

Article

Emerging Quantum Fields Embedded in the Emergence of Spacetime

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Abstract: Based on a local causal model of the dynamics of curved discrete spacetime, a causal model of quantum field theory in curved discrete spacetime is described. At the elementary level, space(-time) is assumed to consist of interconnected space points. Each space point is connected to a small discrete set of neighbor space points. Density distribution of the space points and the lengths of the space point connections depend on the distance from the gravitational sources. This leads to curved spacetime in accordance with general relativity. Dynamics of spacetime (i.e., the emergence of space and the propagation of space changes) dynamically assigns "in-connections" and "out-connections" to the affected space points. Emergence and propagation of quantum fields (including particles) are mapped to the emergence and propagation of space changes by utilizing identical paths of in/out-connections. Compatibility with standard quantum field theory (QFT) requests the adjustment of the QFT techniques (e.g., Feynman diagrams, Feynman rules, creation/annihilation operators), which typically apply to three in/out connections, to $n > 3$ in/out connections. In addition, QFT computation in position space has to be adapted to a curved discrete space-time.

Keywords: quantum field theory, local causal models, general relativity theory, spacetime models, discrete spacetime, computer simulations

1. Introduction

The authors attempt to construct a local causal model of quantum theory (QT), including quantum field theory (QFT), soon resulted in the recognition that a causal model of the dynamics of QT/QFT should better be based on a causal model of the dynamics of spacetime. Thus, a causal model of the dynamics of spacetime has been developed with the major goals (1) as much as possible compatibility with general relativity theory (GRT), and (2) the model should match the main features of the evolving model of QT/QFT. The main features of the authors model of QT/QFT are

- the model has to be a causal model,
- if possible, the model should be a *local* causal model,
- discreteness of the basic parameters (time, space, propagation paths).

Not surprisingly, it turned out that a clear definition of these features/requirements, especially of a local causal model, is useful (not only for understanding the requirements, but also for the derivation of the implications). A semi-formal definition of a (local) causal model has been published in several articles from the author (see [1], [2] and [3]) and is also given in Section 2.

The construction of a causal model of spacetime dynamics started with the search for some existing theory or model which might be at least a starting point for the model to be developed. Causal dynamical triangulation (CDT, see [4], [5], [6]) and more abstractly the concepts of loop quantum gravity (see [7] and [8]) were identified to match the authors requirements and thinking. The further model construction showed that, in order to come up with a local causal model according to the definitions given in Section 2, adaptations and refinements of the original CDT-based model appear appropriate. The adaptations and refinements concern basic GRT concepts such as (i) the elementary structure of space(-time), (ii) the representation of space(-time) curvature, and (iii) the relation between

39 space and time. With GRT and special relativity theory (SRT), space and time are said to be integrated
 40 into spacetime. For the GRT-compatible model of spacetime dynamics, the integration of space and
 41 time remains, but with a different interpretation. The elementary structure of space(-time), including
 42 the space-time relationship is described in Section 3. The causal model of the spacetime dynamics is
 43 described in Section 4.

44 The major goal for the development of a causal model of spacetime dynamics (Sections 3 and
 45 4) was to develop a model of the spacetime elementary structure that constitutes a suitable base
 46 for both the causal model of spacetime dynamics and the causal model of QT/QFT. The proposed
 47 model satisfies this goal. The emergence and propagation of quantum fields (including particles)
 48 can be mapped to the emergence and propagation of space changes by utilizing identical paths of
 49 in/out-connections between space points. In Section 5, this main subject of the article is described.

50 2. Causal Models

51 The specification of a causal model of a theory of physics consists of (1) the specification of the
 52 system state, (2) the specification of the laws of physics that define the possible state transitions when
 53 applied to the system state, and (3) the assumption of a "physics engine."

54 2.0.1. The physics engine

55 The physics engine represents the overall causal semantics of causal models. It acts upon the state
 56 of the physical system. The physics engine continuously determines new states in uniform time steps.
 57 For the formal definition of a causal model of a physical theory, a continuous repeated invocation of
 58 the physics engine is assumed to realize the progression of the state of the system.

59
 60 physics engine $(S, \Delta t) := \{$
 61 DO UNTIL($\text{nonContinueState}(S)$) {
 62 $S \leftarrow \text{applyLawsOfPhysics}(S, \Delta t);$
 63 }
 64 }

65 2.0.2. The system state

66 The system state defines the components, objects and parameters of the theory of physics that can
 67 be referenced and manipulated by the causal model. In contrast to the physics engine, the structure
 68 and content of the system state are specific for the causal model that is being specified. Therefore, the
 69 following is only an example of a possible system state specification.

70
 71 $\text{systemstate} := \{\text{spacepoint}...\}$
 72 $\text{spacepoint} := \{x_1, x_2, x_3, \psi\}$
 73 $\psi := \{\text{stateParameter}_1, \dots, \text{stateParameter}_n\}$
 74

75 2.0.3. The laws of physics

76 The refinement of the statement

77 $S \leftarrow \text{applyLawsOfPhysics}(S, \Delta t);$ defines how an "in" state s evolves into an "out" state $s.$

78 $L_1 := \text{IF } c_1(s) \text{ THEN } s \leftarrow f_1(s);$
 79 $L_2 := \text{IF } c_2(s) \text{ THEN } s \leftarrow f_2(s);$
 80 \dots
 81 $L_n := \text{IF } c_n(s) \text{ THEN } s \leftarrow f_n(s);$

82 The "in" conditions $c_i(s)$ specify the applicability of the state transition function $f_i(s)$ in basic formal
 83 (e.g., mathematical) terms or refer to complex conditions that then have to be refined within the formal
 84 definition.

85 The state transition function $f_i(s)$ specifies the update of state s in basic formal (e.g., mathematical)
86 terms or refers to complex functions that then have to be refined within the formal definition.
87 The set of laws L_1, \dots, L_n has to be complete, consistent and reality conformal (see [9] for more details).
88 In addition to the above-described basic forms of specification of the laws of physics by $L_n :=$
89 $IF c_n(s) THEN s \leftarrow f_n(s)$, other forms are also imaginable and sometimes used in this article.¹

90 2.1. Requirements for causal models of spacetime

91 For causal models of spacetime, obviously, some notion of space and time must be supported.
92 Ideally, the treatment of space and time would be, as much as possible, compatible with special
93 relativity theory (SRT) and general relativity theory. However, the formally defined causal model
94 of Section 2 presupposes a certain structure of spacetime in which space and time are rigorously
95 separated. This disturbs the integrated view of space and time that is taught by GRT/SRT. In the
96 proposed model of spacetime dynamics, the integration of space and time is largely restored by the
97 specification of the relationships described in Section 3.1.

98 2.1.1. The representation of time in the causal model

99 In the causal model defined above, time is not like space and other parameters a system state
100 component, but it has a special role outside the system state. The overall purpose of the causal model
101 is seen in showing the progression of the system state in relation to the progression of time. This
102 relationship can best be described by assuming a uniform progression of the time. This leads to the
103 model (described above) where the time and the progression of time is built into the model in the form
104 of the physics engine. The physics engine progresses the system state in uniform time steps called
105 state update time intervals (SUTI).

106 In GRT and SRT, there are situations where the clock rate of a causal subsystem is predicted to
107 differ depending on the relative speed of movement or the position within a gravitational field. GRT
108 and SRT refer to this by the name "proper time". If, for a specific causal model of an area of physics
109 the differing proper times of causal subsystems are relevant and/or the internal processes within the
110 subsystems are included in the model, separate physics engines may be assigned to the subsystems
111 with different proper times.²

112 If, however, the causal model describes an area of physics where the relationship between proper
113 times and other parameters is to be shown, it should be possible to show this with a single physics
114 engine and a uniform SUTI for the overall system. For the proposed causal model of spacetime
115 dynamics, the space-time relationship described in Section 3.1 enables a single physics engine and a
116 uniform SUTI.

