

Article

# PAVEMENT DAMAGE CRACK RECOGNITION METHOD BASED ON HIGH-RESOLUTION LINEAR ARRAY CAMERAS AND ADAPTIVE LIFTING ALGORITHM

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**Abstract:** This paper proposes a crack recognition method based on high-resolution line array cameras and adaptive lifting algorithm. By defining the crack rate, this algorithm calculates the ratio of the crack area to the area of the entire collected image to characterize the damage extent of the current section. The algorithm first uses image preprocessing to reduce the image noise, then uses histogram equalization to enhance the feature of the crack region, divides the whole image into multiple sub-blocks, and extracts region features in the sub-block. At the same time, this algorithm defines related feature descriptors, and constructs weak classifiers according to each feature descriptor, and converts the weak classifiers into strong classifiers by using an adaptive lifting algorithm. Finally, this algorithm realizes the division of the crack regions. Experimental results show that the proposed algorithm can meet the actual needs and is better than other classical algorithms.

**Keywords:** line array cameras; pavement crack detection; feature analysis; adaptive lifting

## 1. Introduction

With the large-scale construction of high-grade pavement in China in recent years, the detection of pavement damage has become a very important task [1-4]. Currently, semi-automated testing vehicle equipment is widely adopted in the detection of pavement problems. This approach requires manual processing of offline data and fails to achieve full automatic detection of pavement damage [5-6]. It also has many obvious drawbacks. Firstly, the results of manual processing may be affected by the subjectivity of manual detection and thus may not accurately and objectively reflect the real conditions of pavement [7-8]. Secondly, the efficiency of manual detection is usually very low, therefore consumes a lot of manpower. These drawbacks are extremely unfavorable to highway management and maintenance. Moreover, the recognition effect of automatic identification system is not satisfactory and there are still many problems [9-13]. The main causes of these problems are: (1) pavement interference factors, such as shading shadows, water stains, grease and so on; (2) complex road conditions, the lighting conditions of the pavement are different at different time periods, which is highly detrimental to our identification; (3) pavement damage

types, including transverse cracks, longitudinal cracks, chaps, block fractures, etc.. In view of the current testing needs and situation, this paper proposes the use of image processing technology, combined with the adaptive lifting algorithm in machine learning to automatically identify the crack area on the road image [14-18]. The algorithm has high recognition rate and fast speed, and meanwhile can basically meet the actual needs.

2. Materials and Methods

2.1. Image Acquisition

In this paper, high-resolution linear array cameras, image capture cards, combined with integrated LED lights, industrial personal computer(IPC), optical encoder, GPS and other auxiliary devices are used to acquire and store real-time road images, and are integrated as a whole system in a commercial vehicle [19-22]. By contrast, we use line frequency of 140kHz, a resolution of 4k, the model for the Basler sprint-spL4096-140km CMOS linear array cameras to capture road images [23-26].

During the driving process of the vehicle, the photoelectric encoder rotates synchronously with the wheel to generate TTL(Transistor-Transistor Logic) pulse signals, which are processed by the data acquisition card and part of peripheral circuits [27-29]. The computer counts the pulses and converts them into mileage and speed information in real time. In this process, the pulse generated by the photoelectric encoder is modulated to generate a pulse trigger signal for the linear array cameras. When the left and right linear array cameras are triggered, the image of the road surface is collected [30-31]. After the image signal is processed by the image capture card via the Camera Link interface, the image is transmitted to IPC memory to complete the acquisition and storage of information on the road.

