

Article

“All that matter ... in one Big Bang ...,” & other cosmological singularities*

Emilio Elizalde^{1,2,3,†} 

¹ Consejo Superior de Investigaciones Científicas, ICE/CSIC and IEEC, Campus UAB, Carrer de Can Magrans s/n, 08193 Bellaterra (Barcelona) Spain; elizalde@ieec.uab.es

² International Laboratory for Theoretical Cosmology, TUSUR University, 634050 Tomsk, Russia

³ Kobayashi-Maskawa Institute, Nagoya University, Nagoya 464-8602, Japan

† Current address: Affiliation 1

1 **Abstract:** The first part of this paper contains a brief description of the beginnings of modern
2 cosmology, which, the author will argue, was most likely born in the Year 1912. Some of the
3 pieces of evidence presented here have emerged from recent research in the history of science, and
4 are not usually shared with the general audiences in popular science books. Then, the important
5 issue of the formulation of the original Big Bang concept, in the exact words of Fred Hoyle, is
6 discussed. Too often, this is very deficiently explained (when not just misleadingly) in most of the
7 available generalist literature. Other frequent uses of the same words, Big Bang, as to name the initial
8 singularity of the cosmos, and also whole cosmological models, are then addressed, as evolutions of
9 its original meaning. Quantum and inflationary additions to the celebrated singularity theorems by
10 Penrose, Geroch, Hawking and others led to subsequent results by Borde, Guth and Vilenkin. And
11 corresponding corrections to the Einstein field equations have originated, in particular, R^2 , $f(R)$, and
12 scalar-tensor gravities, giving rise to a plethora of new singularities. For completeness, an updated
13 table with a classification of the same is given.

14 **Keywords:** The Big Bang concept; history of modern cosmology; singularity theorems; cosmological
15 singularities in modified gravity models.

16 1. Introduction

17 ‘Big Bang’ is one of the very few scientific terms that have transcended its original domain of use
18 and meaning, to become a common expression employed by literally everybody nowadays. It even
19 gives name to a very popular TV series, and this is actually the first meaning that pops up now when
20 you do a search on the internet. Many people associate Big Bang to an extraordinarily huge explosion
21 at the beginning of everything, at the origin itself of our Universe, a bang which scattered all existing
22 matter and energy that was concentrated in a nutshell just a fraction of a second before. Needless to
23 say, this description, which at first sight might seem perfectly reasonable, makes very little sense, more
24 than that, it is in fact utterly wrong, according to what cosmologists now know. But if we try to be
25 more precise and resort to more specialized literature, there still is a lot of confusion going on, what is
26 much more deceiving; the reason being that, commonly, the same two words are applied in several
27 different contexts, with different meanings, never bothering to specify which is which. Only true
28 specialists will not be lost, since they can easily distinguish the different contexts; but we cannot be

*Parts of this paper have been presented by the author, under different titles, in the following 2017 Conferences, Seminars, and Workshops: (i) Università degli Studi di Trento, Trento, Italy; (ii) Kobayashi-Maskawa Institute for the Origin of Particles and the Universe, Nagoya University, Japan; (iii) Yukawa Institute for Theoretical Physics, Kyoto University, Japan; (iv) 5th CORE-U, Core of Research for the Energetic Universe, Hiroshima University, Japan; (v) 4th Korean-Japan Joint Workshop on Dark Energy at KMI, Nagoya, Japan; (vi) IV Cosmology and the Quantum Vacuum, Segovia, Spain; (vii) 3rd International Winter School-Seminar on Gravity, Astrophysics and Cosmology “Petrov School”, Kazan Federal University, Kazan, Russian Federation.

29 satisfied with that, since the Big Bang issue has transcended the scientists' domains and the confusion
30 will persists if we leave things as they are right now. To summarize, this concept is in need of a lot of
31 clarification, one should try to be more precise and clearly distinguish among these several versions
32 and their exact meanings, in each situation, as we will now discuss.

33 There is, to start, the original meaning, the idea that Fred Hoyle intended to convey when he
34 pronounced the two magic words for the first time ever, in order to make an important point clear,
35 concerning two competing models of the cosmos. Then, there is a second, more modern meaning,
36 mathematically very precise (although physically much more blurred): the Big Bang singularity at the
37 very origin of space and time. And there is also the concept of the Big Bang model, with two essential
38 variants, the hot and the cold models, with hot or cold dark matter, variants that were under passionate
39 discussion during several decades and until at least some twenty years ago, in the fine details.

40 To repeat, the author is quite convinced that these issues, although well-known to the true
41 specialists, are in need of a serious discussion and clarification, what, unfortunately, can hardly be
42 done in the reduced space of this article. But he will try, at least, to sketch and start walking along a
43 possible way to be followed in further depth, in future analysis. To be remarked is that there are recent
44 and very important discoveries by historian of science on different aspects of this subject, which need
45 to be digested and put together into a global and detailed description, with the aim to draw a much
46 more clear picture, replacing the wrong or misleading ones that commonly appear in such popular
47 references as the Wikipedia, National Geographic, or even the British Encyclopedia. Maybe the main
48 common problem has always been, and is still now, the following: it turns out that the physics involved
49 in a well-grounded explanation of those issues, namely General Relativity, is far from being trivial,
50 more specifically, far beyond the proper comprehension of most of the authors of those chronicles and
51 short descriptions. And, as we know well, a deep understanding is necessary before you are able to
52 explain physics to your barber.

53 Going into the contents of this paper, after a brief approach, in Sect. 2, to the origins of modern
54 cosmology, which the author will strongly argue it was born in the Year 1912, in Sect. 3 the first of the
55 three different meanings of Big Bang, as discussed above, namely the original one, made explicit in
56 the exact words of Fred Hoyle, will be addressed. Then, in Sect. 4, some of the main developments
57 pertaining to the second meaning, the Big Bang singularity, will be summarized, starting with the
58 classical singularity theorems. Concerning this same issue, quantum and inflationary additions to the
59 celebrated singularity theorems by Penrose, Geroch, Hawking and others led later to two subsequent
60 theorems by Borde, Guth and Vilenkin. And corresponding corrections to the Einstein field equations
61 [1] have originated, among others, R^2 , $f(R)$ and scalar-tensor gravities, giving rise to a bunch of new
62 (mainly future) singularities, which will be summarized there. Sect. 4 ends with a subsection that
63 contains a short discussion of the hot and the cold Big Bang models (the third distinct meaning of these
64 words), supplemented with a selected bibliography of the same. For completeness, in Sect. 5 a table
65 with the classification of the new cosmological singularities, which show up in theories of modified
66 gravity and are now under hot discussion, in the context of the accelerating universe, is given. Finally,
67 Sect. 6 is devoted to conclusions.

68 2. The very origins: Leavitt, Slipher, Hubble, Lemaître, Einstein, ...

69 This section is devoted to a short remembrance of the origins of modern cosmology. Common
70 to the study of any dynamical system, the two main issues in the discussion of the dynamics of the
71 cosmos are the determination both of the distances to celestial objects, and of their velocities. But it
72 turns out that calculating distances to far celestial objects has always been, and is still, one of the most
73 difficult tasks in astronomy. The reader will surely remember the enduring discussions, which lasted
74 for several years, concerning the supernovae SNIa as standard candles (the possible role of dust, of
75 large-scale matter inhomogeneities, etc.), in the precise definition and evolution of the distances with
76 time, which eventually led to the highly surprising and remarkable result of the acceleration of the
77 cosmic expansion.

78 2.1. Old models of the Universe

79 But here we are looking back into the early history of modern cosmology, which started, in the
80 authors' opinion, in the first half of the second decade of last Century. Before that, however, we should
81 throw a quick look into a much more remote past, with the main purpose of realizing how difficult it is
82 to calculate astronomical distances. Recall that in the first models of our Universe, as the celebrated one
83 by Anaximander (ca. 610 - 546 BC) [2] an early pre-Socratic philosopher from the Greek city of Miletus,
84 the Sun was considered to be the most distant object from the Earth; and this in spite that, in this time,
85 Greeks could see in the night sky many more stars and galaxies with the naked eye that we are able to
86 observe from our polluted cities nowadays. Of course there was a scientific reason for the Sun being
87 that distant, since (recall the four-element theory) the Sun is fire and fire always goes up, therefore... In
88 Anaximander's universe the Moon was the second most distant object (another fire, but smaller than
89 the Sun), while stars were constrained to a cylinder much more close to us. Anaximander's universe
90 was very advanced to his time; apparently he was the first cosmologist to get rid of Atlas, the hero who
91 prevented the Earth from falling down and which had been omnipresent in previous Greek models of
92 the cosmos. For Anaximander everything, including the Earth, was floating in space (the ether, if you
93 want) in perfect equilibrium, with the measures of the Earth, the radius of the Moon and Sun's orbits,
94 etc., keeping accurate harmonic proportions.

95 In the Ptolomean universe of the second Century AD there are several important changes, which
96 for the sake of conciseness will not be discussed in any detail here, but the stars continue to be closer to
97 the Earth than the Sun. It is not until the Copernican revolution that we can find an 'official' map of the
98 cosmos where stars are depicted outside and far away, the Sun lying now at the center of the universe,
99 as can be seen in the very famous Thomas Digges' representation, of 1576, of the Copernican universe
100 [3]. This was a true revolution that went on during the centuries to follow, to eventually 'enlarge' the
101 dimensions of the observable Universe to those of our Milky Way. And here ends our short travel to
102 the remote past.

103 Such was actually the situation at the beginning of the XXth Century. Indeed, the Milky Way was
104 the entire observed Universe: all stars, spiral nebulae, and other celestial objects were considered to be
105 inside of our own galaxy, none of them was suspected to lie far beyond its boundaries. Moreover, all
106 those objects were moving in perfect equilibrium, that is, the Universe was static. Again, there was
107 a strong scientific reason for that, for such is the final result of the evolution of any physical system
108 under quite general conditions and the Universe, being eternal, had had enough time to evolve and
109 reach such regime. It was precisely this beautiful model of the Universe: eternal, static, and small as
110 the Milky Way, which led Albert Einstein to the most horrible blunder of his whole life: "... die größte
111 Eselei meines Lebens!" where, according to George Gamow, his exact words [4].