117 2.1.2. Spatial causal model

118 A causal model of a theory of physics is called a *spatial* causal model if (1) the system state contains
119 a component that represents a space, and (2) all other components of the system state can be mapped
120 to the space. There exist many textbooks on physics (mostly in the context of relativity theory) and
121 mathematics that define the essential features of a "space". For the purpose of the present article, a
122 more detailed discussion is not required. For the purpose of this article and the subject locality, it is
123 sufficient to request that the space (assumed with a spatial model) supports the notions of position,
124 coordinates, distance, and neighborhood.

¹ This article does not contain a proper definition of the used causal model specification language. The language used is assumed to be largely self-explanatory.

² An example can be found in the causal model described in [3], where separate physics engines are assigned to the "quantum objects".

125 A special type of spatial causal model that has been increasingly addressed in recent years is
126 the cellular automaton (see [10], [11], [12] and [13]). The causal model described in this article also
127 represents a spatial causal model.

128 2.1.3. Local causal model

129 The definition of a local causal model presupposes a spatially causal model (see above). A
130 (spatially) causal model is understood to be a local model if changes in the state of the system
131 depend on the local state only and affect the local state only. The local state changes can propagate to
132 neighboring locations. The propagation of the state changes to distant locations; however, they must
133 always be accomplished through a series of state changes to neighboring locations.³

134 Based on a formal model definition of a causal model, a formal definition of locality can be
135 given. A physical theory and a related spatially causal model with position coordinates x and position
136 neighborhood dx (or Δx in the case of discrete space-points) are given. A causal model is called a
137 local causal model if each of the laws L_i applies to no more than a single position x and/or to the
138 neighborhood of this position $x \pm dx$.

139 In the simplest case, this arrangement means that L_i has the form

140
$$L_i : \text{IF } c_i(s(x)) \text{ THEN } s'(x) = f_i(s(x));$$

141 The position reference can be explicit (for example, with the above simple case example) or implicit by
142 reference to a state component that has a well-defined position in space. References to the complete
143 space of a spatially extended object or to a property of a spatially extended object are considered
144 to violate "space-point-locality". Causal models with a system state that includes composite objects
145 with global properties (e.g., mass, charge, velocity) may still be considered local causal models, more
146 specifically "object-local causal model", even if such global properties are referenced in the model.

147 2.1.4. Background-independence

148 Background independence is an important requirement that is typically established for spacetime
149 models such as spin networks, spin foam, and causal dynamical triangulation. This requirement seems
150 to be mandatory for a local causal spacetime model that supports the emergence of spacetime from a
151 minimal or zero source. Background independence means that all spacetime dynamics, in particular
152 the emergence of space, must be expressible without reference to any predefined coordinate system or
153 other global spacetime properties. For a causal model, this means that the structure of spacetime must
154 not contain components and properties that are non-local.

155 2.1.5. Composite objects

156 Models of areas of physics typically contain spatially extended composite objects such as particles,
157 atoms, stars, and so forth, and typically object-global properties (e.g., mass, charge, velocity) are
158 referenced in such models. According to the definition of a local causal model (above), such models
159 may only be called "object-local causal models" (as opposed to "space-point-local causal models"). Such
160 models may be useful; however, care must be taken that the assignment of object-global properties
161 to composite objects is admissible with the level of accuracy aimed for. Object-global properties are
162 typically the result of aggregations from lower-level relationships. The aggregations toward a single
163 global attribute value may be admissible with classical physics, but questionable with refinements of
164 modern theories of physics. A famous example of the inclusion of global object properties refers to the
165 attributes of mass and charge with quantum field theory when particles are no longer considered to be
166 point-like particles.

³ Special relativity requests that the series of state changes does not occur with a speed that is faster than the speed of light. This requirement is not considered essential for a causal model.

¹⁶⁷ **3. The elementary structure of spacetime**

¹⁶⁸ *3.1. The space-time relationship*

¹⁶⁹ With GRT and SRT, space and time are said to be integrated into spacetime. For a GRT-compatible
¹⁷⁰ model of spacetime dynamics, the integration of space and time remains visible, but with a different
¹⁷¹ interpretation. With GRT, the integration of space and time is mathematically expressed in the usage of
¹⁷² tensors (e.g., curvature tensor) and 4-vectors with a time component and space components. Physically,
¹⁷³ the integration is reflected, among other ways, in the metric and the symmetries that hold for the
¹⁷⁴ combined (space+time) entities and the corresponding laws of physics.

¹⁷⁵ In the proposed causal model of spacetime dynamics, the tensors and 4-vectors of GRT/SRT
¹⁷⁶ occur only as the starting point for the introduction of GRT-compatible equivalent model parameters.
¹⁷⁷ The integration of space and time appears to be disturbed by the fundamentally different roles space
¹⁷⁸ and time represent in a causal model. Time and the progression of time are an inherent feature of the
¹⁷⁹ physics engine of the causal model. The physics engine implements the uniform and simultaneous
¹⁸⁰ progression of time. Space is the explicit global object that is part of the system state. Other objects of
¹⁸¹ the system state are positioned in space. Although space and time conceptually have quite different
¹⁸² roles within the causal model, it is their mutual relationship that establishes their (re-)integration.

In GRT, the curvature specification, i.e., the curvature tensor, contains, in addition to the three space-related components, a time-related component. As an example of the impact of the time factor, the gravitational redshift is explained as the consequence of the time factor in the spacetime curvature (see, for example, [14], page 231).

$$\Delta s^2 = -(1 - \frac{2GM}{c^2r})(c\Delta t)^2 + (\Delta x)^2 + (\Delta y)^2 + (\Delta z)^2 \quad (1)$$

This means a clock at position (x, y, z) would run by a factor

$$F_1 = \sqrt{1 - \frac{2GM}{c^2r}} \quad (2)$$

¹⁸³ slower than a clock that is not affected by a gravitational field. A standard clock at some point A of
¹⁸⁴ low potential (for example, on the surface of the earth) would go slower than the same clock at point B
¹⁸⁵ of higher potential (for example, at a GPS satellite). In [14]: "... The gravitational redshift implies that
¹⁸⁶ time itself runs slightly faster at the higher altitude than it does on the Earth." For the GPS system, the
¹⁸⁷ difference is 45 microseconds per day: This is the rate at which the clocks at the satellites go faster (see
¹⁸⁸ [15]). In GRT, this effect is called "gravitational time dilation". For reasons that are described in the
¹⁸⁹ following, the author prefers the wording (gravitational) "clock rate dilation".

¹⁹⁰ For a mapping of the time factor of the GRT curvature specification to the proposed spacetime
¹⁹¹ model, two problems arise:

- ¹⁹² In the causal model, the clock rate (i.e., the proper time) is a property of the whole causal
¹⁹³ subsystem. The assignment of clock rates to the different positions occupied by a spatial
¹⁹⁴ distributed causal subsystem is not supported with the proposed causal model.⁴
- ¹⁹⁵ In the causal model, the clock rate is maintained by the physics engine (i.e., the clock is part of
¹⁹⁶ the physics engine which delivers the uniform state update time interval). Changes in the clock
¹⁹⁷ rate resulting from the objects motion in space would mean that the clock of the physics engine
¹⁹⁸ has to run slower or faster depending on the object's position in space. This would require a
¹⁹⁹ rather ugly interface between the space and the physics engines of the causal subsystems.

⁴ The assignment of differing clock rates to the different positions occupied by a spatial distributed causal subsystem would make causal models for the dynamics of subsystems extremely difficult.

