of these qualitative indices after normalized can be calculated as equations (10)-(11):

223

$$\alpha_{\beta}^{K'} = \frac{\alpha_{\beta}^K}{\hat{\alpha}_{\beta}} \quad (\beta = 2, 3) \quad (10)$$

224

$$\alpha_{\gamma}^{K'} = \frac{\alpha_{\gamma}^K}{\hat{\alpha}_{\gamma}} \quad (\beta = 5, 6) \quad (11)$$

225

226

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In equations (10)-(11),  $\alpha_{\beta}^K$  and  $\alpha_{\gamma}^K$  are the score of the qualitative input and output indices,  $\hat{\alpha}_{\beta}$  represents the enterprise's highest capital investment for the qualitative input indices and  $\hat{\alpha}_{\gamma}$  is the optimum value of the qualitative output indices,  $\alpha_{\beta}^{K'}$  and  $\alpha_{\gamma}^{K'}$  are the final value of these qualitative input and output indices after normalized. Here, the quantized and normalized values of these quantitative indices can be calculated.

230

#### 4 Construction of the Evaluation Model

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CCR model is a typical DEA analysis method with the advantages of simple, practical, operable, and the results in many applications show that it has a strong advantage in analyzing the technological and scale efficiency for the decision-making units of multi-inputs and multi-outputs [33], which is highly suitable to evaluate the synergetic of PPC. So, this paper puts forward a synergetic evaluation model of PPC from the perspective of inputs as following steps:

236

(1) Absolute effect of single project.

237

(2) Absolute effect of project portfolio.

238

(3) Build the synergetic evaluation model of the PPC.

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242

The absolute effect of single project and project portfolio could ensure the feasibility of the decision-making units, which may not only enable enterprises do not make wrong decisions in the non-effective projects, but also can target to carry on an DEA analysis for the project portfolio in the feasible solution region .

243

##### 4.1 Absolute effect of single project

244 In order to ensure all selected projects in keeping with corporate strategic objectives, the absolute  
 245 effect of single project before proposes a project portfolio is necessary. Assuming the number of  
 246 decision-making units  $DMU$  is  $n_1$ , the input and output indices of each decision-making unit is  
 247 known,  $x_{\beta j}$  is the  $\beta$ th input of  $DMU_k$  (the decision-making unit of project portfolio  $K$ ) and  $X_{\beta}$  is  
 248 the maximum of the  $\beta$ th input of  $DMU_k$ ,  $y_{\gamma j}$  ( $j = 1, 2, \dots, n_1$ ) is the  $\gamma$ th output of  $DMU_k$  and  $Y_{\gamma}$  is  
 249 the minimum expectation of the  $\gamma$ th output of  $DMU_k$  in the premise of given amount of investment  
 250 resources. The amount of investment resources is not more than the  $X_{\beta}$  and the amount of outputs  
 251 is not less than  $Y_{\gamma}$ . Therefore, the equation of absolute effect of project  $j$  can be shown as equation  
 252 (12):

$$253 \quad \begin{cases} x_{\beta j} \leq X_{\beta} & (\beta = 1, 2, 3) \\ y_{\gamma j} \geq Y_{\gamma} & (\gamma = 1, 2, 3) \end{cases} \quad (12)$$

#### 254 4.2 Absolute effect of project portfolio

255 Assuming the number of decision-making units by absolute effect of single project is  $n_2$ , the  
 256 amount of the possible portfolios which needed to through the absolute effect is  $2^{n_2}$ . It is obviously  
 257 that the demand amount of investment resources for the project portfolio  $K$  is not more than total  
 258 amount of investment resource  $X_{\beta}$  and the amount of outputs for project portfolio  $K$  is not less than  
 259 the minimum expectation  $Y_{\gamma}$ . Therefore the equation of absolute effect of project portfolio can be  
 260 shown as equation (13):

$$261 \quad \begin{cases} X_{\beta}^k \leq X_{\beta} & (\beta = 1, 2, 3) \\ Y_{\gamma}^k \geq Y_{\gamma} & (\gamma = 1, 2, 3) \end{cases} \quad (13)$$

262 In equation (13),  $X_{\beta}^k$  represents the total amount of investment resource  $\beta$  for project portfolio  
 263  $K$ , the  $X_{\beta}$  represents the total amount of investment resource  $\beta$ ,  $Y_{\gamma}^k$  refers to the aggregate amount  
 264 of  $\gamma$ th output that project portfolio  $K$  may bring and  $Y_{\gamma}$  is the minimum expectation for the  
 265  $\gamma$ th output in the premise of given amount of investment resources that project portfolio  $K$  may  
 266 bring.