112 2.2. Henrietta Leavitt

113 By now we should have grasped already how extremely difficult it is to calculate distances in
114 astronomy. The order of magnitude of the mistakes committed in this respect during past epochs are
115 just colossal. And this is precisely why the first hero in our story, in fact a she-hero, a heroine, must
116 undoubtedly be Henrietta Swan Leavitt. Such was the importance of the extraordinary discovery
117 she did in 1912 –after several years of collecting thousands of data, in particular from the Magellanic
118 clouds– namely the period-luminosity relationship of Cepheid variable stars: a linear dependence
119 of the luminosity vs the logarithm of the period of variability of the star's luminosity [5]. It would
120 be interesting to describe the favorite physical mechanisms available to explain such relationship
121 (as the Eddington valve [6], for a very beautiful one), but regrettably there is no place here for that.
122 Henrietta was a distinguished member of the so-called Edward Pickering's Harvard harem, or better
123 known as Harvard computers, a group of young ladies that did a tremendous job in astronomy during
124 that time (the interested reader can find in, e.g. [7], more details). Leavitt's result was an extremely
125 powerful weapon to calculate distances, in fact the main tool used by Hubble in the years to follow,
126 and subsequently by several generations of astronomers with remarkable success, until the advent of

127 other improved techniques [8] that have culminated in the SNIa standardizable candles mentioned
128 above [9].

129 2.3. *Vesto Slipher*

130 Our second hero in this story is, again by his extraordinary merit, the well-known astronomer
131 Vesto Slipher who, starting on the very same year 1912 obtained the first radial velocities of spiral
132 nebulae from their spectral blue- or red-shifts, by using the 24-inch telescope of the Lowell Observatory,
133 in Arizona. Actually his first calculation, which he produced on Sep. 17, 1912, was for the Andromeda
134 nebula, a blueshift [10]. In 1914, in a meeting of the American Astronomical Society, he presented
135 results for 15 nebulae, results that were received by the audience (chronicles say) with a very long,
136 standing ovation [11]. This is most unusual, in a scientific conference, then and now. He was, without
137 any doubt (as Hubble himself later recognized), the first astronomer to see that something highly
138 remarkable and very strange was going on in the static model of the cosmos: those distant nebulae
139 escaping from us at such enormous speeds, and it is very clear that the importance of his discovery
140 was immediately appreciated by the attendees, according to the chronicles.

141 Now, with *distances* and *speeds* the two necessary tools were ready for the greatest revolution in
142 the study of the cosmos to occur: a radical conceptual change that marked the beginning of modern
143 cosmology.

144 2.4. *A Great Debate*

145 Before continuing along this line, a very short mention of the so-called Great Debate [12], Harlow
146 Shapley vs Heber Curtis, which took place at the Smithsonian Institution in Washington on Apr. 26,
147 1920. Shapley defended the orthodox view that the Milky Way was the entire Universe, while Curtis,
148 his opponent, raised serious doubts, one of his arguments being that an unusual concentration of
149 novae stars had been reported in Andromeda, this pointing to the possibility that such nebulae was in
150 itself another world, another universe disconnected from us and similar to the Milky Way.

151 In any case, it seems clear from the chronicles that, in this case, nobody won that debate, none of
152 the two astronomers could convince the opponent with his arguments and, at the end of the day, the
153 result of the scientific contest was a draw. There are several very nice accounts of this famous debate
154 and of this epoch of astronomy (see, e.g., [13], and for additional material on subsequent developments
155 [14]).

156 2.5. *An Island Universe*

157 Nov. 23, 1924, is the following important date in this story. That day, on the 6th page of the New
158 York Times the following news appeared:

159 "FINDS SPIRAL NEBULAE ARE STELLAR SYSTEMS; Dr. Hubbell Confirms View
160 That They are 'Island Universes' Similar To Our Own.

161 WASHINGTON, Nov. 22. Confirmation of the view that the spiral nebulae, which
162 appear in the heavens as whirling clouds, are in reality distant stellar systems, or "island
163 universes," has been obtained by Dr. Edwin Hubbell of the Carnegie Institution's Mount
164 Wilson observatory, through investigations carried out with the observatory's powerful
165 telescopes."

166 Some months before that day, in 1923, Edwin Hubble had spotted a Cepheid variable star in a (now
167 very famous) photographic plate of the Andromeda nebula, namely the variable Cepheid star V1 [15]
168 and, using Leawitt's law, he was able to calculate a distance of 285 kpc to the Cepheid. To his surprise,
169 this was about ten times larger than any other distance calculated before for celestial objects in the
170 Universe, what very clearly supported the view that Andromeda was definitely outside of the Milky
171 Way. Hubble presented his results to the Meeting of the American Astronomical Society that took place
172 in Washington starting Dec. 30, 1924. On Jan. 1, 1925, he submitted his contribution, which was read in

173 fact by Henry Russell, the director of the Princeton University Observatory, who had forced Hubble to
 174 present his still unfinished paper. Its title was “*Cepheid variables in spiral nebulae*”, and was read in the
 175 joint morning session of astronomers, physicists and mathematicians. It won the year’s 1,000 dollar
 176 prize of the American Association for the Advancement of Science (to concur to the prize was the real
 177 reason for such urgency).

178 This was indeed an astonishing discovery, one that finally decided the result of the Great Debate,
 179 substantiated the ideas of philosophers, as Immanuel Kant, and completely changed our vision of the
 180 cosmos. It has been righteously highlighted in innumerable occasions.

181 However, what Hubble seems not to have been aware of at that point, and many scientists (and,
 182 incredibly, most of the references to the subject) still ignore *even today!*¹ is that, two years before
 183 Hubble, a well-known Estonian astronomer, Ernst Öpik, had published a paper in the prestigious
 184 *Astrophysical Journal* [16], in which he had obtained a distance to Andromeda of 450 kpc, what is
 185 much closer to the actual value of 775 kpc than the value obtained by Hubble! Öpik used a very
 186 different method to calculate the distance [16], which has nothing to do with the presence of a Cepheid
 187 star. His method was based on the observed rotational velocities of the galaxy, and on the assumption
 188 that the luminosity per unit mass was the same as that of the Milky Way. Although Öpik was a reputed
 189 astronomer at the time and, on top of this discovery, he was the first to calculate the density of a white
 190 dwarf, very few, outside of the community of astronomers, remember his name now.

191 2.6. Hubble’s law

192 In the late 1920s, putting together the table of *Radial velocities in km/s of 25 spiral nebulae* published
 193 by V.M. Slipher in 1917 [17] (which, by the time, had even appeared in Eddington’s book [18]) and
 194 his own table of *Distances in Mpc of spiral nebulae* [19], Edwin Hubble obtained the very famous law
 195 that bears his name, and published it in 1929 [20]. When one puts side by side the two tables one
 196 immediately realizes how easy is to fit the values to a straight line, $V = H_0 D$, with H_0 a constant,
 197 named now after Hubble. He did not mention in his paper that Slipher was the author of the redshift
 198 table and, even today, in many references to his work he is wrongly considered to have produced both
 199 tables: the one of the distances and the other of the redshifts.

200 It is fair to say that Hubble did later recognize Slipher’s remarkable contribution, and in all of its
 201 importance. Indeed, in a Letter to V.M. Slipher, of March 6, 1953 [21], he wrote:

202 “... *your velocities and my distances...*”

203 More than this, Hubble acknowledged the great influence of Slipher’s seminal and important
 204 contribution to his own subsequent work by declaring that [22]:

205 “... *the first steps in a new field are the most difficult and the most significant. Once the barrier*
 206 *is forced further development is relatively simple.*”

207 In fact, it was Slipher the first to realize, as we have explained above, that something very important
 208 and remarkably strange was going on in the Universe model: how on Earth could it be static with
 209 those distant nebulae getting away from us at such enormous speeds?

210 2.7. The interpretation of Hubble’s law

211 As advanced, Hubble’s law is quite easy to obtain from the two aforementioned tables, but this is
 212 by no means the whole point, not even the *main* one. The key issue is the *interpretation* of Hubble’s law.
 213 Namely, (i) do the high escape velocities of the spiral nebulae correspond to real displacements of the
 214 celestial objects (as was believed by *everybody* at the beginning) or, (ii) on the contrary, they correspond
 215 to the movement of the reference system, to an expanding space? Of course, the obvious answer is

¹ This being one of the reason why it is my inescapable duty to explain all that here with such emphasis.

216 that, in fact, both contribute to the redshift; even today this is a most difficult problem in astronomy:
217 to disentangle these two components in the observational redshift maps of astronomical objects. But
218 we are here talking of the movement of very distant objects where we know now that the second
219 interpretation (and the corresponding contribution) prevails, without any doubt. This interpretation
220 was extremely difficult to understand at the beginning and the only accepted explanation was the first
221 (what no popular-science writer seems to be able to grasp now, in retrospect!).

222 Further to this point. From recent studies of historians of cosmology it seems now clear that
223 Hubble never believed that the universe was expanding. What is without question is that he never
224 wrote this statement in any of his works. In a letter of Hubble to Willem De Sitter, in 1931, he stated his
225 thoughts about the velocities by saying: [23]

226 *“... we use the term ‘apparent velocities’ in order to emphasize the empirical feature of the*
227 *correlation. The interpretation, we feel, should be left to you and the very few others who are*
228 *competent to discuss the matter with authority.”*

229 A second important remark is also in order. It is written in books and in many other places in the
230 literature that it was Hubble the one who convinced Einstein that the Universe was expanding, when
231 the later visited Hubble at Mount Wilson in 1931, during his famous tour in the USA that year. But,
232 examining in detail Einstein’s notebooks and other writings, it has been unveiled now that he was
233 actually convinced –in 1931 in fact– by Eddington, Tolman, and de Sitter (*not at all by Hubble*) of both
234 the fact that his static model was unstable and that the Universe was actually expanding [24].