200 Problem (2) may be viewed as a problem due to the specific definition of a causal model given in
201 Section 2. However, there are (good) reasons for this definition of a causal model. Problem (1) refers to
202 the causal model of causal subsystems in general. It would also be difficult to avoid this problem with
203 alternative causal model concepts.

204 A possible solution that would make it possible to maintain a uniform progression of the state
205 update time interval SUTI while enabling non-uniform clock rates may be found if one remembers
206 that, in SRT and GRT, space and time are considered as an entity and that this implies that space
207 intervals and time intervals can be jointly transformed by certain symmetry transformations. For
208 the example gravitational redshift, this means that the redshift is interpreted as the dilation of the
209 wave length instead of the increase of the frequency and that the length dilation affects not only the
210 wave length but all lengths within the gravitational potential. For the proposed model of spacetime
211 dynamics, it is assumed that

212

213 **Proposition 1.** *Lengths within the gravitational field are dilated by the factor F_1 .*

214 ⁵ How can this help to prevent the need for the dynamic and position-dependent change of the
215 state update time interval (SUTI)? A further proposition was introduced:

216 **Proposition 2.** *Physical processes run faster/slower depending on the length scale at the position where the
217 respective physical process executes.*

218 Notice that the clock rate dilation concerns physical processes, not the spacetime structure.
219 Space(-time) curvature is the result of length dilations. Clock rate dilation is another consequence of
220 length dilations.

221 The major process that demonstrates the fixed relationship between the length dilation and the
222 process change rate is the propagation of light. This (simple) process is used as a measure for the
223 change rate of other processes by setting the speed of light to be a constant c . The next class of
224 processes where the change rate depends on the length dilation in precisely the proportions as with
225 the propagation of light are clocks in differing realizations.

226 In summary, in the model of spacetime dynamics, there is no direct reflection of time dilation as a
227 spacetime attribute. Clock rate dilation (rather than time dilation) occurs as a property of processes
228 running within space. The clock rate dilation factor can be derived from the length dilation factor F_1 of
229 the space points where the respective process is currently executing.

230 In the model of spacetime dynamics, two levels of time are distinguished, which in GRT/SRT are
231 seen as an entity:

- 232 1. At the basic level, the progression of time is associated with the physics engine of the causal model.
233 The time of the physics engine proceeds in uniform state update time intervals. Simultaneity
234 is assumed for all state changes occurring at the same state update cycle.
- 235 2. Differing clock rates, proper times, and relativity of simultaneity are not associated with the
236 basic overall spacetime, level (1), but are associated with objects residing and moving in space -
237 more precisely, with processes running in these subsystems.

238 With space, two levels also may be distinguished, but these are two levels of consideration:

5 "Gravitational length dilation" appears to be a very controversial subject among physicists (see various discussion in internet forums). The author here takes a strong position while at the same time stating a clear relation between (1) the length dilation and (2) the clock rate dilation, namely by saying that (2) is a consequence of (1).

239 • At the abstract level (i.e., mathematical level), the space consists of a set of interconnected space
240 points (see Section 3). Whether or not the totality of interconnected space points represents an
241 Euclidean space or a specific topology (e.g., Riemann manifold) is left open.
242 • At the physical level (i.e., the essential level), meaning is assigned to the components of the space
243 point. Especially, the length of the connections is no longer a geometrical property, but specifies
244 the Δ length *only* with respect to a specific physical process executing at the respective space point
245 for the time interval SUTI. The process that is used as the measure for the specification of the
246 length is the propagation of light.

247 Thus, the integration of space and time into spacetime is established in the model of spacetime
248 dynamics by the physical meaning assigned to the components of the space points and their
249 connections.

250 1. Time progresses uniformly in constant units. As a suitable basic unit of time progression, the
251 state update time interval (SUTI) of the physics engine is taken. This means, the SUTI is assumed
252 to be a system constant.
253 2. Length specification is expressed in relation to the spatial distance change caused by a specific
254 physical process running for the duration of the standard unit of time (i.e., the SUTI).⁶
255 3. The physical process that is used as the measure for the standard unit of time as well as the
256 measure of spatial distances is the propagation of light.⁷

257 The proposition (fact?) that there is such a simple relationship between the spatial length dilations
258 and the rate of state changes of processes that execute at a given position in space is the root of the
259 space-time integration in the proposed model of spacetime dynamics. A possible foundation of this
260 supposed space-time relationship (reflecting the space-time integration) may be that

261 **Conjecture 3.1.** All physical processes can ultimately be broken down to length-related state changes,
262 and changes in the length scaling therefore directly result in clock rate dilations of the affected process.

263 3.2. The elementary structure of space

264 The proposed elementary structure of spacetime constitutes the base for the overall model of
265 spacetime dynamics that is compatible with GRT. A number of works toward the same or a similar
266 goal have been published. The work that shows the most similarities with the model described in this
267 article in terms of the overall orientation (background independence; discreteness of time, space, and
268 paths; expressing causal relationships) is causal dynamical triangulation (CDT, see [4], [5], and [6]).
269 The spacetime structure of the model described in this article is based on CDT. However, it was felt
270 that adaptations were required to further refine the causal relationships of spacetime dynamics, in
271 particular to construct a causal model of the emergence of space from a single source.

272 With CDT, the basic space elements are n-dimensional simplexes (e.g., triangles, tetrahedrons; see
273 Fig. 1). In contrast to CDT, the proposed causal model of curved discrete spacetime considers only
274 3-dimensional space elements, i.e., tetrahedrons. The time dimension is treated separately within the
275 causal model. In addition, the elementary units that represent the total space are not (as with CDT)
276 the n-dimensional simplexes, but only the space points together with their connections to neighbor
277 space points⁸. Whether the space points together with the connections establish specific 2-dimensional
278 surface areas (e.g., triangles) and 3-dimensional solids (e.g., tetrahedrons) is initially left open.

6 This means, in the causal model, spatial distances are not primarily a geometrical property, but rather a physical property used to formulate interrelationships between objects in space.

7 This has the consequence, that in the model (as with most models of physics), the speed of light c is a constant.

8 The reason for this simplification was that it was not possible to build up a larger space object by the continuous addition of uniform regular tetrahedrons and (2) the uniformness of the tetrahedrons is obsolete with the proposed model (see Section 4).

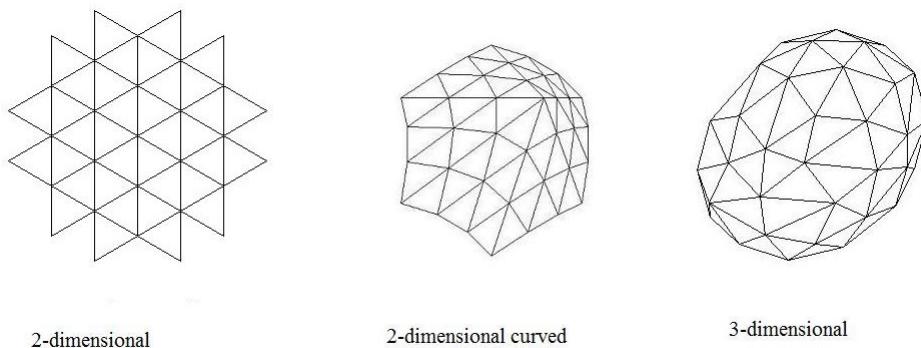


Figure 1. Elements of spacetime of Causal Dynamical Triangulation.