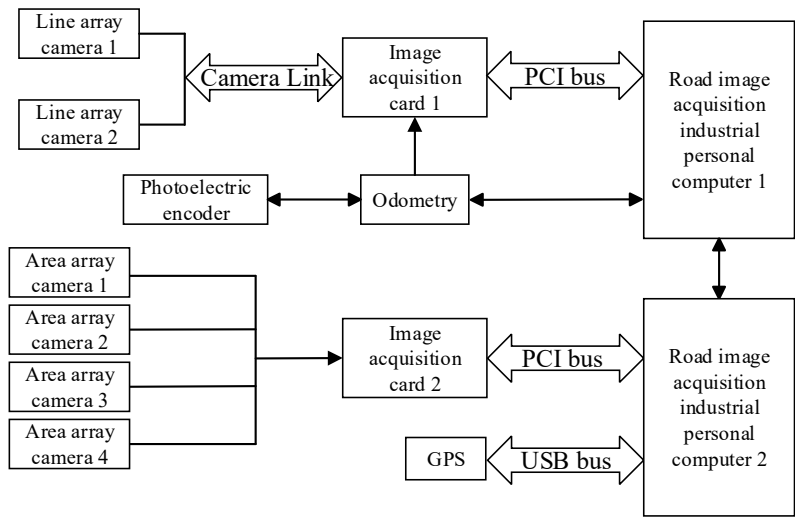
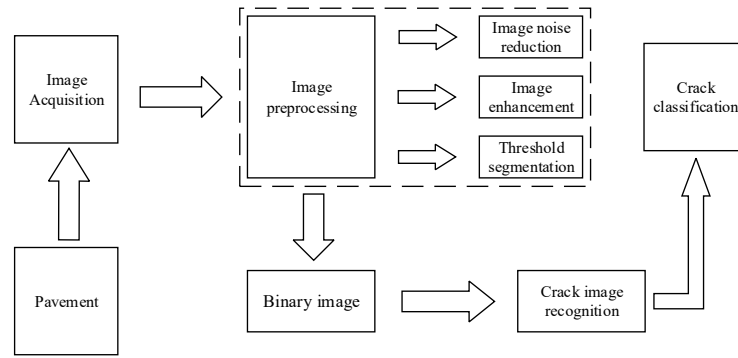


Figure 1. Image acquisition structure block diagram

After road images are obtained, road cracks can be identified through steps shown in Figure 2.



**Figure 2.** Operation flow chart

## 2.2. Image preprocessing

Before cracks in the captured image are identified, the image needs to be preprocessed because acquisition hardware and the natural lighting in the actual scene may inevitably introduce some interference and noise into the captured image [32-34]. In order to facilitate subsequent image processing, these unfavorable factors must be eliminated firstly. To avoid the obvious shortcoming of blurred image of the mean filter, we use the Gauss filter to reduce the image noise [35-38]. Our Gauss filter has a size of 5×5, and can be expressed as:

$$F_{GS} = \frac{1}{273} \begin{bmatrix} 1 & 4 & 7 & 4 & 1 \\ 4 & 16 & 26 & 16 & 4 \\ 7 & 26 & 41 & 26 & 7 \\ 4 & 16 & 26 & 16 & 4 \\ 1 & 4 & 7 & 4 & 1 \end{bmatrix} \quad (1)$$

The convolution of the Gauss filter and the original image  $P_o$  produces the noise-reduced image  $P_d$  [39].

$$P_d = P_o \otimes F_{GS} \quad (2)$$

After some noise is eliminated with the Gauss filter, the image can be further processed to enhance regional characteristics of the cracks to be identified and to weaken background features of the images [40]. The purpose of this process is to reduce the impact of the background information on the later recognition while preserving most of the crack information. We implement the image enhancement with histogram equalization, which converts the input image to hold the same pixel value in each gray scale [41-45]. This method can significantly enhance the contrast of the image.

Assuming that the gray scale range of the captured image is  $[0, L-1]$ , the approximate probability of gray scale  $r_k$  can be calculated as:

$$p(r_k) = \frac{n_k}{N}, k = 0, 1, \dots, L-1 \quad (3)$$

Where  $n_k$  is for the number of pixels in the image with gray scale  $r_k$ ,  $N$  is for the sum of the numbers of all the pixels, and  $L$  is for the number of gray scale  $r_k$ . Gray scale  $r_k$  and the probability of appearance of gray scale  $p(r_k)$  can be expressed as the histogram of the original image [46].

For gray images, the method of the enhancement of histogram equalization can be expressed as [47]:

$$\sum_{i=0}^{r_k} p(i) - \frac{f(r_k)}{L-1} \geq 0, 0 \leq r_k < L \quad (4)$$

Where

$$f(r_k) = \sum_{j=0}^{r_k} u_j (0 \leq j < L) \quad (5)$$

$$\begin{cases} u_j \geq 0 \\ \sum_{j=0}^{L-1} u_j < L \end{cases} (0 \leq j < L) \quad (6)$$

$f(r_k)(0 \leq r_k < L)$  stands for the mapping relationship between the pre-enhancement image gray scale  $r_k$  and the enhanced image gray scale  $r_k'$ .