235 As is well known, Einstein had introduced his famous cosmological constant in 1917 (exactly
236 100 Years ago now), as an additional term to his field equations of General Relativity –which he had
237 previously derived, in final form, in 1915– in his attempt to describe with them the whole Universe.²
238 As we have pointed out, the Universe, at that time, was considered to be static and everybody believed
239 that it was reduced to the Milky Way. But a static Universe is not a solution of the original Einstein’s
240 equations (nor of Newtonian physics), since it will definitely collapse under the influence of the
241 gravitational force. With an appropriate sign, the cosmological constant would provide a repulsive
242 force preventing this collapse. When Einstein finally got convinced of the Universe expansion, he
243 pronounced his famous sentence recognizing his horrendous mistake, as reported above.

244 2.8. *George Lemaître and the expanding Universe: a perfect example of Stigler’s law of eponymy*

245 But, who was the first person on Earth to understand that space, the fabric of the Universe was
246 expanding? We come here to our next huge surprise: it turns out that Hubble was not the first to
247 derive Hubble’s law. There is a famous principle, widely known now under the name of Stigler’s law
248 of eponymy [25], which states that:

249 *“No scientific discovery is named after its original discoverer”.*

250 The reader may have realized that we are encountering several clear examples of this principle here.

251 While working for his PhD Thesis at MIT (Cambridge, MA, USA), George Lemaître rediscovered
252 Friedmann’s mathematical solution to Einstein’s equations. But he was in no way a mere
253 mathematician, but a true physicist pursuing to build a cosmological model in accordance with

² Theoretical cosmologists may, alternatively, consider the Year 1915, when Einstein completed his formulation of the gravity field equations, incorporating his revolutionary principle of equivalence, as the one actually marking the beginning of modern cosmology. This is, in particular, the opinion of one of the referees of the present paper. Indeed, the moment Einstein had his “most happy thought” unveiling the relativistic role of the equivalence principle is another seminal event from which the whole theoretical framework stems. Also, the expansion of the universe was first apparent in the work of Friedmann, and partly on de Sitter’s 1917 contributions. I am myself a theoretician and, although I recognize that GR is probably the most beautiful and transcendental theory of Physics ever conceived and constructed, I still stand by my opinion, as expressed above. Which is also supported by the fact that the very important developments of 1912 preceded those of 1915 and 1917.

254 the astronomical observations. No wonder then that he went to visit the most prominent astronomers
255 of the time, in particular Vesto Slipher, at Lowell Observatory in Arizona, and Edwin Hubble at Mount
256 Wilson, and got from them the two aforementioned tables, namely the one of redshifts, and that of
257 distances. It was for him a child's play to discover the correlation and immediately obtain Hubble's
258 law, two years before Hubble.

259 Actually, he did this only after having submitted his PhD Thesis at MIT in 1925, since he had
260 had no time in Boston to complete the whole study leading to his cosmological model. What he
261 finally finished on his return to Belgium, to teach at the Catholic University of Leuven. In 1927 he
262 published his complete results, in a Belgian journal of very low impact (Annals of the Scientific Society
263 of Brussels) [26]. Those who know French may check that, in fact, Hubble's law is already there, with
264 a value of the Hubble constant very close to the one obtained by Hubble in 1929, since the late just
265 added a couple of extra nebulae to the tables (with the new redshifts having been obtained by his
266 coworker Milton Humason) [27].

267 During the Fifth Solvay International Conference on Electrons and Photons, which took place
268 in Brussels in Oct. 1927 (a most famous meeting, because 17 of the 29 participants appearing in
269 the celebrated picture of the meeting were already, or later became, Nobel Prize winners), Lemaître
270 approached Einstein, handing him his recently published paper. He told Einstein, in short, that he
271 had discovered a solution to his original field equations, which would correspond to an expanding
272 universe, perfectly matching the latest astronomical observations. His cosmological constant was
273 not necessary at all, he told Einstein, quite on the contrary, the static universe solution that Einstein
274 obtained by adding it was, in fact, unstable! Some days later, after having examined Lemaître's
275 calculations with some care, Einstein's answer to him was that he could not find any mistake in the
276 mathematical formulas but that his physical insight, the fact that the universe was expanding, was
277 nonsensical (*abominable*, in French, as Lemaître reported later).

278 It turned out that Einstein had already rejected this same idea in an answer to a letter from
279 Friedmann on the same issue, some years before. Even worse, his first answer to Friedmann had
280 been that his equations were in error! what he had to retract few weeks later, after a complaint by
281 Friedmann that this was not at all the case. But even this had not convinced Einstein of the feasibility
282 of an expanding universe. Nor was he convinced by Lemaître and by the clear astronomical evidence
283 that he showed to him, for the first time.

284 The (rather astonishing) fact that it took Einstein –the creator of General Relativity, the master of
285 space and time, the discoverer of gravitational lenses and gravitational waves– still four full years,
286 until 1931, to become convinced of the fact that the Universe was actually expanding may seem now
287 very strange. On the contrary, this just supports the author's conviction that such was indeed, at the
288 time, an extremely revolutionary idea, which many (starting with Hubble) could not comprehend in
289 all its significance.

290 Lemaître was, for a while, the only guy on Earth who was comfortable with the idea that space
291 was in fact expanding, and he had a very hard time to convince other colleagues of this discovery. The
292 first one to understand his model was Arthur Eddington, who knew Lemaître well from a visit of the
293 later to Cambridge (England), previous to his stay at MIT. Eddington, for one, had also proven by
294 himself that Einstein's static solution (of the equations with the cosmological constant) was unstable,
295 and he was already working along the idea of a possibly expanding universe, so that when he saw
296 Lemaître's paper he realized at once that this was the solution he had been looking for. He was
297 positively surprised to see all the work already done, and even more, that the result was in full
298 accordance with the astronomical data.

299 In 1930, Eddington published, in the Monthly Notices of the Royal Astronomical Society, a
300 long commentary on Lemaître's 1927 article, in which he described it as a "brilliant solution" to
301 the outstanding problems of cosmology [28]. Moreover, Eddington helped Lemaître to translate
302 his paper to English, and it was published in March 1931 in the prestigious Monthly Notices of the
303 Royal Astronomical Society, but only the first part ("*première partie*") of it [29], which does not contain

304 Hubble's law. For some decades it remained a mystery why the second part of the paper was not
305 translated. It now seems that this was a personal decision of Lemaître himself, who did not consider
306 these results to be so important any more, after the appearance of Hubble's paper that improved them
307 somehow [27]. I would add to this my own personal considerations, which I think are quite reasonable:
308 Lemaître must have been perfectly aware of the fact that the tables of data from which he had obtained
309 Hubble's law before Hubble himself were handed to him, graciously, by their authors, namely Slipher
310 and Hubble. To derive from them the correlation had been a simple exercise.

311 However, it still remains, as stressed above, the most crucial issue of the interpretation of the law as
312 an expansion of the Universe, and in this aspect Lemaître had no rival; quite on the contrary, he was so
313 much ahead of everybody else that he had a very hard time trying to convince the rest of cosmologists
314 that this was the true reality, indeed. Anyhow, that I know, Lemaître never complained, in his whole
315 life, for not having been credited with the discovery of the Universe expansion.

316 3. "All matter ... in one Big Bang ..."

317 In this section we will explain the original meaning of 'Big Bang', as crystal clearly expressed in
318 the sentence of Fred Hoyle, the man who pronounced these two words together, for the very first time,
319 in 1949.

320 Looking backwards in time, into the past evolution of the cosmos, Lemaître judiciously argued
321 that if the Universe was expanding it should have had an origin. That is, at the beginning, all matter
322 and energy, as space itself, should have been constrained to a small region, a nutshell. In a meeting of
323 the British Association on the relation between the physical universe and spirituality, he proposed in
324 fact that the Universe expanded from an initial point-like structure, namely a "*Primeval Atom*", or a
325 "*Cosmic Egg exploding at the moment of the creation*", as his precise words were. In 1931, he published
326 this theory in *Nature* [30]. It is really shocking that this erroneous, absolutely misleading (in our
327 present understanding) theory of the origin of the Universe is now much better known to the public
328 than Lemaître's extraordinary contributions and insight concerning the expansion of the cosmos, as
329 described in detail in the previous section, and which are largely ignored, all tribute going to Hubble
330 and Friedmann. Maybe the reason is that everybody understands what an explosion is, sending debris
331 everywhere, even if it is that of an enormously huge bomb. But who is really able to grasp the sense of
332 the fabric of space expanding extremely fast? and thereby allowing for the possibility (according to
333 GR) of the creation of big amounts of matter and energy (e.g., eventually, the quark-gluon plasma) *out*
334 *of nothing!*. Moreover, that the total content of matter and energy of the Universe is zero (or almost
335 zero, for all we now know). Nobody, not even a vast majority of trained physicists, much less popular
336 science writers (as I will certify below), but only true specialists on the subject of GR can actually deal
337 with these concepts.

338 To wit, I will here reproduce some of the crazy definitions of "Big Bang" recently encountered in
339 the internet, in different places and languages.

340 3.1. Some common popular sources on the Big Bang

341 **Wikipedia webpage:** "If the known laws of physics are extrapolated to the highest density regime, the
342 result is a singularity ..." "Since Georges Lemaître first noted in 1927 that an expanding universe could
343 be traced back in time to an originating single point, scientists have built on his idea ..." "Extrapolation
344 of the expansion of the universe backwards in time using general relativity yields an infinite density
345 and temperature at a finite time in the past ..."

346 **French Wikipedia:** "De façon générale, le terme "Big Bang" est associé à toutes les théories qui
347 décrivent notre Univers comme issu d'une dilatation rapide qui fait penser à une explosion ..."

348 **Italian version:** "La fase iniziale calda e densa è denominata "Big Bang" ..."

349 **The National Geographic:** “Before the big bang, scientists believe, the entire vastness of the observable
350 universe, including all of its matter and radiation, was compressed into a hot, dense mass just a few
351 millimeters across.”

352 **Global Britannica:** “Its essential feature is the emergence of the universe from a state of extremely
353 high temperature and density: the so-called big bang ...”