279 **Definition 1.** *Space := { spacepoint ...};*
 280 *spacepoint := { ψ , dilationfactor, connections };*
 281 *connections := { connection₁, ..., connection_n };*
 282 *connection := { neighborspacepoint, direction, Δ curvature };*

283 ψ is the physical content that is directly associated with the space. These are the fields residing
 284 in space. As with spin networks, spin foam networks, and causal dynamical triangulation, each
 285 space point is connected with a number of other space points via "connections" (i.e., edges in CDT). A
 286 connection carries the information about the connected neighbor space point, the connection direction,
 287 and the propagation gradient of the curvature changes (see Section 4).

288 All the information associated with the space point is local to the space point (i.e., no globally
 289 defined position or direction specification). This supports the background independence of the
 290 spacetime model.

291 To enable the determination of the spatial distance between two space points, some information
 292 about the distance between neighbor space points is required. This could be provided, for example,
 293 in form of position coordinates ⁹ or by the specification of the lengths of connections between the
 294 neighbor space points. In support of a causal model of the movement of objects in curved space, for
 295 the proposed model of spacetime dynamics, it is defined that

296 **Proposition 3.** *The length of the connections between space points is a constant;*
 297 $L_{connection} = c \cdot SUTI$.

298 The overall distance between two space points within the curved space is then obtained by
 299 multiplying $L_{connection}$ by the number of space points k_p on the geodesic path from space point-1 to
 300 space point-2. Length dilation within a gravitational potential as assumed by Proposition 1 in Section
 301 3.1, is realized by the appropriate arrangement of the space points within space (see Section 4).

302 Proposition 3 is, first of all, a physical statement, although it has consequences for the space
 303 geometry. The physical statement is:

304 *The (spatial) distance that light moves during a state update time interval (SUTI) is equal to the distance*
 305 *between two connected neighbor space points, which is equal to the distance by which space expands during a*
 306 *SUTI.*

307 The geometry of the emerged space (e.g., whether an Euclidean space or a Schwarzschild metric
 308 emerges) depends on the space expansion algorithm. With the proposed model of spacetime dynamics

⁹ Provision of space point coordinates would violate background independence.

309 the resulting geometry depends on the ratio by which the number of space points grow at a single
 310 expansion step (see Section 4.1).

311 *3.3. The representation of space(-time) curvature*

312 Space curvature is a major ingredient of GRT. In GRT, specifically in Einstein's equation

$$313 G^{\alpha\beta} = 8\pi T^{\alpha\beta},$$

314 space curvature is expressed by the curvature tensor $G^{\alpha\beta}$. Thus, the simplest solution would be to say
 315 that a space-curvature component is assigned to the space point and that this curvature specification
 316 provides the same information as the curvature tensor of GRT. However, some adaptations appear
 317 reasonable. In Section 3.2 above, the space component of the system state is specified as consisting
 318 of a set of space points, and, at the next level of detail, a space point is specified as consisting of
 319 dilationfactor, connections, and the space content ψ .

320 $\text{spacepoint} := \{ \psi, \text{dilationfactor}, \text{connections} \};$

321 The dilationfactor supports the generation of the space curvature with the propagation of space
 322 changes (including the emergence of space). Once the space has emerged, the space(-time) curvature
 323 is represented by (1) the distribution and density of the space points and (2) the (spatial) distances
 324 between neighboring space points. Proposition 3 (above) states that the length of the connections
 325 between space points, i.e., the distances between neighboring space points, is a constant. Thus, the
 326 main parameter that determines the space curvature is the density distribution of the space points.
 327 The density distribution of space points is realized by the appropriate arrangement of the space points
 328 within space.

329 As described in Section 3.1, Proposition 2, the the clock rate dilation (i.e., the time-related
 330 component of the GRT curvature) is a consequence of the length dilations. This means that the
 331 information which specifies the length dilations implies the time-related component of the GRT
 332 curvature.

333 **4. Space(-time) dynamics**

334 The dynamics of spacetime is triggered by the minimal sources, called "quantum objects". With
 335 each update cycle of the system state a new space change action starts at each quantum object. The
 336 space changes propagate from the quantum objects through the whole space in steps according to the
 337 update cycles of the physics engine. In support of a *local* causal model, with each update cycle, the
 338 space changes propagate only to (part of) the neighboring space points. The propagating space changes
 339 always have definite directions at each space point, from the "in-connections" to the "out-connections"
 340 of the space point. The out-connections of space point sp , at a given update cycle i , are in-connections
 341 of some neighbor space points of sp with the subsequent update cycle $i+1$.

342 The directions of space changes, i.e., the identification of in/out-connections, are determined
 343 by the $\Delta\text{curvature}$ attribute of the space point connections. For a given space point, only part of
 344 the connections can be in-connections, which means $\text{connection}.\Delta\text{curvature} > 0$. The remaining
 345 connections of the space point are out-connections.

346 The overall process of space change propagation is specified as

347 **Specification 1.** $\text{spaceprogression}() := \{$
 348 FOR (all space points sp_i) {
 349 IF (inconnections(sp_i) {
 350 propagateOUT(sp_i);
 351 } }
 352 }

353 4.1. The emergence of space from a single source

354 The space that emerges from a single source represents a Schwarzschild metric. In the causal
 355 model, the large-scale space object emerges by the successive addition of surface layers to the initial
 356 space object.

357
 358 SSspaceemergence(source) ::= {
 359 spaceobject ← source;
 360 DO UNTIL(*nonContinueState(S)*){
 361 spaceobject ← *extendbynextlayer*(spaceobject);
 362 }
 363 }
 364 }

364 For the refinement of the above space emergence process, answers to the following questions have to
 365 be provided:

366 1. What are the elementary units of space?
 367 2. How does the initial space object look like?
 368 3. What is the detailed algorithm for *extendbynextlayer*(*spaceobject*)?

369 4.1.1. The elementary units of space

370 The elementary structure of space, including the elementary units of space, have already been
 371 described in Section 3.2. In the proposed model, the elementary units of space are the space points
 372 together with their connections to neighbor space points (see Definition 1). The number of connections
 373 (and thus the number of neighbor space points) of a given space point must be large enough to span
 374 the complete three-dimensional space. It should be small enough to enable a moderate growth of the
 375 number of space points with the chosen algorithm of the space emergence process. In the model, a
 376 typical space point has 14 connections (see Fig. 2):

377 • source connection: one connection towards the source of the emerging space,
 378 • target connection: one connection in the primary emerging direction,
 379 • surface connections: four connections in the plane that is perpendicular to the source connection
 380 (S1, S2, S3, S4 in Fig.2),
 381 • four connections in between the source connection and the surface connections (A1, A2, A3, A4
 382 in Fig.2),
 383 • four connections in between the target connection and the surface connections (B1, B2, B3, B4 in
 384 Fig.2).

385 4.1.2. The initial space object

386 There are several alternatives for the initial space object from where the emergence of space and
 387 the propagation of gravitational space dynamics may start. Fig. 3 shows a number of alternatives
 388 investigated by the author. The simplest solution would be to have the space emergence process,
 389 starting from a single tetrahedron (case (a) in Fig. 3) or a double-tetrahedron (case (b) in Fig. 3).
 390 However, more symmetrical initial space objects, such as case (c) or case (d) enable the early emergence
 391 of a symmetrical larger space object through simple space extension algorithms. For the present model
 392 of spacetime dynamics the initial space object is a single space point surrounded by 14 neighbor space
 393 points and the respective connections. The 14 neighbor space points, together with the interconnections
 394 among them represent a spherical surface - the initial surface from where the space emergence starts
 395 (case (d) in Fig. 3).

396 4.1.3. The space expansion algorithm- *extendbynextlayer*(*spaceobject*)

397 As described above, space emergence from a single source is a continuous process where each
 398 system state update cycle of the causal model adds another layer of space to the existing space object.