#### 267 4.3 Evaluation model of PPC

268 Assuming the number of decision-making units by absolute effect of project portfolio is  $n_3$ , the  
 269 amount of the possible portfolios is  $2^{n_3}$ . According to equation 13,  $X_{\beta}^k$  represents the total amount  
 270 of investment resource  $\beta$  for project portfolio  $K$  and  $Y_{\gamma}^k$  refers to the aggregate amount of  
 271  $\gamma$ th output that project portfolio  $K$  may bring, the vector of input indices and the output indices are  
 272  $X^K = (X_1^K, X_2^K, X_3^K)^T$  and  $Y^K = (Y_1^K, Y_2^K, Y_3^K)^T$  respectively. According to the DEA principles, the  
 273 weight vectors of input and output indices are  $V = (V_1, V_2, V_3)^T$ ,  $U = (U_1, U_2, U_3)^T$ , the effectiveness of  
 274 decision-making units  $K$  is  $h_k = \frac{U^T Y^K}{V^T X^K}$ . Take the effectiveness of all decision-making units as the  
 275 restrictions, a  $CCR$  model to measure the relative efficiency of the decision-making units  $K$  could be  
 276 constructed, as equation (14) [34]:

$$277 \quad \begin{cases} s. t. \\ \frac{U^T Y^k}{V^T X^k} \leq 1, k = 1, 2, 3, \dots, 2^{n_3} \\ U \geq 0, V \geq 0 \end{cases} \quad (14)$$

278 Let  $s = \frac{1}{V^T X^K}$ ,  $w = sV$ ,  $\sigma = sU$ , the equation 14 could be converted into a linear programming  
 279 problem through the Charnes-Cooper transform, shown as equation 15:

$$280 \quad \begin{cases} \max h_K = \sigma^T Y^K \\ s. t. \\ w^T X^k - \sigma^T Y^k \geq 0, k = 1, 2, 3, \dots, 2^{n_3} \\ w^T X^K = 1 \\ w \geq 0, \sigma \geq 0 \end{cases} \quad (15)$$

281 Solving the dual programming of equation 15, bring the slack variables into this problem, the  
 282 synergetic evaluation model of the PPC could be proposed, shown as equation (16):

$$\begin{aligned}
 & \min \theta \\
 & \left\{ \begin{array}{l}
 \text{s. t.} \\
 \sum_{k=1}^{2^{n_3}} \lambda_k X^k + S^- = \theta X^K \\
 \sum_{k=1}^{2^{n_3}} \lambda_k Y^k - S^+ = Y^K \\
 S^-, S^+ \geq 0
 \end{array} \right. \quad (16)
 \end{aligned}$$

284 In equation (16),  $(X^K, Y^K)$  is the solution set of  $\begin{cases} \sum_{k=1}^{2^{n_3}-1} \lambda_k X^k \leq X^K \\ \sum_{k=1}^{2^{n_3}-1} \lambda_k Y^k \geq Y^K \end{cases}$ ,  $\theta$  is the objective function  
 285 represents the minimum of the investment if the output  $Y^K$  constant. According to DEA principles,  
 286 only  $\theta=1$ ,  $S^- = 0$ ,  $S^+ = 0$ , the *DMU* project portfolio  $K$  in this *CCR* model is valid and the vector of  
 287 input indices is optimal. Otherwise, the DEA is invalid. Then, the synergetic evaluation model of the  
 288 PPC is built, which will provide a reference for project portfolio decision making.

## 289 5. Computational Experiment and Results

290 In order to prove the effectiveness and scientific of the above methods, this paper takes company  
 291 A as a case study. The company is required to choose three out of nine available projects to run  
 292 simultaneously with a RMB 5.9 billion budget while aiming to find the optimal combination of the  
 293 PPC. Based on the annual corporate strategic objectives, the experts' reviews as well as the company's  
 294 input Indices (capital cost  $X_1$ , organizational capacity  $X_2$  and component function  $X_3$ ) and output  
 295 Indices (economic profit  $Y_1$ , enterprise adaptation  $Y_2$  and social satisfaction  $Y_3$ ), the probability of  
 296 success for the project, and the synergistic effect between projects under synergistic configuration are  
 297 shown in the Table 2 below:

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**Table 2.** Initial data of different projects