354 **NASA webpage:** “Was the Big Bang an explosion? No, the Big Bang was not an explosion. We don’t
355 know what, exactly, happened in the earliest times, but it was not an explosion in the usual way that
356 people picture explosions. There was not a bunch of debris that sprang out, whizzing out into the
357 surrounding space. In fact, there was no surrounding space. There was no debris strewn outwards.
358 Space itself has been stretching and carrying material with it.”

359 Of all those, only the very last definition, and in part the last but one, in its indefiniteness, can
360 be saved. All the rest reduce to re-formulations of Lemaître’s concept of the (in his own words)
361 “*Cosmic Egg exploding at the moment of the creation*” that was proven to be absolutely erroneous and
362 fully misleading by nuclear physicists already before the end of the thirties of last Century [31], and
363 onwards to the 1940s [32], where the activity in this direction was extraordinary. For several reasons, it
364 was by then already appreciated that it was absolutely impossible that the whole matter and energy of
365 the present universe could have been initially present, already, and confined to a nutshell. What is
366 most incredible is that, if this impossibility was so crystal clear almost 80 years ago, this utterly wrong
367 definition continues to be present in almost all books, encyclopedias and general references today.

368 3.2. Fred Hoyle

369 Further to the point, among these nuclear physicists and astrophysicists there was one named Fred
370 Hoyle (1915-2001), an English astronomer noted primarily for the theory of stellar nucleosynthesis,
371 on what he wrote groundbreaking papers [33]. During the II World War, he worked on Britain’s
372 radar project with Hermann Bondi and Thomas Gold. Although Hoyle never got the Nobel Prize, his
373 colleague William Fowler, who did get it in 1983 for work on stellar nucleosynthesis, recognized that:

374 “*The concept of nucleosynthesis in stars was first established by Hoyle in 1946*”.

375 Hoyle had always found the idea that the universe could have a beginning to be pseudoscience, mere
376 arguments for a creator,

377 “... for it’s an irrational process, and can’t be described in scientific terms”; “... belief in the first
378 page of Genesis”.

379 Hoyle, Gold and Bondi published in 1948 their (later quite famous) *steady state theory*, involving a
380 “*creation or C-field*”. The reasoning was the following. Like many other physicists in the 1940’s, they
381 continued to believe that the static model of the Universe was the right one. There had never been
382 any doubt that Hubble’s law was correct; therefore, in order to compensate for the matter density loss
383 due to the distant galaxies going away from us, they had to introduce a term in their equations, which
384 created matter in far regions of the cosmos, at a rather smooth rate. This was the creation or C-field.
385 And how did they manage to generate matter out of ‘nothing’? Very simple, they just used General
386 Relativity to do this job. They involved in their theory exactly the same physical principle that allows
387 for the creation of the quark-gluon plasma in most of present day’s inflationary theories.

388 3.3. The ‘free lunch’ concept

389 Regretfully, nowadays it is not so widely known that the concepts of a universe of “*zero total*
390 *energy*”, or the “*free lunch*”, namely keeping this zero-energy balance along the formation and
391 subsequent evolution of the universe, are not concepts invented by A. Guth, A. Linde or A. Vilenkin,
392 nor by any of the inflation physicists. These concepts are very clearly explained already, e.g., in the
393 famous book by Richard C. Tolman of 1934, “*Relativity, Thermodynamics, and Cosmology*” [34]. There,
394 one finds how

395 “... a closed universe can equal zero energy. All mass/energy is positive and all gravitational
396 energy is negative, and they may cancel each other out, leading to a universe of zero energy”.

397 This is now called, in Allan Guth’s brilliant lectures at MIT the “*Miracle of Physics No. 2*” [35]. It is
398 preceded by the “*Miracle of Physics No. 1*” [35], as explained in the same lectures, which is actually
399 the one that interests us now, to begin with. Keeping the energy balance (or principle of energy
400 conservation) all the time, in accordance with General Relativity, and in particular with Friedmann’s
401 equations, where we see that matter/energy density goes together with pressure of the reference
402 system, it turns out that a positive amount of matter/energy can be generated provided an equivalent
403 amount of negative pressure, e.g. an expansion of the reference system (in mathematical terms), or of
404 the fabric of space (in physical ones), is available (aka inflation).

405 But we have got too far along this way and we need now get back to the point. Hoyle perfectly
406 new, in the late 1940s, that it was absolutely impossible for the whole matter and energy of the universe
407 to be initially present, already at the very beginning, and confined to a nutshell. To start with, all but
408 the three or four lightest elements had to be generated under much more energetic conditions, e.g.
409 in star explosions (stellar nucleosynthesis), a physics that he pioneered. And he also realized that,
410 in Lemaître’s model, these lightest elements had to be generated *all at once* at the beginning of the
411 universe: all that huge amount of matter, and instantly! –unlike in his coauthored *steady state theory*,
412 where this took place quite smoothly, in far apart regions of our universe, and in small proportions.
413 In Lemaître’s model one would need such an enormous blow of space, an incredibly large negative
414 pressure of the reference system, in order to be able to create, instantly, such huge amount of positive
415 matter/energy.

416 3.4. A Big Bang!

417 This is what Hoyle had in mind, and it is exactly, word by word, what he said in the now very
418 famous BBC radio’s Third Program broadcast of March 28th, 1949:

419 “[Lemaître’s model implies that] ... all matter in the universe was created in one **Big Bang** at a
420 particular time ...”.

421 This one (and no other!) is the precise meaning of ‘Big Bang’ according to the person who came
422 up with these two words for the first time ever, in order to express the idea of an *impossible blow of space*
423 being needed to create all that matter in the universe instantly, in accordance with the fundamental
424 principles of General Relativity.

425 Now, again, how can one explain that such well formulated concept, rigorously expressed, with
426 so precise words from the very beginning, is today explained in popular references in such absurd
427 ways? In my view, I repeat, this is because while everybody understands the meaning of a Bang as an
428 ordinary explosion scattering matter in all directions, only very, very few will understand the concept
429 of a Bang of the fabric of space, an enormous blow that allows for the creation of large amounts of
430 matter out of nothing, without violating the energy conservation principle.

431 I must stress again the enormous contradiction pervading all these popular references above.
432 Lemaître is now remembered for the *wrong* reason, namely for his primordial atom model –that was
433 so far from reality– and never for his fabulous insight and wonderful cosmological model of 1927, so
434 much advanced to his time that not even the greatest physicists of the epoch, Einstein included, could
435 understand. Exactly the same misunderstanding happens with Hoyle, who is now only remembered
436 as the proposer of the discredited Steady State theory of the universe, which proved to be a wrong
437 model in the end –and for having prevented the teaching of the universe expansion in Cambridge
438 during decades, even much after the Cosmic Microwave Background (CMB) radiation was detected
439 [36] (also his panspermia ideas did not help at all). But this attitude was just because he considered
440 that such an incredible blow of space, which he called Big Bang and it is now called inflation, and has
441 become the standard theory of the universe origin, was absolutely impossible to happen, it could not
442 be! in his understanding.

443 John Gribbin, in Hoyle's obituary, beautifully called "*Stardust memories*" [37], writes:

444 *"Everybody knows that the rival Big Bang theory won the battle of the cosmologies, but few (not*
445 *even astronomers) appreciate that the mathematical formalism of the now-favored version of Big*
446 *Bang, called inflation, is identical to Hoyle's version of the Steady State model".*

447 Truly, Hoyle was the stardust guy, the man who proved to us that we are all stardust, our bodies
448 containing a bunch of elements that are nothing but ashes of star explosions. This sounds to me as first
449 class poetry, as is also the beautiful title of Hoyle's obituary. However, in my humble opinion, to say
450 that the mathematical formalism of inflation is just the same as that of Hoyle's coauthored Steady State
451 model is simply going too far, it is not certain, as also many inflation specialists will tell you. What is
452 indeed true, as I want to stress again, is that the *underlying physics*, the physics that allows creating
453 matter out of negative pressure and keep the energy balance till the end of the process, is certainly the
454 same physics of inflation, as beautifully explained in Tolman's book of 1934 [34]. But this is ultimately,
455 in essence, just General Relativity, interpreted, as it should be, in the proper way.

456 An important remark is here in order, namely that Hoyle invoked the Big Bang (which you may
457 call now 'inflation') just with one single purpose, namely in order to create matter/energy, and not
458 for any of the other crucial reasons which ultimately led to its formulation by Allan Guth in his very
459 famous paper published on 15 January 1981 [38], namely the horizon problem, flatness, causality, the
460 monopole problem, and so on. This should have been clear already from the above discussion, but it
461 must be properly stressed.

462 4. The many different faucets of the concept of Big Bang

463 The confusion we have addressed above, which arises in the definition of the term Big Bang in the
464 popular literature, is even worsened because the same expression has been used, since 1949, in other
465 different contexts. Until now, we have here only considered the original meaning of Big Bang, namely
466 the one coming out of the mind and exact words of Fred Hoyle, the author of such expression. But it
467 turns out that in the almost seventy years elapsed since then, the same two words have been used in
468 more or less related subjects, notably, in physics, the Big Bang Singularity, the Hot and Cold Big Bang
469 Models, and outside of physics in innumerable contexts, in novels, movies, and in a very popular TV
470 series. No wonder, this last is actually the first meaning that inevitably appears now when one does a
471 search on the internet. Thus, whenever one uses the term "Big Bang" one should immediately specify
472 which of these concepts one is actually refereeing to. This is too often not the case in the literature,
473 adding to the general confusion.

474 4.1. The Big Bang Singularity

475 Nowadays, in many scientific sources, including pictures and plots of the evolution of the
476 Universe, the most common use of Big Bang is to refer to the singularity at the origin of the Universe. I
477 will not discuss this second meaning of Big Bang in much detail, since this is not the main scope of this
478 paper, but just give a brief summary.