By the following formula, the transformed gray scale allows the output histogram to be uniform over the entire output gray scale range so that the contrast of the image can be increased.

$$T(r_k) = \text{round}((L-1) \sum_{j=0}^k p(r_j)) \quad (7)$$

Figure 3 is a pavement crack image. After the image preprocessing, Figure 3 turns into Figure 4.

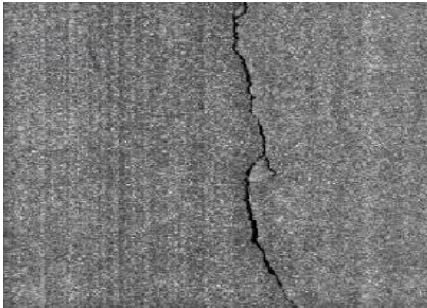


Figure 3. Original image

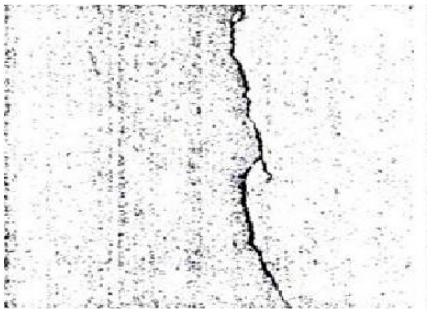


Figure 4. Image after preprocessing

Due to the complexity of the overall pavement condition, the gray value of cracks in different regions of the image varies greatly. Even if the whole image is segmented by the noise reduction with Gauss filter and the image enhancement with histogram equalization, the obtained results still can't meet the actual needs. Therefore, we divide the whole image into a plurality of sub-blocks, and the sub-block regions are separately subjected to threshold segmentation [48-49]. A collected  $3024 \times 2048$  pavement image is divided into  $16 \times 16$  blocks, as shown in Figure 5.

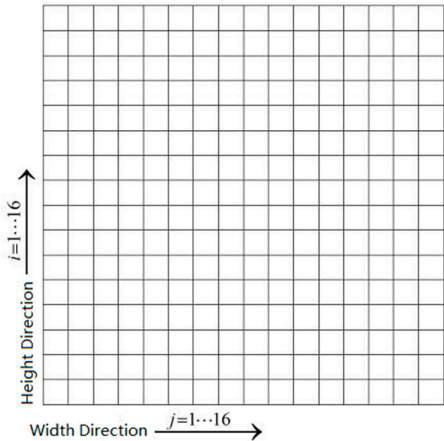


Figure 5. Regional block diagram

2.3. Feature selection

The 256 blocks fall into two categories, those containing cracks and those containing no cracks, as shown in Figure 6.

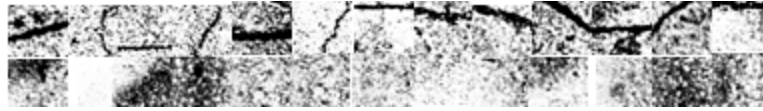


Figure 6. Image after dividing into blocks

Observation and analysis of a large number of image samples reveal that the target of pavement cracks has specific shape features that can be used to categorize the blocks. These shape features can be obtained by binarizing the segmented image with the maximum entropy method. The principle of maximum entropy method states that the entropy takes the maximum value when all events of the system are equally likely to occur [50-51].

The following is the process to use the maximum entropy method to calculate the threshold. For a gray image, assuming the range of the image gray values is  $[0, L-1]$ , and the minimum and maximum gray values are  $V_{\min}$  and  $V_{\max}$  respectively. According to the entropy formula, the entropy value corresponding to the gray value  $t$  can be calculated as

$$E(t) = \lg P_t(1 - P_t) + \frac{H_t}{P_t} + \frac{H_L - H_t}{1 - P_t} \quad (8)$$

Where

$$P_t = \sum_{i=0}^t p_i \quad (9)$$

$$H_t = -\sum_{i=0}^t p_i \lg p_i \quad (10)$$

$$H_L = -\sum_{i=0}^L p_i \lg p_i \quad (11)$$

Here  $p_i$  is the probability that the gray value  $i$  appears,  $P_t$  is the sum of the probability of the gray values from 0 to  $t$ ,  $H_t$  is the sum of the entropy of the gray values from 0 to  $t$ , and  $H_L$  is the entropy of the original image. The objective of our method is to find a proper value of  $t$  between  $V_{\min}$  and  $V_{\max}$  to maximizes  $E(t)$ . The value of  $t$  is the optimal threshold determined by the maximum entropy method.