Project	Output Indices			Input Indices			Probabili ty of Success
	Econo mic Profit	Enterpris e Adaptatio n	Social Satisfacti on	Capit al Cost	Organizatio nal Capacity	Compone nt Function	
1	7700	4.53	6.71	17500	6.63	6.81	0.75
2	3100	8.2	5.53	25000	4.38	7.33	0.65
3	7500	6.14	8.01	19000	6.3	6.93	0.55
4	7000	7.84	7.45	17000	7.3	8.25	0.4
5	6200	8.53	7.23	15800	7.93	6.4	0.7
6	2250	7.54	6.01	23900	4.50	7.53	0.58
7	5600	7.65	5.15	10100	8.13	7.94	0.5
8	6820	5.54	6.84	41900	3.47	5.64	0.7
9	8890	3.92	7.25	34000	2.87	6.93	0.65

$U^{1_{34}}=300$   $U^{2_{23}}=2$   $U^{3_{12}}=2$   $V^{1_{23}}=-2300$   $V^{2_{68}}=-1$   $V^{3_{13}}=-2$   $P_{23}=0.1$   $U^{1_{35}}=200$   
 $U^{2_{35}}=3$   $U^{3_{89}}=1$   $V^{1_{13}}=-2700$   $V^{1_{35}}=-1400$   $V^{2_{23}}=-1$   $V^{3_{35}}=-3$   $U^{1_{68}}=100$   $U^{2_{29}}=2$   $V^{2_{14}}=-2$

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300 Based on the basic conditions of the company such as capital limit and reasonable yield  
 301 thresholds, resource constraints, 10 kinds of portfolios through the absolute effect can be obtained  
 302 according equation 12-13, and the normalized data and the efficiency of decision-making units can  
 303 be calculated by equation 10-16, and the results of them are shown in Table 3:

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**Table 3.** Values of indices and results for DMU of project portfolio

DMUs of project portfolio	composition of project portfolio	output indices			input indices			$\theta$
		Y1	Y2	Y3	X1	X2	X3	
PP-DMU 1	Project 1,2,3	0.6561	0.5279	0.569	0.9417	0.6041	0.7063	1.000
PP-DMU 2	Project 1,2,4	0.5085	0.4394	0.466	0.9917	0.6041	0.8293	0.825
PP-DMU 3	Project 1,2,5	0.5945	0.5444	0.5431	0.9717	0.7015	0.7607	0.916
PP-DMU 4	Project 1,3,4	0.6943	0.367	0.4599	0.8917	0.6752	0.7404	0.931
PP-DMU 5	Project 1,3,5	0.856	0.5149	0.537	0.8033	0.7726	0.5607	1.000
PP-DMU 6	Project 1,4,5	0.7336	0.4631	0.4842	0.8383	0.7356	0.7948	0.903
PP-DMU 7	Project 2,3,4	0.5013	0.4917	0.4568	0.9783	0.6289	0.8337	0.825
PP-DMU 8	Project 2,3,5	0.5979	0.666	0.5339	0.9350	0.6522	0.6541	1.000
PP-DMU 9	Project 2,4,5	0.4525	0.5347	0.431	0.9633	0.7263	0.8141	0.781
PP-DMU10	Project 3,4,5	0.667	0.5051	0.461	0.8400	0.7974	0.6881	0.896

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In Table 3, the efficiency of PP-DMU1, PP-DMU5, PP-DMU8 are 1.000, so these DMUs are valid, and the others are invalid. Analyze these invalid DMUs can obtain the obstacles to the further development of the company, which will provide the decision-making advice for managers.

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### 5.1 Analysis of invalid DMUs

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By analyzing the slack of input and output indices will contribute to find the reasons why the decision-making units are invalid and provide a direction for adjusting the input-output scale. The slack of inputs and outputs for DMUs are shown as Table 4:

**Table 4.** Slack of inputs and outputs for DMUs

DMUs of project portfolio	Insufficient output			Redundant input		
	Y1	Y2	Y3	X1	X2	X3
PP-DMU 2	0.028	0	0	0.045	0	0.106
PP-DMU 3	0.083	0	0	0	0	0.049
PP-DMU 4	0	0.071	0	0.128	0	0.192
PP-DMU 6	0	0	0.002	0.015	0	0.192
PP-DMU 7	0.018	0	0	0.031	0	0.124
PP-DMU 9	0.035	0	0	0	0.038	0.110
PP-DMU10	0	0	0.461	0	0.074	0.091
Mean	0.016	0.007	0.001	0.022	0.011	0.086

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Compared to other project portfolio decision making units, the organizational capacity in PP-DMU9 and PP-DMU10 has exceeded the optimal actual demand, however, this is not a bad thing to the management process as it reflects the fact that the managers in PP-DMU9 and PP-DMU10 could manage more complex projects, which puts forward some favorable suggestions for manager to allocate its' the human resource.