479 4.1.1. The Belinsky-Khalatnikov-Lifshitz and the Misner Singularities

480 In the 1960s, one of the main cosmological issues being studied by the Landau group in Moscow
481 was about the possible time singularity at the origin of the Universe. In particular: (i) whether
482 cosmological models based on general relativity necessarily contain a time singularity, or (ii) if
483 actually the time singularity was an artifact of the assumptions used to simplify these models (such as
484 homogeneity and isotropy of the universe). In several papers published between 1963 and 1971 [39],
485 Belinsky, Khalatnikov and Lifshitz (BKL) proved that the universe oscillates around a gravitational
486 singularity, in which time and space become equal to zero.

487 They also showed that the singularity is not artificially created by the simplifications made by
488 the other special solutions, such as the Friedmann-Lemaître-Robertson-Walker, quasi-isotropic, and

489 Kasner solutions. Their model was described by an anisotropic, homogeneous, chaotic solution to
 490 Einstein's field equations of GR.

491 In 1969 Charles Misner constructed a similar model [40], named the mixmaster universe, which
 492 was also homogeneous but not isotropic, and which would expand in some directions and contract in
 493 others, with the directions of expansion and contraction changing repeatedly, what suggested that the
 494 evolution was in fact chaotic.

495 4.1.2. The classical Singularity Theorems

496 We will here summarize in a unified fashion just two of the main singularity theorems that
 497 appeared starting in the mid 1960's for Einstein's field equations without further specific assumptions,
 498 as homogeneity or isotropy. The starting point here was the pioneering Penrose singularity theorem
 499 [41] of 1965 (for a few more references, see [42]). Roger Penrose closed in fact the loophole discussed
 500 above by showing that, under very general assumptions, the singularity is unavoidable. Penrose proof
 501 relies on the concept of incomplete geodesics.

502 **Theorem 1. (Big Bang).** *Let (M, g) be a global hyperbolic spacetime satisfying $R_{ab}X^aX^b \geq 0$ (being R_{ab} the*
 503 *curvature tensor) for all temporal vectors X^a (Einstein's Eqs. with the strong energy condition.) If there exists a*
 504 *spatial Cauchy C^2 hypersurface, S , for which the trace of the intrinsic curvature κ satisfies $\kappa < k < 0$, with k*
 505 *const., then no temporal curve starting from S and going towards the past can have a length that is larger than*
 506 *$3/|k|$.*

507 All temporal geodesics to the past are incomplete.

508 This is to say, under the conditions observed to be true for our Universe (Hubble's law) and
 509 admitting the validity of General Relativity, our Universe did have a beginning, in a singularity, which
 510 everybody now calls *the Big Bang singularity*.

511 **Theorem 2. (Black Holes).** *Let (M, g) be a global hyperbolic space-time satisfying $R_{ab}L^aL^b = 0$ (being R_{ab}*
 512 *the curvature tensor) for all lightlike vectors L^a (Einstein's Eqs. with the strong or the weak energy conditions.)*
 513 *Assume that there is a spatial Cauchy C^2 hypersurface, S , and a trapped surface, and let τ_0 be the maximum*
 514 *value of the expansion over it. If $\tau_0 < 0$, there exists at least a lightlike geodesic that cannot be extended to the*
 515 *future, and is orthogonal to the trapped surface. Moreover, the value of the affine parameter, up to the point of no*
 516 *further extension of the geodesic, is less than $2/|\tau_0|$.*

517 In other words, the existence of a non-extensible lightlike geodesic implies that there will be
 518 a lightlike observer (e.g. a photon), which, starting from that surface and after a time of travel
 519 proportional to $2/c|\tau_0|$, will necessarily fall into a future time singularity.

520 In any case, since we do not have a theory of quantum gravity we cannot know with certainty the
 521 physical nature of this singularity.

522 The following important consideration is here in order. It turns out that, before one ever reaches
 523 the singularity at the origin of everything, classical physics, as described by Einstein's field equations,
 524 ceases to be valid. Actually, we need not go so far back in time in order to experience this: try to
 525 describe the Hydrogen atom with GR, this has simply no sense. Thus, in a way, the classical singularity
 526 theorems, although mathematically rigorous, lack physical meaning.

527 Those were the reasons of the Moscow Russian school again, now however around Yakov
 528 Zel'dovich (Starobinsky, Mukhanov, Chibishov, ...) at the end of the 1970s, for invoking the inescapable
 529 necessity of quantum corrections to the gravity equations –a limited possibility but the only one
 530 available, given that a rigorous theory of quantum gravity was, and is still, lacking. It was during a
 531 visit of Hawking to Moscow in the early 1970s where he got the idea of adding quantum corrections to
 532 black hole physics, what resulted in his extremely important discovery of the Hawking radiation, as
 533 Hawking himself has recognized several times.

534 4.1.3. On the BGV (Borde-Guth-Vilenkin) Theorem

535 Inflationary cosmological models seemed bound to invalidate the conditions of all the classical
 536 singularity theorems above [38,43]. In the 1980's, it was attempted (without success, in fact) to construct
 537 models that, starting from an exact de Sitter solutions would be past eternal. In 1994 Borde and Vilenkin
 538 (BV94) proved an extended theorem [44], which states that inflationary spacetimes are past geodesically
 539 incomplete, what again implies, in other words, an initial singularity. The key assumption for this
 540 theorem was that the energy-momentum tensor obeys the weak energy condition (WEC), what was an
 541 advance over the previous theorems.

542 However, quantum corrections to inflationary models seem to violate such condition, too, when
 543 quantum fluctuations result in an increase of the Hubble parameter: $dH/dt > 0$, which, on the other
 544 hand, is an essential condition for chaotic inflation to be eternal. Thus, the WEC must be generically
 545 violated in those models! And this seemed to open the door to a scape from the BV theorem.

546 Such was the motivation for Borde, Guth & Vilenkin in his celebrated paper [45] "*Inflationary
 547 Spacetimes Are Incomplete in Past Directions*". As the title already indicates, they recovered again
 548 the result of BV94, but with a few important additional considerations, which have not been fully
 549 appreciated by some unconditional supporters of the creationists theories. I will not further discuss
 550 this issue here [46].

Technically, one starts now from the (sufficient) condition of a "quasi dS" state with a minimal
 condition of "averaged expansion" (along t -paths):

$$H_a v > 0,$$

551 that is, an average taken over all time trajectories.

552 Moreover, the theorem can be extended to extra dimensions, and also to cyclic models [47], for
 553 $H_a v > 0$ in those models.

554 As a consequence, in all these cases, and under the strict conditions of the theorem, one gets initial
 555 geodesic incompleteness! That is, an origin, once again [45].

556 4.2. A quick sketch of the possible origin of the Universe

557 A rather extended view today is that the origin of the Universe took place out of nothing –or
 558 almost nothing. Let us be more precise.

559 The first question that occurs to us is: What is *nothing*? The answer of modern physics is (at the
 560 very least) twofold, namely

- 561 1. In fundamental classical physics the ultimate theory is GR, and there the vacuum solution is the
 562 de Sitter solution (the zero-energy one) of Einstein's field equations.
- 563 2. In quantum physics, on the other hand 'nothing' means the vacuum state of the quantum system
 564 at hand, e.g., in our case the one at the very beginning of all, as far as we can go into the past.
- 565 3. It needs little explanation that we are missing here the actual theory that we would need in order
 566 to answer the question with more property, namely the theory of quantum gravity (QG).
- 567 4. However, it is not clear at all that, even in possession of QG, we would be allowed to penetrate
 568 the Planck domain, which establishes a limit to all known theories of Physics (quite probably
 569 also to this unknown QG).

570 And this is the state of the art of such fundamental issue today. Letting aside the Planckian constraint
 571 and ensuing considerations, some possibilities have been recently proposed with essentially two
 572 different, so to say, minimalist starting points:

- 573 1. Just quantum spacetime, and nothing else! In spite of some attempts to do that (as most recently
 574 by Lawrence Krauss and Frank Wilczek) nobody has convincingly succeeded yet.
- 575 2. In addition, a scalar field Hamiltonian (or two), namely the Higgs, an inflaton,... This seems of
 576 course a more feasible possibility, at the expense of having to explain where do these additional
 577 necessary fields come from.

578 4.3. Big Bang Cosmological Models

579 Just a rather brief mention, accompanied with a number of basic references, of this vast subject,
580 which was at the heart of the most fundamental discussions about cosmology for some generation
581 of physicists, namely hot or cold Big Bang model? clearly decided in favor of the first. A question
582 that had an even more important second part, under the form of hot or cold dark matter? eventually
583 decided in favor of the second.

584 4.3.1. The Hot Big Bang Model

585 Skipping now the details of the Big Bang and previous to the formulation of inflation, with its
586 many specific theories, what remained true of the original idea of Lemaître was that, in fact, in the past
587 the Universe was in a very dense state and very hot, so that matter could relax to statistical thermal
588 equilibrium. Black body radiation was filling the whole space. With the expansion of the Universe
589 the temperature went down until the first (neutral) atoms could form, namely Hydrogen ones, and
590 radiation could travel across the whole Universe under the form of what is now called the CMB or
591 cosmic microwave radiation (formerly also called CRB, cosmic background radiation). Some useful
592 references where this process is described in detail are [48]-[57].

593 In the beautiful description of Lemaître, the ulterior processes which took place can be compared
594 with fireworks:

595 *"The evolution of the world can be compared to a display of fireworks that has just ended; some*
596 *few red wisps, ashes and smoke. Standing on a cooled cinder, we see the slow fading of the suns, and*
597 *we try to recall the vanishing brilliance of the origin of the worlds."*

598 In the time interval from about two to thirty minutes, but mostly within the first three minutes
599 after the Big Bang (see [58] for a very popular reference), an efficient synthesis of the light elements,
600 namely Deuterium, Helium-3, and Helium-4 took place. This is what is called the era of primordial
601 nucleosynthesis. The current abundances of light elements are in accordance with what happened
602 during that time, placing strong constraints on the state of the Universe then, and particularly on the
603 baryon density. Our Universe contains now some 23% of its mass in Helium (its production in stars is
604 not relevant, as compared to the primordial production during the first three minutes). The conditions
605 then had to be precisely those leading to our Universe, which has nine Hydrogen nuclei for every
606 Helium nucleus [52]. Moreover, it is well known now that most of the Universe's Hydrogen is in its
607 simplest form and not in heavier isotopes, namely deuterium or tritium. Deuterium, on its turn, is not
608 produced, but only destroyed, in stars, so that its abundance today sets a lower limit on the amount of
609 deuterium from primordial nucleosynthesis, and again on the density of baryons, too.