After the image process by using the threshold, there are still some discrete small particles in the original picture. Therefore, four description values are designed as classification features of the binary image for the obtained image area that is less than the threshold.

(1) The rectangularity of the largest connected region: the ratio of the area of the region to the area of a rectangular region having the same first-order moment and second-order moment in this region. For the fractured segment, the largest connected region is the region where the fractures are located. And the rectangularity of the largest connected region of fractured segments is generally smaller than the non-fractured segments.

(2) The eccentricity of the largest connected region: the ratio of the semi-major axis to the semi-minor axis of the smallest ellipse that can cover the largest connected region. The larger the ratio, the more likely there are cracks in the pavement image.

(3) The area of the largest connected region

$$MA = \max(A_i) \quad (12)$$

where  $A_i$  is the area of the  $i$ th connected domain.

(4) The compactness of the largest connected region: the square of the length of the region outline is divided by the area of the region.

#### 2.4. Crack recognition classification

The regional characteristic descriptors obtained from the previous step can be used to determine whether the current sub-block contains cracks. We utilize an adaptive lifting algorithm to train the classifier to complete the related classification work [52]. The algorithm consists of the following steps.

(1) Given  $N$  samples of the training data set, each sample contains the above four characteristic description values and whether it is a mark of a crack region or not. The sample set is expressed as follows:

$$T = \{(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)\}; y = \{-1, 1\} \quad (13)$$

where  $\{x_i, y_i\}_{i=1}^N$  stands for training sample set and the corresponding mark.

(2) Initialize weights distribution of the training data set as

$$D_1 = (w_{1,1}, \dots, w_{1,i}, \dots, w_{1,N}), w_{1,i} = \frac{1}{N}, i = 1, 2, \dots, N \quad (14)$$

(3) For  $m = 1, 2, 3, 4$ , uses a training dataset with weight distribution  $D_m$  for learning, and generates the basic classifier  $G_m(x)$  [53]. In the meantime, calculates the error rate  $e_m$  of classification and the coefficient  $\alpha_m$  of the basic classifier  $G_m(x)$  in the training data set using the following formulas.



$$e_m = P(G_m(x_i) \neq y_i) = \sum_{G_m(x_i) \neq y_i} w_{m,i} \quad (15)$$

$$\alpha_m = \frac{1}{2} \lg \frac{1-e_m}{e_m} \quad (16)$$

Where  $w_{m,i}$  is the weight of the  $i$ th sample in round  $m (m \in \{1, 2, 3, 4\})$ , and

$$\sum_{i=1}^N w_{m,i} = 1 \quad (17)$$

(4) Update the distribution of weights of the training data set.

$$D_{m+1} = (w_{m+1,1}, \dots, w_{m+1,i}, \dots, w_{m+1,N}) \quad (18)$$

$$w_{m+1,i} = \frac{w_{m,i}}{Z_m} \exp(-\alpha_m y_i G_m(x_i)), i = 1, 2, \dots, N \quad (19)$$

Where  $Z_m$  is the factor of normalization.

$$Z_m = \sum_{i=1}^N w_{m,i} \exp(-\alpha_m y_i G_m(x_i)) \quad (20)$$

(5) Construct the linear combination of the basic classifier and obtain the strong classifier that can determine whether the current sub-block image contains cracks.