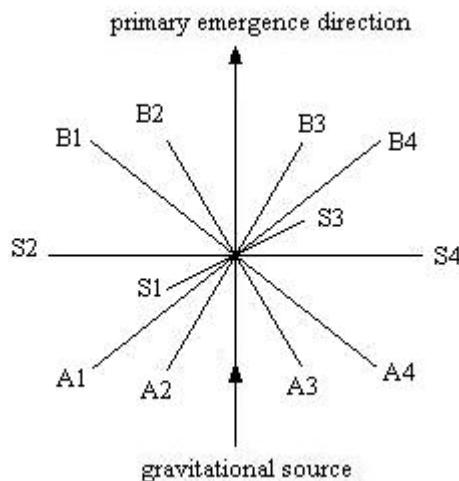


Figure 2. The 14 standard connections of a space point.

Table 1. Layers of space expansion, constant surface $\Delta r = 1.0$

Layer number	surface triangles, kt	surface points, kp	total points, kpt	radius, r_i	av. edge length, L
0	12	8	8	1.00	1.63
1	36	20	72	2.00	1.72
2	108	56	228	3.00	1.55
3	324	164	660	4.00	1.22
4	972	488	1956	5.00	.88
...
12	6377292	3188648	12754596	13.00	...
13	19131876	9565940	38263764	14.00	...
14	57395628	28697816	114791268	15.00	...
...
i	$3 \cdot kt_{i-1}$	$kp_{i-1} + kt_{i-1}$	$ks_i + 3kp_{i-1}$	$(i + 1)100$	

399 This means, with each expansion step st_i a number kp_i of new space points is generated. The new space
 400 points are interconnected with their respective neighbor space point, forming kt_i surface triangles.
 401 Various kinds of space expansion algorithms are possible. The key differentiating parameters for
 402 the alternative space expansion algorithms are the growth factor gp of the number of surface space
 403 points (i.e., $kp_i = gp \cdot kp_{i-1}$) and the related growth factor gt of the number of surface triangles (i.e.,
 404 $kt_i = gt \cdot kt_{i-1}$). Table 1 shows the major parameters for an example space emergence algorithm that
 405 starts with an initial space object with 12 surface triangles (case (c) in Fig. 3). The surface growth
 406 factor $gt = 3$, i.e., $kt_i = 3 \cdot kt_{i-1}$. The number of surface space points increases by the number of surface
 407 triangles, $kp_i = kp_{i-1} + kt_{i-1}$.
 408 Further parameters shown in Table 1 are the total number of space points, the radius r_i of the surface
 409 and the average edge length, L of the surface triangles. The average edge length, L is the length
 410 measured by the author's computer simulations and these computer simulations and the length
 411 measurements assume *Euclidean space*. However, *the space emergence process of the model of spacetime*
 412 *dynamics has to generate curved space* that adheres to Schwarzschild metric, with length dilations in
 413 accordance with the Propositions 1, 2 and 3. Especially, Proposition 3 says that $L_{connection}$ is constant.
 414 With the example shown in Table 1, $L_{connection} = \Delta r = 1.0$. This means that the circumference of a
 415 surface, if curved space and $L_{connection} = 1.0$ is assumed, depends solely on the number of surface
 416 space points, kp_i . The number of surface space points, kp_i for a surface S_i is determined by the space
 417 expansion algorithm. For the proposed model of spacetime dynamics, a curved space with length

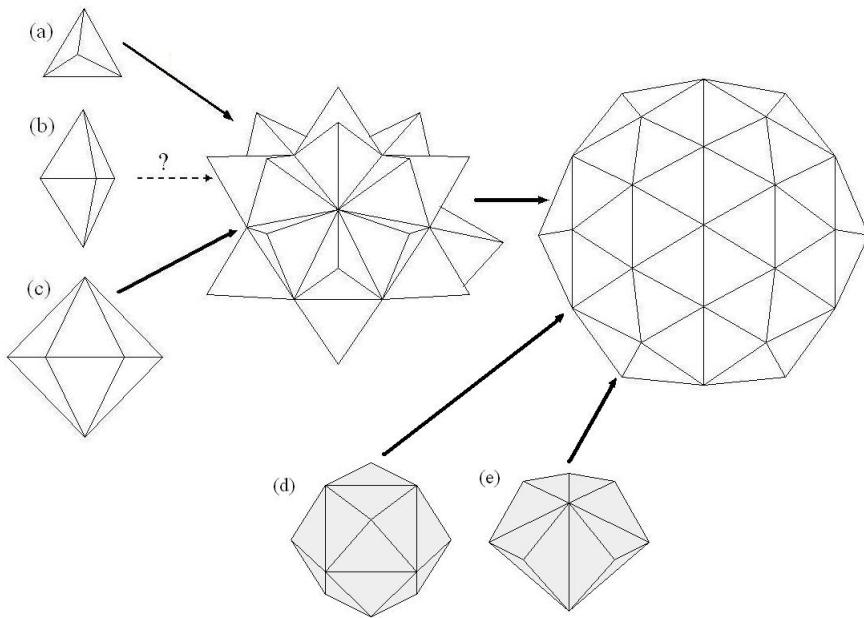


Figure 3. Alternative initial space elements.

418 dilations according to F_1 at the surfaces (see Eq. 2) has to emerge. This can only be achieved with
 419 a decreasing growth factor gp . The space expansion algorithms that have been investigated by the
 420 author showed that with the proposed model, GRT compatible space expansion algorithms are feasible.
 421 However, unless the algorithm gets unnaturally complex, occasional inhomogeneities seem to be
 422 unavoidable. In particular at the very small scale, i.e., near the minimal gravitational sources, it
 423 appears to be difficult or impossible to preserve the GRT compatible behaviour.¹⁰

424 *4.2. The propagation of space changes caused by multiple sources*

425 The assumption that space changes start at the minimal sources implies that the aggregation of
 426 space changes from many sources is the normal case. The model of the propagation of space changes
 427 that are caused by multiple sources is based on the single-source propagation (Section 4.1). The
 428 aggregation of the single-source propagations has to be accomplished by a local causal process, i.e.,
 429 by a series of aggregations of neighboring space changes. Only long range, this dynamical process,
 430 can achieve overall gravitational space changes (i.e., curvature changes) that are compatible with the
 431 predictions of GRT and Newtonian dynamics.

432 To simplify the description, in this article, "multiple sources" is initially equated to "two sources".
 433 In simple cases, the treatment of many sources can be performed by a series of two source propagation
 434 processes.

435 For the overall two-source propagation process, three phases can be distinguished:

436

- 437 • Phase-1, the phase where the changes from the two sources propagate independently.
- 438 • Phase-2, the phase where the changes start to overlap and therefore have to be aggregated.
- 438 • Phase-3, the phase where the aggregated changes propagate like single source changes.

¹⁰ The surrender of perfect GRT compatibility at the very small scale may ease the provision of a causal model of the dynamics of QT/QFT (see Section 5) and avoids singularities that occur with the differential equations of GRT.