610 The Hot Big Bang model does explain what we see in our Universe. To summarize further
611 evidence, we know list what have been called sometimes the four pillars of the standard Hot Big Bang
612 model: [51]

- 613 1. The Universe expansion.
- 614 2. The origin of the CMB.
- 615 3. The primordial nucleosynthesis of the light elements.
- 616 4. The formation of the galaxies and of large-scale structures.

617 After some six decades of dealing with this model with considerable success, a crisis took place
618 at the beginning of the 1990s [59], just anticipating the discovery of the acceleration of the Universe
619 expansion, which completely changed the paradigm [60] and, in particular, the energy content of
620 the Universe. Some important consequences of this discovery, in special concerning the possible
621 appearance of finite time future singularities, will be discussed in the next Section.

622 4.3.2. The Cold Big Bang and other models

623 The idea of a possible Cold Big Bang goes back to Lemaître's theory of a primeval atom, forming
624 a gigantic ball of nuclear liquid in a state at very low temperature, which was required in order to keep
625 it from falling apart via thermal fluctuations [61]. In Lemaître's words:

626 *"If matter existed as a single atomic nucleus, it makes no sense to speak of space and time in*
627 *connection with this atom. Space and time are statistical notions that apply to an assembly of a*
628 *great number of individual elements; they were meaningless notions, therefore, at the instant of first*
629 *disintegration of the primeval atom."*

630 Ultimately, this idea was not able to explain the Universe expansion and the origin of the light elements.

631 A variant on Lemaître's cosmology was proposed in 1966 by David Layzer [62], who developed a
632 short-lived alternate to the standard Hot Big Bang cosmology by proposing that the initial state was
633 near absolute zero, thus reminiscent of Lemaître's initial state. Through thermodynamic arguments,
634 Layzer argued that rather than the universe starting in a high entropy state, it began with a very low
635 entropy (see also [63]). Anyhow, the CMB radiation is very difficult to explain in these theories, in spite
636 of some more recent attempts [64]. To finish, most of the versions of a Cold Big Bang being considered
637 predicted an absence of acoustic peaks in the cosmic microwave background radiation, a possibility
638 that was eventually ruled out quite clearly by WMAP, and most recently PLANCK, observations.

639 For completeness, some other theories, which are in a way alternative to the Hot Big Bang model,
640 can be found here [65]-[68].

641 5. Acceleration: new singularities

642 According to the most recent and accurate astronomical observations, it is very likely that our
643 universe had an origin, some 13.8 billion years ago, from nothing (or almost nothing, a quasi de Sitter
644 space) –e.g., from a vacuum state of a tiny quantum system including space-time and possibly a scalar
645 field– and is currently in accelerated expansion. In many of the models of modified gravity, which
646 have been discussed in order to obtain this accelerated expansion new singularities, in a way similar
647 to the Big Bang one, have shown up.

Recall the second Friedmann equation

$$648 \frac{\ddot{a}}{a} = -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right) + \frac{\Lambda c^2}{3}, \quad (1)$$

649 where a is the scale factor, while ρ is the matter/energy density, p the pressure, and Λ the cosmological
650 constant.

651 For a fluid with equation of state $P = w\rho$, where w is the so-called equation of state parameter,
652 the following three possibilities appear, according to the different values this fundamental parameter w
653 may have, and which we already know, from the most recent and accurate astronomical observations,
654 to be $w \sim -1$. Namely,

- 654 • $w = -1$, **the cosmological constant case**. The simplest and most natural in general relativity,
655 but difficult to explain, and it seems to need for a symmetry no one has been able to find yet, in a
656 convincing way, in order to solve the associated cosmological constant problem.
- 657 • $w > -1$, **so-called quintessence case**. It is the most ordinary case and usually involves an
658 evolving scalar field.
- 659 • $w < -1$, **the phantom case**. It involves a so-called phantom field (of negative kinetic energy)
660 and leads to a number of future singularities at finite (or infinite) time.

661 If the universe is now, indeed, in the Λ CDM era (that is, cold dark matter with a cosmological
662 constant Λ), it might remain in such era, eventually becoming asymptotically de Sitter, i.e., a regular
663 universe during all its future evolution. This would be the most simple and natural situation, were it
664 not for the annoying cosmological constant problem.

665 For a phantom or quintessence dark energy era, other singularities appear (for a few seminal
666 references, see [69–73]). According to Ref. [74], they can be most conveniently classified as follows.

- 667 • **The Big Rip or Type I** singularity (occurring in a phantom dominated universe) [75]. In the limit
668 $t = t_s$ (a finite value of time in the future) all quantities, namely the scale factor, effective energy
669 density and pressure of the universe diverge.
- 670 • **Sudden Singularity, or Type II**, discovered in [71]. In the limit $t = t_s$ only the effective pressure
671 of the universe becomes infinite, while the scale factor a and the total effective energy density ρ
672 remain finite.
- 673 • **Type III or Big Freeze** future singularity. In this case, only the scale factor remains finite, while
674 both the effective energy density and pressure of the universe diverge at $t = t_s$. These can be
675 either weak or strong singularities, which are geodesically complete solutions.
- 676 • **Type IV or Generalized Sudden** singularity. In the limit $t = t_s$ none of these, the scale factor,
677 effective energy density or pressure diverge. However, higher derivatives of the Hubble rate
678 H become divergent (not H itself and its first derivative), as discovered in [74], where a full
679 classification was given. In this case a weak singularity appears and geodesics are complete.

680 Eventually, the universe may survive the passage through a Type IV singularity or a Sudden Singularity
681 (Type II).

682 And there is still the case of the so-called **Little Rip** universes, where the future singularities occur
683 asymptotically, at infinite time only. Typically, this happens when the scale factor increases rapidly, as
684 $a(t) = \exp[\exp(t)]$ or higher exponentials [76,77]. But different combinations are also possible, as an
685 oscillating universe (bounce). Also, the very important point must be remarked that quantum gravity
686 effects may affect this future evolution, preventing a Big Rip to occur by such quantum effects [78] or
687 by a similar Casimir-type effect or other (see, e.g., [80]).

688 Increasing effort is being devoted towards the classification of singularities in all sort of
689 cosmological models. In particular, there is an ongoing intensive study of cosmic singularities for very
690 different modified gravity theories.

691 6. Conclusions

692 As explained in the first section of this paper, there are powerful reasons to consider 1912 as the
693 Year that marks the beginning of modern cosmology. The author is now fully convinced that it should
694 be officially declared as such. Indeed, two extraordinary, almost simultaneous developments occurred
695 that Year, to wit: (i) the publication by Henrietta S. Leavitt of her crucial law, the period-luminosity
696 relationship of Cepheid variable stars, namely a linear dependence of the luminosity vs the logarithm
697 of the period of variability, and (ii) the beginning of Vesto Slipher's investigation of the velocities of
698 spiral nebulae, obtained by means of their corresponding spectral deviations, as red- (or blue-) shifts.
699 These two extremely powerful tools allowed, in the few following years, the formulation of Hubble's
700 law and its matching (by Georges Lemaître) with the expanding solution of the Einstein field equations,
701 a solution that actually had been first obtained by Alexander Friedmann, a couple of years before. The
702 Universe was expanding, indeed! It took some time, even to astronomers and theoretical cosmologists
703 (in Einstein's case four full years) to understand this very difficult concept. In many cases it took even
704 decades, what proves that this is far from being an easy notion, as we have discussed in the paper in
705 detail.

706 The fine tools put in place by Leavitt and Slipher, in 1912, were used by Hubble and many other
707 astronomers subsequently –as were the Einstein field equations, from 1915, by Friedmann, de Sitter,
708 Lemaître and so on– to craft the extraordinary structure, still under construction, of Modern Cosmology.
709 Therefore the proposal of the Year 1912 as the one marking the birth of Modern Cosmology.

710 The second part has been devoted basically to the history of the original meaning of the Big Bang
711 concept, a definition that is too badly explained in the available generalistic literature. Fred Hoyle
712 had a very clear idea in mind when he said these two words for the first time. Indeed, the complete

713 sentence he pronounced on that occasion is perfectly understandable and absolutely meaningful to
 714 anyone who is versed in General Relativity, but not so at all to non-specialists, and this is maybe the
 715 main reason for the unbelievable confusion generated around this term. Another one being that the
 716 same two words, namely 'Big Bang', have been subsequently used in a number of different situations,
 717 most notably to give name to cosmological models, e.g. the hot and the cold Big Bang models, and
 718 to the Big Bang singularity at the very origin of space and time. In this paper I have defended the
 719 thesis that all this new terminology has practically buried the original concept, which we have had
 720 here to rescue from its ashes, with the help of recent important discoveries from historians of science.
 721 Needless to say, all the above is quite well known to professional cosmologists and astrophysicists
 722 with a solid background, but not so, regretfully, to many other scientists and intellectuals, in general.

723 As a final conclusion, owing to the fact that these two magic words, Big Bang, have become
 724 so extremely popular in many different contexts and mass media channels (even little children use
 725 them sometimes), all of us, scientists who know about this matter, must consider as our inescapable
 726 duty a serious compromise to explain the precise meaning of Big Bang in a fair, understandable, but
 727 non-misleading way, not only to students, at our universities, institutes, and schools, but also to the
 728 general public, anywhere and at any opportunity.

729 **Acknowledgments:** This work was partially supported by CSIC, I-LINK1019 Project, by MINECO (Spain),
 730 Projects FIS2013-44881-P and FIS2016-76363-P, by the CPAN Consolider Ingenio Project, and by JSPS (Japan),
 731 Fellowship N. S17017. This research was started while the author was visiting the Kobayashi-Maskawa Institute
 732 in Nagoya, Japan. He is much obliged with S. Nojiri and the rest of the members of the KMI for very warm
 733 hospitality. The paper was finished during a research stay at Dartmouth College, NH, USA. The author thanks the
 734 referees of this paper for very interesting remarks.