$$G(x) = \text{sign}(\sum_{m=1}^4 \alpha_m G_m(x)) \quad (21)$$

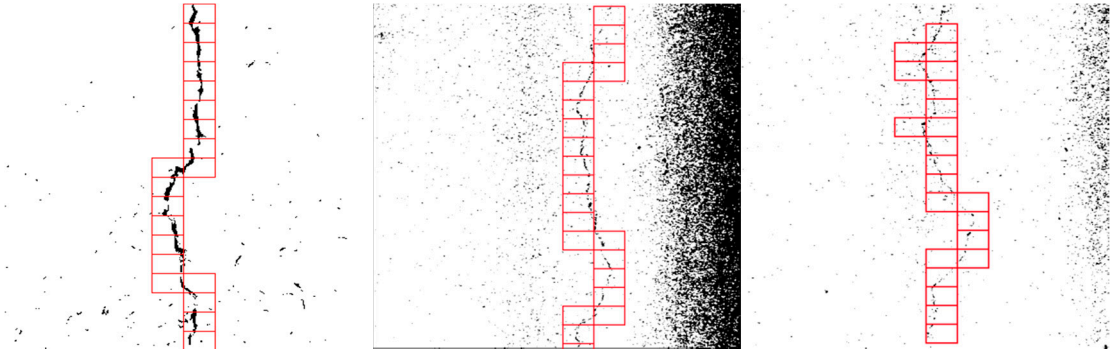
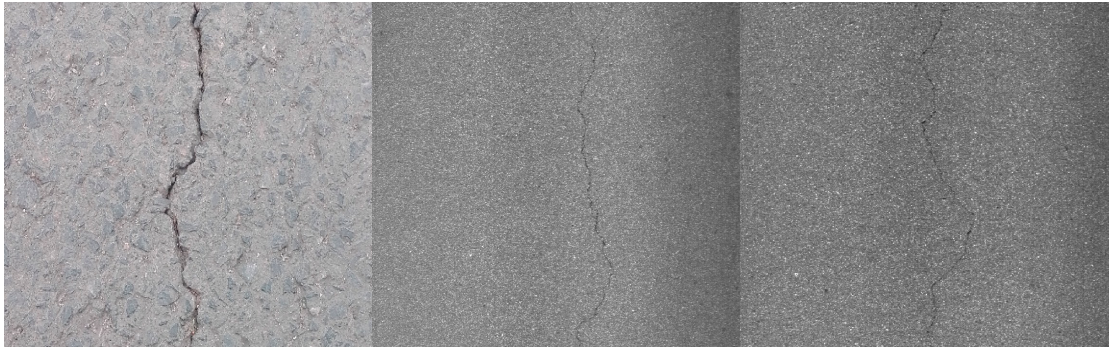
The target area containing the cracks is marked with a red range. The damage rate is calculated as the ratio of the number of marked sub-blocks to the total number of sub-blocks [54]. The recognition results are shown in Figure 7.





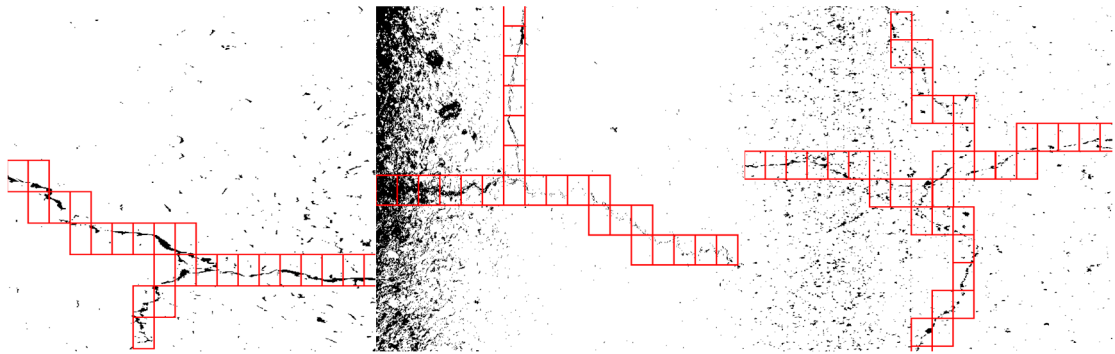


(a)



(b)





(c)

Figure 7. Crack recognition results. (a) Transverse cracks; (b) Longitudinal cracks; (c) Irregular cracks

The overall algorithm is shown in Figure 8.