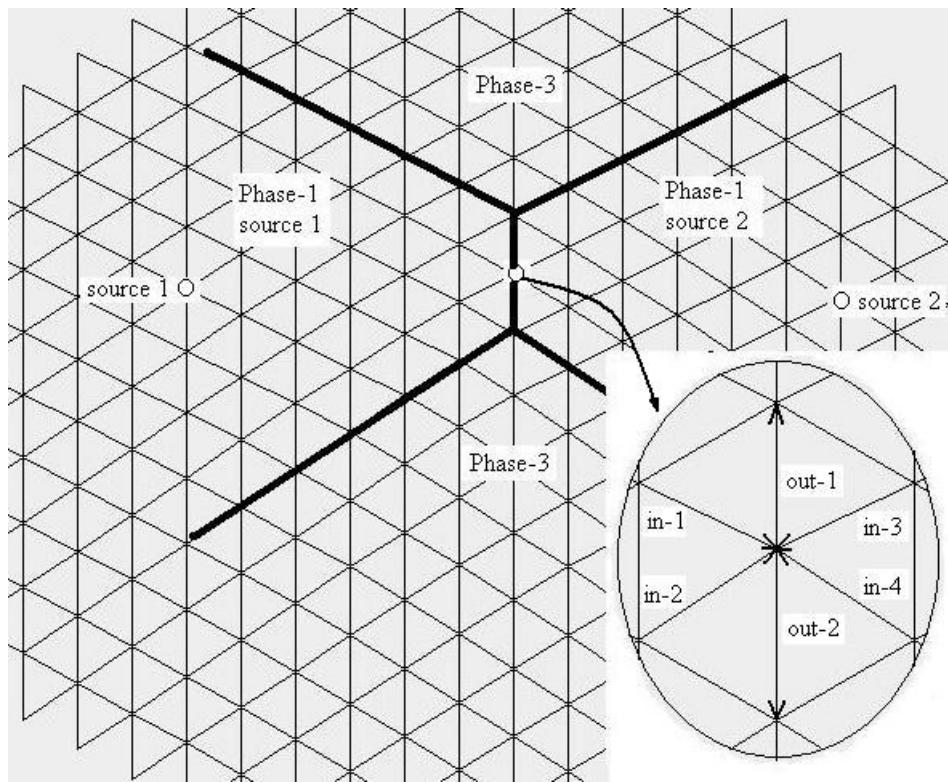


Figure 4. Propagation of space changes caused by 2 sources.

439 Fig. 4 shows an example snapshot in two dimensions, with the areas that are covered by phase-1 and
 440 phase-3 roughly indicated.¹¹

441 A major assumption of the proposed model is that the propagation that occurs at a space point
 442 sp has a definite (consolidated) in-direction and the same (overall) out-direction. The consolidated
 443 in-direction is the vector sum of the multiple in-connections. The overall out-direction is distributed
 444 over the multiple out-connections.

445 4.2.1. Phase-1:

446 The propagation of space changes prior to the points where the changes meet is exactly the single
 447 source propagation described in Section 4.1.

448 4.2.2. Phase-2:

449 When the space changes originating from (two) different sources meet at space point sp, the
 450 changes that arrive from n space point connections ($n \geq 2$) are summarized into a single out-vector.
 451 The out-vector is then distributed to the out-connections (see Fig. 4, the magnifying glass area).
 452 If there are no out-connections left – i.e., if all connections of sp are in-connections – the weakest
 453 in-connection(s) are taken as out-connection(s).

454 4.2.3. Phase-3:

455 After the changes from the multiple sources are summed up, the further common propagation
 456 of the space changes continues like the single-source propagation (Section 4.1). As a special case,

¹¹ Notice that the 2-dimensional representation in Fig. 4 is a simplification which is misleading with certain more detailed considerations.

457 the phase-3 propagation may collide with phase-1 propagation from one of the two sources. With
 458 the proposed model of spacetime dynamics, the collision of space changes is handled like a phase-2
 459 propagation, described above.

460 Compatibility with classical, i.e., Newtonian dynamics evolves during phase-3. The compatibility
 461 with classical dynamics is reflected in mainly the following items:

- 462 1. It is valid to assume an aggregated mass M_{aggr} that represents the aggregation of the masses of
 463 the sources of the space changes.
- 464 2. It is valid and possible to identify a position in space where M_{aggr} is assumed to be located. The
 465 position is usually called the "center of mass".
- 466 3. The (single) aggregated mass M_{aggr} is the sum of the masses of the sources of the space changes.

$$467 M_{aggr} = M_1 + \dots + M_n.$$

468 Only when the propagation of space changes reaches a certain distance r from the center of mass
 469 that the aggregated mass $M_{aggr}(r)$ can be equated to the sum of the masses of the sources.

470 4.2.4. Aggregation of space dynamics from $n \gg 2$ sources

471 The above-described model of the space dynamics aggregation from two sources, with the three
 472 aggregation phases shows that compatibility with classical dynamics will only evolve at the end of
 473 phase-3. Prior to that stage, inhomogeneities, i.e., areas where only a subset of the gravitational source
 474 participates in the aggregation, will occur (and will not disappear during the continued propagation of
 475 space changes). If the aggregation of space dynamics applies to $n \gg 2$ sources, further inhomogeneities
 476 may exist, depending on the distribution of the sources within the space. If the distribution of the
 477 sources establishes gravitational sub-clusters such as solid bodies, planets or stars, where it is possible
 478 to assign an aggregated mass M_{aggr} and a center of mass, the sub-clusters may represent a gravitational
 479 source at the next higher level.

480 5. The dynamics of quantum fields

481 The model that is roughly described in the following is based on three types of work:

- 482 1. The causal model of spacetime dynamics described in Sections 3 and 4 constitutes the base with
 483 respect to the underlying spacetime structure and dynamics.
- 484 2. Further works that influenced the causal model described in the following is known under the
 485 names spin networks (see [17]), spin foam (see [18]) and causal fermion systems (see [19]). The
 486 coupling of the dynamics of space (e.g., the propagation of space changes) with the dynamics
 487 of quantum fields and particles is an idea that has already been pursued with causal fermion
 488 systems.
- 489 3. In [1] and [3] a causal model of QT/QFT is proposed where the physics of QT/QFT is confined
 490 in "quantum objects". For the refinement and an improved foundation of the model described in
 491 [1] and [3], a causal model of spacetime dynamics was felt to be required. The causal model of
 492 spacetime dynamics described in Sections 3 and 4 has been developed with the goal to provide
 493 this.

494 5.1. Mapping of the dynamics of quantum fields to the dynamics of spacetime

495 The refined causal model of QT/QFT can be summarized as follows:

496 A quantum object is a composite object consisting of 1 to n particles. From the external point of
 497 view, i.e., for other quantum objects that may interact with it, the quantum object appears as a
 498 single object because for a certain time span it has associated well-defined, though possibly varying
 499 non-deterministically quantum-object-global attributes.

500 **Definition 2.** $quantumobject := \{$
 501 $globalquantumobjectattributes;$

```

502     particle1,
503     ...
504     particlen;
505 }
```

506 The lifetime of a quantum object, i.e., the time span for which the quantum object may be viewed
507 as an entity with its specific attributes, depends on (1) the internal processes within the quantum object
508 and on (2) possible interactions with other quantum objects (e.g., measurements or scatterings). A
509 (semi-) stable quantum object, i.e., an object with a longer than a minimal lifetime, it can only occur
510 if the internal process that involves the quantum objects particles is a (semi-) stable process, which
511 means a process with a repetitive system state. A (semi-stable) process with a repetitive system state
512 can only be achieved, if the spatial relationships among the components of the quantum object do not
513 vary too much.

514 This leads back to the underlying model of spacetime dynamics. With the model of spacetime
515 dynamics described in Sections 3 and 4, spacetime dynamics starts at the quantum object. This means
516 that the spacetime curvature is maximal near the quantum object and within the quantum object. With
517 the following proposition, a repetitive system state, and thus a semi-stable internal process, and thus a
518 semi-stable quantum object is achievable.