735 References

- 736 1. Albert Einstein, *Die Feldgleichungen der Gravitation*, Sitzungsberichte der Preussischen Akademie der
 737 Wissenschaften zu Berlin (25-11-1915), 844-847;
 738 <http://nausikaa2.mpiwg-berlin.mpg.de/cgi-bin/toc/toc.x.cgi?dir=6E3MAXK4&step=thumb>.
- 739 2. Carlo Rovelli, *The First Scientist, Anaximander and his Legacy* (Yardley, Westholme, 2011); James Luchte, *Early*
 740 *Greek Thought: Before the Dawn* (Bloomsbury Publishing, London, 2011); Nikolaus Steenken, *Anaximander, der*
 741 *erste Kosmologe*, Spektrum der Wissenschaft 10.01.2014.
- 742 3. Edward R. Harrison, *Darkness at Night: A Riddle of the Universe* (Harvard University Press, 1987).
- 743 4. Conversation of Gamow with Einstein in the 1940s. George Gamow, *My World Line: An Informal Autobiography*
 744 (Viking Press, 1970).
- 745 5. Henrietta S. Leavitt, Edward C. Pickering, *Periods of 25 Variable Stars in the Small Magellanic Cloud* Harvard
 746 College Observatory Circular, vol. 173, pp.1-3 (1912); Leavitt, Henrietta S. *1777 Variables in the Magellanic*
 747 *Clouds*, Annals of Harvard College Observatory. LX(IV) (1908) 87-110; 1912: *Henrietta Leavitt Discovers the*
 748 *Distance Key*,
 749 <https://web.archive.org/web/20140604195000/http://cosmology.carnegiescience.edu/timeline/1912>.
- 750 6. <http://www.kcvs.ca/martin/astro/course/lectures/winter/var.htm>
- 751 7. Nina Byers and Gary Williams, *Out of the Shadows: Contributions of Twentieth-century Women to Physics*
 752 (Cambridge University Press, 2006); Johnson, George, *Miss Leavitt's Stars: The Untold Story of the Woman Who*
 753 *Discovered How To Measure the Universe*, 1st Ed. (Norton, New York, 2005); Gregory M. Lamb, *Before computers,*
 754 *there were these humans* Christian Science Monitor (July 5, 2005); Peggy Aldrich Kidwell, *Leavitt, Henrietta*
 755 *Swan*, American National Biography Online (Oxford University Press, 2000).
- 756 8. Michael Rowan-Robinson, *The Cosmological Distance Ladder: Distance and Time in the Universe*, First Edition
 757 (W.H. Freeman & Co, 1985).
- 758 9. https://ned.ipac.caltech.edu/level5/March03/Perlmutter/Perl2_2.html
- 759 10. Vesto Slipher, *The radial velocity of the Andromeda Nebula*, Lowell Observatory Bulletin, pp.2.56-2.57 (1912).
- 760 11. Vesto Slipher, *Spectrographic Observations of Nebulae*, Popular Astronomy, Vol. 23, p. 21-24 (1915).
- 761 12. H. Shapley and H.D. Curtis, *The scale of the universe*, Bulletin of the National Research Council 2 (Part 3,
 762 Issue 11): 171-217 (1921); J.R. Gott III, et al., *A Map of the Universe*, Ap. J. 624, 463-484 (2005); F. Shu, *The*

- 763 *Physical Universe, An Introduction to Astronomy* (University Science Books, Mill Valley, California, 1982) p.
764 286; http://apod.nasa.gov/diamond_jubilee/debate.html.
- 765 13. Marcia Bartusiak, *The Day We Found the Universe* (Random House Digital, 2010); V. Trimble, *The 1920*
766 *Shapley-Curtis Discussion: Background, Issues, and Aftermath*, Publications of the Astronomical Society of the
767 Pacific. 107: 1133 (1995).
- 768 14. Dennis Overbye, *Lonely Hearts of the Cosmos: The Scientific Quest for the Secrets of the Universe* (Back Pay Books,
769 1986).
- 770 15. <http://obs.carnegiescience.edu/PAST/m31var>
- 771 16. Ernst Öpik, *An estimate of the distance of the Andromeda Nebula*, Ap. J. 55, 406 (1922) [Erratum: Ap. J. 57, 192
772 (1923)].
- 773 17. Vesto Slipher, *Nebulae*, Proceedings of the American Philosophical Society, 56, 403 (1917).
- 774 18. A.S. Eddington, *The Mathematical Theory of Relativity* (Cambridge Univ. Press, 1923).
- 775 19. E. Hubble, Pop. Astr. 33, 252-255 (1925).
- 776 20. E. Hubble, Proc. Natl Acad. Sci. USA 15, 168-173 (1929).
- 777 21. Biographical Memoirs, Vol 52, National Academy of Sciences (U.S.).
- 778 22. E.P. Hubble, *The realm of the nebulae*, Biographical Memoirs, Vol 52, National Academy of Sciences (U.S.)
779 (Dover Pub. Inc. 1958).
- 780 23. Sten Odenwald and Rick Fienberg, *Redshifts Reconsidered* (Sky Pub Co, 1993).
- 781 24. Harry Nussbaumer, Eur Phys J H39, 37-62 (2014).
- 782 25. Stephen M. Stigler, in F. Gieryn, ed. *Stigler's law of eponymy*, Transactions of the New York Academy of
783 Sciences 39, 147-58 (1980). (Festschrift for Robert K. Merton)
- 784 26. G. Lemaître, *Un Univers homogène de masse constante et de rayon croissant rendant compte de la vitesse radiale des*
785 *nébuleuses extragalactiques* ("A homogeneous Universe of constant mass and growing radius accounting for
786 the radial velocity of extragalactic nebulae"), Annales de la Société Scientifique de Bruxelles 47, 49 (1927) (in
787 French).
- 788 27. Mario Livio, *Lost in translation: Mystery of the missing text solved*, Nature 479, 171-173 (2011).
- 789 28. A.S. Eddington, *On the instability of Einstein's spherical world*, Monthly Notices of the Royal Astronomical
790 Society 90, 668-688 (1930).
- 791 29. G. Lemaître, *Expansion of the universe, The expanding universe*, Monthly Notices of the Royal Astronomical
792 Society 91, 490-501 (1931).
- 793 30. G. Lemaître, *The Beginning of the World from the Point of View of Quantum Theory*, Nature 127, 706 (1931);
794 doi:10.1038/127706b0.
- 795 31. T. Dunham Jr. and W.S. Adams, Pub. Astron. Soc. Pac. 49, 26 (1937); T. Dunham Jr. and W.S. Adams, Pub.
796 Am. Astron. Soc. 9, 5 (1937); H.A. Bethe and C.L. Critchfield, *The Formation of Deuterons by Proton Combination*,
797 Physical Review 54, 248 (1938), doi:10.1103/PhysRev.54.248; C.F. von Weizsäcker, *Über Elementumwandlungen*
798 *in Innern der Sterne II*, Physikalische Zeitschrift 39, 633 (1938); H.A. Bethe, *Energy Production in Stars*, Physical
799 Review 55, 434 (1939), doi:10.1103/PhysRev.55.434.
- 800 32. G. Gamow, *The Origin of Elements and the Separation of Galaxies*, Physical Review 74, 505 (1948); G. Gamow,
801 *The evolution of the universe*, Nature 162, 680 (1948); R.A. Alpher and R. Herman, *On the Relative Abundance of*
802 *the Elements*, Physical Review 74, 1577 (1948); G. Gamow, *One, Two, Three...Infinity* (Viking Press, 1947, revised
803 1961; Dover P. 1974); R.A. Alpher and R.C. Herman, *Evolution of the Universe*, Nature 162, 774 (1948); R.A.
804 Alpher, R.C. Herman, and G. Gamow, Phys. Rev. 74, 1198 (1948); R.A. Alpher and R.C. Herman, *Remarks on*
805 *the Evolution of the Expanding Universe*, Phys. Rev. 75, 1089 (1949).
- 806 33. F. Hoyle, *The Synthesis of the Elements from Hydrogen*, Monthly Notices of the Royal Astronomical Society
807 106, 343 (1946), doi:10.1093/mnras/106.5.343; F. Hoyle, *On Nuclear Reactions Occurring in Very Hot*
808 *Stars. I. The Synthesis of Elements from Carbon to Nickel*, Astrophysical Journal Supplement 1, 121 (1954),
809 doi:10.1086/190005; E.M. Burbidge, G.R. Burbidge, W.A. Fowler, and F. Hoyle, *Synthesis of the Elements in*
810 *Stars*, Reviews of Modern Physics 29, 547 (1957), doi:10.1103/RevModPhys.29.547.
- 811 34. Richard C. Tolman, *Relativity, Thermodynamics, and Cosmology* (Oxford University Press, Oxford, 1934).
- 812 35. Personal recollection.
- 813 36. Robert W. Wilson, *The Cosmic Microwave Background Radiation*, Nobel Lecture, 8-12-1978;
814 http://nobelprize.org/nobel_prizes/physics/laureates/1978/wilson-lecture.pdf; R.H. Dicke, P.J.E. Peebles,
815 P.G. Roll, and D.T. Wilkinson, Ap. J. 142, 14 (1965); A.A. Penzias, and R.W. Wilson, Ap. J. 142, 420 (1965).