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### 5.2 Analysis of valid DMUs

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From the economic interpretation of this CCR model, the PP-DMU, PP-DMU 5 and PP-DMU 8 are both valid in technological and scale efficiency. These 3 valid DMUs which composed of 3 different projects could help the company managers to narrow the scope of decision-making and improve the level of decision-making. However, the amount of funds (59 million yuan) cannot meet

326 the demand of three valid projects running at the same time. Therefore, based on the needs of the  
 327 company's development at this stage, it is very necessary to select the optimal project portfolio from  
 328 these valid DMUs based on the needs of the company's development at current stage.

329 According to the nature of valid DEA, just consider the situation that different output in the  
 330 same input vector could meet the needs of the analysis of valid DEA. This paper analyzes the valid  
 331 items of DEA from three different situations, and determines the optimal project portfolio, the results  
 332 are shown in Table 5:

**Table 5.** Results of different situations

	DY1	DY2	DY3
PP-DMU 1	0.980	0.856	1.000
PP-DMU 5	1.000	0.902	1.000
PP-DMU 8	0.827	1.000	0.964

334 In Table 5, taking output  $Y_1$ ,  $Y_2$  and  $Y_3$  as the study objects, taking  $X_1$ ,  $X_2$  and  $X_3$  as input  
 335 indices, the economic revenue, strategic fit and social satisfaction can be calculated to reflect the DEA  
 336 efficiency of project portfolio respectively. When the output  $Y_1$  was considered as the study object,  
 337 the PP-DMU 5 is relatively valid, which reflects that the project portfolio is composed of project 1, 3  
 338 and 5 is the best when the economic revenue is considered as the main measurement indices.  
 339 Therefore, when take the output  $Y_1$  and  $Y_2$  as study objects, the best project portfolio in different  
 340 situation such as take strategic fit and social satisfaction as main measurement indices could be  
 341 selected in the same way, which will provide decision basis for the managers to select the best project  
 342 portfolio according to the different requirements.

## 344 6. Conclusions

345 This paper studies the efficiency of the PPC synergistic management by using the DEA method  
 346 under a certain environment. For the selection of Indices, we built up a scientific and rational  
 347 evaluation index system based on the existing research results which takes both financial and non-  
 348 financial objectives into consideration. The scope of this system covers the input indices such as  
 349 capital cost, organizational capacity component function and the output indices includes economic  
 350 revenue, strategic fit and social satisfaction, as well as the auxiliary index: success probability. And  
 351 this system makes it easier to build a synergetic evaluation model of the PPC based on DEA. For data  
 352 processing, an improved energy normalization method is used to eliminate the numerical differences  
 353 between different evaluate Indices. Prior to the evaluation of project portfolio coordination,  
 354 reasonable yield thresholds, resource constraints, and other conditions are set. Subsequently,  
 355 absolute effect on single projects and project portfolio can effectively screen out alternative options  
 356 and further reduce the number of decisions required. Then, a model for selecting the optimal DEA  
 357 effective project portfolio which will provide insights to decision-makers and improve the decision-  
 358 making is proposed, and the results of a computational experiment suggest that this model is  
 359 reasonably for selecting the optimal project portfolio.

360 To our knowledge, this is the first time to apply the notion of synergetic evaluation and DEA to  
 361 the PPC domain, which enriches the theories of project management and makes an important  
 362 contribution to integrating a group of projects into a project portfolio in the synergistic perspective  
 363 and helping an organization optimize its multi-project management. This model is verified by a  
 364 computational experiment from the database of the Chinese firm, and provides a basis for selecting  
 365 the best project portfolio, which contributes to decisions making on the PPC. Practitioners may  
 366 benefit most from applying the finding that the synergetic relationship must be considered and in an  
 367 integrated fashion to achieve the optimal PPC.

368 There are also some shortcomings in this study. (1) the systematic deficiencies of the indices are  
 369 induced by the negative synergistic relationship between indices having not been taken into account,  
 370 and might affect the scientific nature of the evaluation results; (2) The evaluation method of PPC  
 371 synergistic management based on DEA only considers the project at a very specific period of time.  
 372 However, in reality, synergistic effect of projects appears differently at different stages, while demand

373 for resources also varies. Therefore, the PPC multi-stage efficiency analysis will be the authors' future  
374 direction of research. (3) the effectiveness and feasibility of this proposed model can be verified by a  
375 computational experiment, but the selected projects to be implemented only consistent for the  
376 problem of synergetic evaluation and the results of the computational experiment initially cannot be  
377 generalized. These limitations would be further study in the future.  
378

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