519 **Proposition 4.** *The dynamics of the quantum fields, including the external and internal dynamics of quantum*
520 *objects, is an attachment to the spacetime dynamics described in Sections 3 and 4.*

521 The internal dynamics of quantum objects and the dynamics of interactions between quantum
522 objects are described by paths in space. The paths are comparable to the paths known from QFT, i.e.,
523 the paths of (virtual) particles in position space. Proposition 4 means that the paths of (virtual) particles
524 follow the connections between space points. At each space point reached by the propagating space
525 changes, the paths from the in-connections are joined and subsequently split and distributed to the
526 out-connections. In QFT, the join/split operations are expressed in terms of creation and annihilation
527 operators. There is, however, a significant difference between the creation/annihilation operators of
528 QFT and the join/split operation performed at the space points of the proposed causal model. The
529 operator combination of QFT (normally) applies to three operations (two creates and one annihilate
530 or one create and two annihilate). The join/split operations of the causal model of the dynamics of
531 quantum fields apply to the totality of the n space point connections (e.g., n = 14). The in-connections
532 are all joined together and the split affects all out-connections. To maintain compatibility with the
533 Feynman rules of QFT, the following rule is established for the causal model of spacetime dynamics
534 and QT/QFT:

535 **Proposition 5.** *At most two in-connections and two out-connections may be assigned to (virtual) fermions; the*
536 *remaining connections are assigned to (virtual) bosons.*

537 The utilization of the complete set of in/out connections for the join/split operation on (virtual)
538 particle paths delivers the equivalent to the superposition of paths which in QFT is expressed by the
539 path integral. In standard QFT (see [16]), the path integral is written as

$$540 K(b, a) = \int_a^b e^{(i/\hbar)S[b,a]} Dx(t).$$

541 The discreteness of the model parameters (space, time and paths) may results in slight incompatibilities
542 to standard QFT at large scale. It results in significant incompatibilities at very small scale. The
543 discreteness of the model parameters in conjunction with the *local causal* model eliminates the need for
544 renormalization (if a suitable algorithm for the assignment of in/out connections is applied).

545 5.2. Generalized spin networks

546 With spin networks (see [17]) the connections (i.e., line segments) within the network are attributed
547 by "spin numbers". Special rules define the computation of the spin numbers of out connections as a
548 function of the spin numbers of the in connections. A given spin network thus defines possible paths
549 of state transitions including possible final result states. A spin network is called *closed*, if line segments
550 are all joined at vertices. A line segment (i.e., connection) of the spin network represents the spin of an
551 elementary particle or of a compound system of particles, i.e., of a quantum object.

552 In Section 4, the propagation of spacetime changes is also described in terms of in/out connections
553 of the space points. Also, in the causal model of QT/QFT described in [3], Feynman diagrams are
554 mapped to the in/out connections and to split/join operators as with spin networks. The following
555 generalization of the spin networks is therefore obvious.

556 The "generalized spin network" (GSN), is a network where the connections represent (virtual) particle
557 types. As with the spin networks, the intersections of the line segments (i.e., the vertexes) represent
558 split/join operators and the GSN is called a closed GSN, if line segments are all joined at vertexes.
559 A specific GSN corresponds to a set of 1 to n start particles of specific particle types. For example, a
560 GSN containing two start particles can be associated with QFT scatterings and the pertinent Feynman
561 diagrams. Generally, a GSN can be viewed as the network of Feynman diagrams that are applicable to a
562 specific set of elementary particles. This means, the GSN, like a Feynman diagram, represents possible
563 paths of state transitions. The join/split operators of a GSN specify for a given set of in connections the
564 possible out connections together with the QFT rules for the determination of probability amplitudes.

565 While the proper GSN may be viewed as a tool for determination of the possible alternative
566 state transition paths and the alternative outcomes of a set of particles, it may also be utilized for
567 the determination of the multiple *actual* paths taken in a causal model of QT/QFT. For this purpose,
568 actual paths with a definite (virtual) particle type and related attributes (e.g., spin) and probability
569 amplitudes are assigned to the available connections of the space points reached during the propagation
570 of spacetime changes. If the GSN is a closed GSN and in addition further physical conditions are
571 satisfied, the process of state transitions may result in a repetitive loop until external influences disturb
572 the process. The GSN together with the specific parameter settings then represents a stable composite
573 quantum object.

574 The GSN has much similarity with the spin foam (see [18]).

575 5.3. Collective behaviour

576 One of the objectives of the causal model presented in this article is that the model should be a
577 *local* causal model. The target space-point-locality is damaged by the inclusion of composite quantum
578 objects with object-global attributes (e.g. mass and spin) and instantaneous processes (e.g., collapse of
579 the wave function and entanglement), if it is not possible to break down the formation of the composite
580 objects and the related non-local effects to space-point-local state transitions. In the causal model of
581 QT/QFT described in [2], the non-local effects are explained by the collective behaviour of spacetime
582 elements. Based on the causal model of spacetime dynamics described in Sections 3 and 4 and the
583 concepts of the GSN, the model described in [2] can now be refined as follows.

584 The formation of (semi-) stable quantum objects (elementary as well as composite quantum
585 objects) is a collective behaviour process that is

- 586 1. guided by the applicable closed GSN,
- 587 2. executing in a small area of curved space that represents the kernel of a gravitational source.

588 Guidance by the applicable GSN is generally assumed with QFT processes. In order to create a (semi-)
589 stable quantum object, however, the GSN must be a closed GSN and the system must reach a "repetitive

590 state". A repetitive state is a system state which, for a given GSN, has a high probability to recur.¹² In
 591 general, the probability of the repetitive state can only be high if the spatial relationships, such as the
 592 distances between the involved particles, do not change too much, i.e., if the involved particles are
 593 confined in a small area of space. In the model of spacetime dynamics, where it is assumed that the
 594 changes of space curvature start already at the minimal sources (i.e., at the particles), space curvature
 595 around a set of particles is extremely high, forming a kind of lacuna.

596 As the described collective behaviour process represents a model for the emergence of quantum
 597 objects and the related quantum-object-global attributes, the disturbance of this collective behaviour
 598 process provides a possible model for the instantaneous non-local QT/QFT processes such as particle
 599 decay, the collapse of the wave function, and decoherence. The model which describes the emergence
 600 of a quantum object as a collective behaviour process has much similarity with G. Groessing's proposal
 601 to explain the emergence of a quantum system as a self-organization process (see [20]).

602 *5.4. Example: Scattering in quantum electrodynamics*

603 In quantum electrodynamics (QED), the operator equation for the creation and annihilation of the
 604 field has the form (see [21]):

$$605 H_W(x) = -eN\{(\psi^+ + \psi^-)(A^+ + A^-)(\psi^+ - \psi^-)\}_x$$

606 where ψ^+ , ψ^- , $\bar{\psi}^+$, $\bar{\psi}^-$, A^+ , A^- are the creation and annihilation operators for electron, positron and
 photon. This leads to the eight possible first order Feynman diagrams shown in Fig. 5. For a real

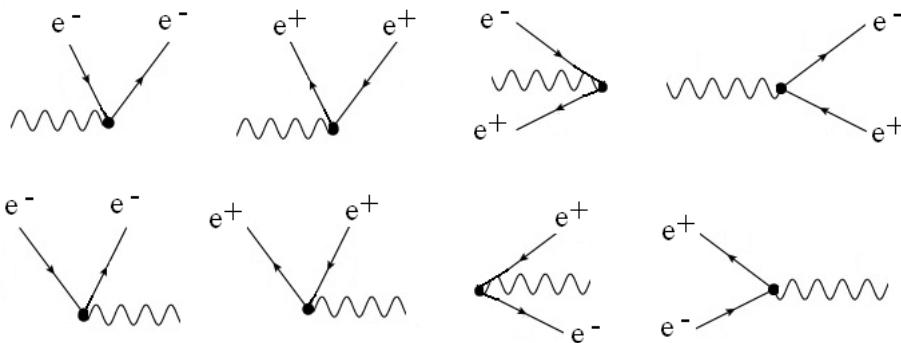


Figure 5. QED first order diagrams.