- 816 37. John Gribbin, *Stardust memories*, The Independent, Friday 17 June, 2005.
- 817 38. Alan H. Guth, *Inflationary universe: A possible solution to the horizon and flatness problems*, Phys. Rev. D23, 347
818 (1981).
- 819 39. E.M. Lifshitz and I.M. Khalatnikov, Usp. Fiz. Nauk 80, 391 (1963) [Sov. Phys. Usp. 6, 495 (1964)]; E.M.
820 Lifshitz and I.M. Khalatnikov, Adv. Phys. 12, 185 (1963); I.M. Khalatnikov and E.M. Lifshitz, Phys. Rev. Lett.
821 24, 76 (1970); V.A. Belinsky, E.M. Lifshitz and I.M. Khalatnikov, Usp. Fiz. Nauk 102, 463 (1970) [Sov. Phys.
822 Usp. 13, 745 (1971)].
- 823 40. C.W. Misner, *Mixmaster Universe*, Phys. Rev. Lett 22, 1071 (1969).
- 824 41. Roger Penrose, *Gravitational collapse and space-time singularities*, Phys. Rev. Lett. 14, 57 (1965).
- 825 42. S. Hawking and G.F.R. Ellis, *The Large Scale Structure of Space-Time* (Cambridge U. P., 1973); R.M. Wald,
826 *General Relativity* (U. Chicago P., 1984); R. Geroch, Ann. Phys. 48, 526 (1968); D. Garfinkle and
827 J.M.M. Senovilla, *The 1965 Penrose singularity theorem*, Class. Quant. Grav., 32 (12): 124008 (2015);
828 <http://www.hawking.org.uk/the-beginning-of-time.html>
- 829 43. K. Sato, *Cosmological baryon number domain structure and the first order phase transition of a vacuum*, Phys. Lett.
830 B33, 66-70 (1981); A. Albrecht and P.J. Steinhardt, *Cosmology For Grand Unified Theories With Radiatively Induced*
831 *Symmetry Breaking*, Phys. Rev. Lett. 48, 1220-1223 (1982); A.D. Linde, *Eternally Existing Self-Reproducing*
832 *Chaotic Inflationary Universe*, Physics Letters B175, 395-400 (1986); V.F. Mukhanov, and G.V. Chibisov *Quantum*
833 *fluctuation and "nonsingular" universe*, JETP Letters 33, 532-5 (1981); A.A. Starobinsky, *Spectrum of Relict*
834 *Gravitational Radiation and The Early State of the Universe*, JETP Lett. 30, 682 (1979); Alexander Vilenkin, *Birth*
835 *of Inflationary Universes*, Physical Review D27, 2848-2855 (1983).
- 836 44. A. Borde and A. Vilenkin, *Eternal Inflation and the Initial Singularity*, Phys. Rev. Lett. 72, 3305 (1993).
- 837 45. A. Borde, A. Guth, and A. Vilenkin, *Inflationary Spacetimes Are Incomplete in Past Directions*, Phys. Rev. Lett.
838 90, 151301 (2003).
- 839 46. [https://physics.stackexchange.com/questions/308325/correct-interpretation-of-the-borde-guth-vilenkin-](https://physics.stackexchange.com/questions/308325/correct-interpretation-of-the-borde-guth-vilenkin-bgv-theorem)
840 [http://www.preposterousuniverse.com/blog/2012/09/25/let-the-universe-be-the-universe/;](http://www.preposterousuniverse.com/blog/2012/09/25/let-the-universe-be-the-universe/)
841 [http://inference-review.com/article/the-beginning-of-the-universe;](http://inference-review.com/article/the-beginning-of-the-universe) [http://creationwiki.org/Borde-Guth-](http://creationwiki.org/Borde-Guth-Vilenkin_singularity_theorem)
842 [https://debunkingwlc.wordpress.com/2010/07/14/borde-guth-vilenkin/;](https://debunkingwlc.wordpress.com/2010/07/14/borde-guth-vilenkin/)
843 [https://evolutionnews.org/2014/08/the_borde-guth/;](https://evolutionnews.org/2014/08/the_borde-guth/) [http://www.wall.org/~aron/blog/did-the-universe-](http://www.wall.org/~aron/blog/did-the-universe-begin-iii-bgv-theorem/)
844 [begin-iii-bgv-theorem/](http://www.wall.org/~aron/blog/did-the-universe-begin-iii-bgv-theorem/).
- 845 47. Paul J. Steinhardt and Neil Turok, *A Cyclic Model of the Universe*, Science 296, 1436-1439 (2002).
- 846 48. G. Calcagni, *Classical and Quantum Cosmology*, Graduate Texts in Physics (Springer International Publishing,
847 Switzerland, 2017), Chap. 2.
- 848 49. Dragan Huterer, *Big Bang Theory: The Three Pillars*, University of Michigan,
849 http://www-personal.umich.edu/huterer/EPO/HOUSTON_2012/three_pillars_houston.pdf
- 850 50. John Ellis, J.S. Hagelin, D.V. Nanopoulos, K. Olive, and M. Srednicki, *Supersymmetric relics from the big*
851 *bang*, Nuclear Physics B238, 453-476 (1984); M. Gasperini and G. Veneziano, *Pre-big-bang in string cosmology*,
852 *Astroparticle Physics* 1, 317-339 (1993).
- 853 51. http://www.damtp.cam.ac.uk/research/gr/public/bb_home.html
- 854 52. <http://www.astro.cornell.edu/academics/courses/astro201>
- 855 53. <https://faraday.physics.utoronto.ca/PVB/Harrison/GenRel/BigBangModel.html>
- 856 54. <https://www.ras.org.uk/publications/other-publications/2040-cosmology-big-bang>
- 857 55. https://map.gsfc.nasa.gov/universe/bb_theory.html
- 858 56. astronomy.swin.edu.au/gmackie/BigBang/universe.htm
- 859 57. <http://spiff.rit.edu/classes/phys240/lectures/bb/bb.html>
- 860 58. Steven Weinberg, *The First Three Minutes: A modern view of the origin of the universe* (Basic Books, 2nd Ed. 1993;
861 1st Ed. 1977).
- 862 59. P.J.E. Peebles, D.N. Schramm, E.L. Turner, and R.G. Kron, *The case for the relativistic hot Big Bang cosmology*,
863 *Nature* 352, 769-776 (1991).
- 864 60. Justin Khoury, Burt A. Ovrut, Nathan Seiberg, Paul J. Steinhardt, and Neil Turok, *Ekpyrotic universe: Colliding*
865 *branes and the origin of the hot big bang*, Phys. Rev. D64, 123522 (2001); Justin Khoury, Burt A. Ovrut, Nathan
866 Seiberg, Paul J. Steinhardt, and Neil Turok, *From big crunch to big bang*, Phys. Rev. D65, 086007 (2002).
- 867 61. <https://web.archive.org/web/20110610170334/http://www.cosmosportal.org/articles/view/138894/>
- 868 62. http://www.informationphilosopher.com/solutions/scientists/layzer/growth_of_order/

- 869 63. Julian Barbour, Tim Koslowski, and Flavio Mercati, *Identification of a Gravitational Arrow of Time*, Phys. Rev.
870 Lett. 113, 181101 (2014).
- 871 64. A.N. Aguirre, *The Cosmic Background Radiation in a Cold Big Bang*, Ap. J. 533 (2000) 1; Phys. Rev. D64 (2001)
872 083508.
- 873 65. C. Wetterich, *Hot big bang or slow freeze?*, Physics Letters B736, 506-514 (2014), arXiv:1401.5313 [astro-ph.CO],
874 DOI: 10.1016/j.physletb.2014.08.013.
- 875 66. Abhay Ashtekar, Tomasz Pawlowski, and Parampreet Singh, *Quantum nature of the big bang: Improved*
876 *dynamics*, Phys. Rev. D74, 084003 (2006).
- 877 67. George L. Murphy, *Big-Bang Model Without Singularities*, Phys. Rev. D8, 4231 (1973).
- 878 68. <http://www.pbs.org/wgbh/nova/blogs/physics/2014/08/when-the-end-is-just-the-beginning-exploring-cosmic-cycles/>
- 879 69. R. R. Caldwell, Phys. Lett. B **545** (2002) 23 doi:10.1016/S0370-2693(02)02589-3 [astro-ph/9908168].
- 880 70. R. R. Caldwell, M. Kamionkowski and N. N. Weinberg, Phys. Rev. Lett. **91** (2003) 071301
881 doi:10.1103/PhysRevLett.91.071301 [astro-ph/0302506].
- 882 71. J. D. Barrow, Class. Quant. Grav. **21** (2004) L79 doi:10.1088/0264-9381/21/11/L03 [gr-qc/0403084].
- 883 72. J. D. Barrow, Class. Quant. Grav. **21** (2004) 5619 doi:10.1088/0264-9381/21/23/020 [gr-qc/0409062].
- 884 73. M. Bouhmadi-Lopez, P. F. Gonzalez-Diaz and P. Martin-Moruno, Phys. Lett. B **659** (2008) 1
885 doi:10.1016/j.physletb.2007.10.079 [gr-qc/0612135].
- 886 74. S. Nojiri, S. D. Odintsov and S. Tsujikawa, Phys. Rev. D **71** (2005) 063004 doi:10.1103/PhysRevD.71.063004
887 [hep-th/0501025].
- 888 75. R.R. Caldwell, Phys. Lett. B545 (2002) 23.
- 889 76. P.H. Frampton, K.J. Ludwick and R.J. Scherrer, Phys. Rev. D84 (2011) 063003.
- 890 77. I. Brevik, E. Elizalde, S. Nojiri, S.D. Odintsov, Phys. Rev. D84 (2011) 103508.
- 891 78. E. Elizalde, S. Nojiri and S. D. Odintsov, *"Late-time cosmology in (phantom) scalar-tensor theory: Dark energy and*
892 *the cosmic speed-up"*, Phys. Rev. **D70** (2004) 043539 [hep-th/0405034].
- 893 79. E. Elizalde, S. Nojiri, S. D. Odintsov and D. Saez-Gomez, Eur. Phys. J. C **70** (2010) 351
894 doi:10.1140/epjc/s10052-010-1455-7 [arXiv:1006.3387 [hep-th]].
- 895 80. E. Elizalde, R. Myrzakulov, V. V. Obukhov and D. Saez-Gomez, Class. Quant. Grav. **27** (2010) 095007
896 [arXiv:1001.3636 [gr-qc]]; G. Cognola, E. Elizalde, S. Nojiri, S. D. Odintsov, L. Sebastiani and S. Zerbini, Phys.
897 Rev. D **77** (2008) 046009 [arXiv:0712.4017 [hep-th]]; F. Briscese, E. Elizalde, S. Nojiri and S. D. Odintsov, Phys.
898 Lett. B **646** (2007) 105 [hep-th/0612220].