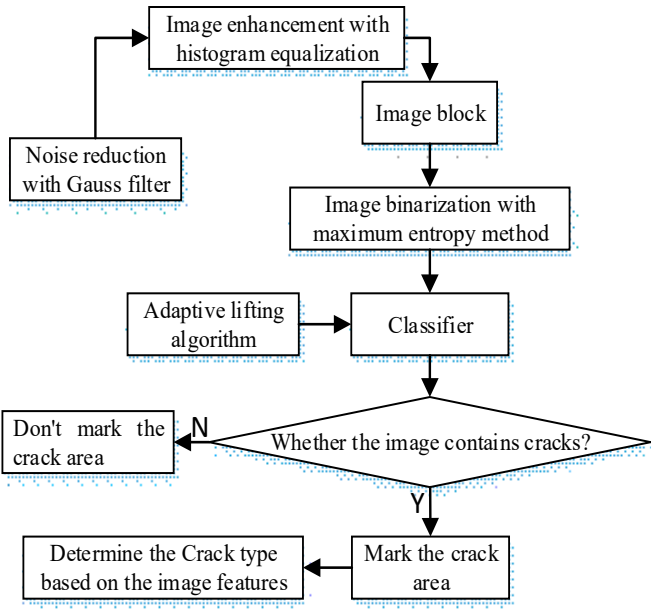


Figure 8. Flow diagram of algorithm

3. Results

To verify the effectiveness of this algorithm, a set of 1000 pavement damage pictures provided by a provincial highway bureau were used to perform a comparison experiment with manual detection, and two other commonly used algorithms: the minimal deviation algorithm and the OSTU algorithm. The experiment hardware environment is 2.40GHZ CPU, 8G memory IPC, and the software environment is VC2010. The experiment was repeated eight times and the results are shown below in Table 1.

Table 1. Average time taken to detect cracks in a single image by the four methods

	Manual detection	Algorithm in this paper	Minimal deviation algorithm	OSTU algorithm
#1	4387ms	235ms	892ms	1233ms
#2	3315ms	346ms	1123ms	1452ms
#3	5789ms	532ms	965ms	1678ms
#4	4310ms	490ms	1387ms	1783ms
#5	3520ms	456ms	732ms	1653ms
#6	5120ms	378ms	1232ms	1723ms
#7	4760ms	612ms	934ms	1974ms
#8	4239ms	563ms	1365ms	1923ms

It can be seen that the detection speed of the algorithm in this paper is faster than that of manual detection and the other two commonly used algorithms. We also compared the accuracy of the detection methods of the four algorithms. The results are shown in Figure 9.

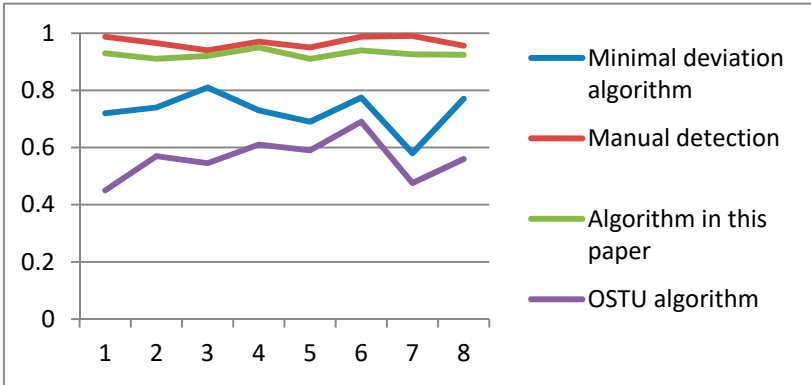


Figure 9. Accuracy of crack detection of the four methods

4. Discussion

From Figure 9, we can see that the accuracy of crack detection of the proposed algorithm is slightly lower than manual detection, but far superior to the other two commonly used algorithms. The accuracy of the algorithm in this paper can meet the detection accuracy requirements of the actual pavement detection department.

5. Conclusions

Through theoretical research and actual experiments, we can draw the following conclusions:

(1) Currently, the detection of pavement crack is mainly conducted with manual identification. On the other hand, there are still many problems with automatic recognition, such as slow identification, poor accuracy and so on. Therefore, this paper adopts the adaptive lifting algorithm for automatic pavement crack recognition.

(2) Through image processing combined with adaptive lifting model in machine learning, we can calculate the ratio of the number of crack sub-blocks to the total number of image sub-blocks and use it to characterize the degree of crack damage in the current image. The results suggest that the speed and accuracy of recognition of our proposed algorithm can meet actual requirements.

(3) The current research mainly focuses on pavement cracks, but it cannot automatically detect other types of damage, such as bags, pits, and repair of cracks. In the future, our research goal should place on other types of damage pavement to further improve the automatic pavement damage recognition system.

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**Conflicts of Interest:** The authors declare no conflict of interests.

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