607 specific QFT scattering process, such as Bhabha scattering ($e^+, e^- \rightarrow e^+, e^-$), the Feynman diagrams
 608 are combinations of the appropriate first order diagrams. For Bhabha scattering this leads to the two
 609 Feynman diagrams shown in Fig. 6.

610 With QFT in position space, the vertexes of the diagrams shown in Fig. 5 and 6 can be associated
 611 with space points. In the proposed model of spacetime, space points have associated connections to
 612 their immediate neighbor space points. As described in Section 5.1, the propagation paths of QFT
 613 (i.e., the lines of the Feynman diagrams) are mapped to the space point connections. As described in
 614 Section 4.1, a typical space point has 14 connections. This enables different strategies for the mapping
 615 of the three lines of the QED Feynman diagrams to the 14 space point connections. In Section 5.1
 616 the overall strategy is described as the preservation of the number of fermion in-connections and
 617 fermion-out connections and the allowance of additional boson connections. This enables the types
 618 of QED space point connections shown in Fig. 7.¹³ The cases that correspond to the QED first
 619 order diagrams shown in Fig. 5 are the cases (1) to (3). Case (4) and case (5) increase the diversity
 620

¹² For a given GSN, there may exist multiple repetitive states and a repetitive state may allow a range of values for specific state components.

¹³ For practical purposes only part of the boson connections are shown in Fig. 7

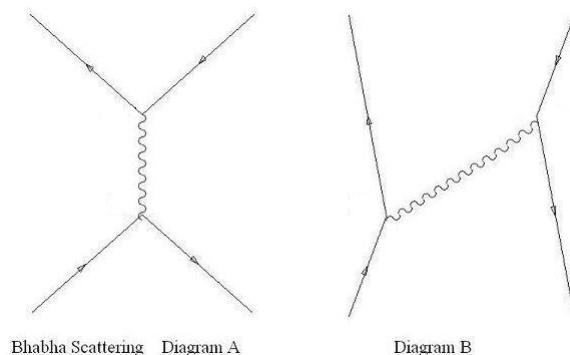


Figure 6. Feynman Diagrams for Bhabha Scattering.

of the possible fermion and boson paths. The more detailed strategy (i.e., algorithm) of the model

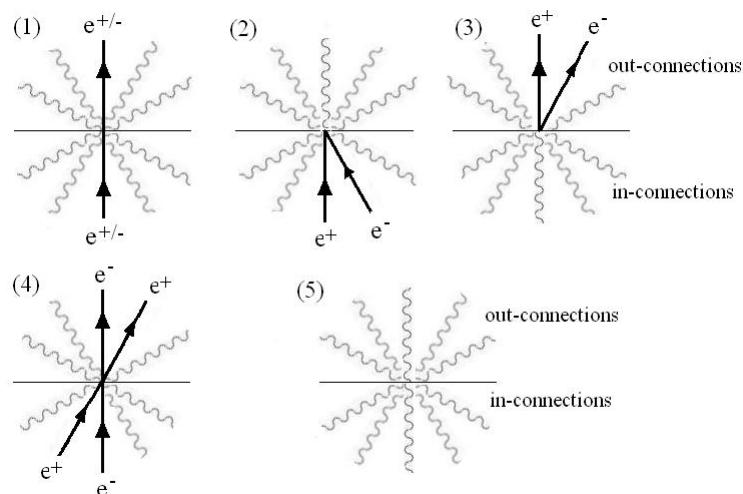


Figure 7. Possible QED connections of a space point.

621 determines (1) which of the connections of the space point are used as out connections, (2) which of
622 the out connections are fermion connections and (3) the distribution of attributes such as momentum
623 among the out connections. The respective algorithm contained in the present model is considered not
624 to be the final algorithm. Further experimentation by use of computer simulations is in progress.
625

626 6. Discussion

6.1. Local causal models. John Bell and David Bohm

The work described in this article is presented in the form of a causal model. The availability of (or at least the feasibility of constructing) a causal model of an area of physics has been requested by the author in many articles (see, for example, [3]). The introduction of the term "local causal model" probably goes back to J. Bell when he formulated his famous Bell inequality and concluded that the refutation of the inequality in experiments prohibits the creation of a local causal model of QT (see [22]). It is probably not wrong to assume that J. Bell was convinced of the necessity of a (local) causal model of QT. This would also explain his admiration of David Bohm (see [23]) whose search for a deterministic model of QT may also be interpreted as the search for a causal model of QT (although a causal model does not necessarily have to be a deterministic model). In [23], J. Bell wrote "I think

637 that conventional formulations of quantum theory, and of quantum field theory in particular, are
638 unprofessionally vague and ambiguous. Professional theoretical physicists ought to be able to do
639 better. Bohm has shown us a way." Although Bells inequality has been refuted in Aspects experiment
640 (see [24]) and Bohm's interpretation of QT did not get many supporters among QT physicists, their
641 work and thinking influences QT physicists still until today with the attempts to overcome the many
642 ambiguities, vaguenesses, and non-localities still contained in QT.

643 The authors attempt to construct a local causal model of QT/QFT (and later of the dynamics of
644 spacetime) resulted in the experience that already, the attempt to construct a local causal model of an
645 area of physics may uncover weaknesses and vaguenesses of a theory (see [9]). In addition, the goal
646 of constructing a local causal model directs the selection of solutions towards specific solutions. For
647 example, the space-time relationship described in Section 3.1. and the Propositions 1, 2 and 3 are all
648 derived from the goal to construct a local causal model.

649 6.2. The special role of time

650 SRT and GRT have taught that space and time are integrated into spacetime. The major reason for
651 taking this view is that in the laws and equations of SRT and GRT, time and space occur in combination,
652 and the causal progression of the system state depends on the progression of the combination of both
653 space and time. The causal model of spacetime dynamics presented in this article also implies a tight
654 relationship of space and time, although with a different interpretation (see Section 3.1).

655 Nevertheless, there are also (good) reasons for not neglecting some fundamental differences
656 between space and time. The major points where the concept of time assumed for the model described
657 deviates from the time concept described (or implied) in some physics literature are:

- 658 • Arrow of time

659 The formal definition of a causal model (in general, not just for the model described in this
660 article) assumes a constant direction in which time progresses, i.e., an arrow of time. Reverse
661 progression of time or variable direction of time progression is just not supported by the model.
662 The author believes that a causal model in general implies an arrow of time. In other words, a
663 model that does not adhere to a unique constant direction of time would show more flexibility
664 than nature shows in reality. The model would not be reality conformal.

- 665 • Time slices

666 With the goal of showing as much commonality as possible between space and time, some
667 physics literature do not describe the extension of the time coordinate as differing from the
668 extension of the space. In the formal definition of a causal model, the laws of physics that specify
669 the state transitions can always access only the system state of the current point in time. It is not
670 possible to access past or future time slices of system states. Models that would allow reference
671 or even modifications of past or future system states are considered as (probably) not reality
672 conformal and would be very complicated.

673 6.3. Time dilation and/or length dilation?

674 Both SRT and GRT predict, under specific circumstances, time dilation and/or length contraction.
675 In textbooks covering SRT and GRT, it is not always clear whether (1) the two effects occur
676 simultaneously, (2) the two effects are just two possible views from a non-local observer, or (3)
677 there are cases where time dilation occurs (but no length contraction) and vice versa. For the proposed
678 model of spacetime dynamics, length dilation is the primary effect. In the model, time dilation - more
679 precisely, the clock rate dilation - is seen as a consequence of the length dilation. Length is a spatial
680 attribute, while clock rate is a property of processes running in a causal subsystem. (In areas of space
681 where there is no causal subsystem, there is no clock rate dilation, nor time dilation.) Despite the basic
682 differences in the roles that time dilation and length dilation play (in the model), these functions are
683 highly interrelated (see Section 3.1).

684 6.4. *The general dependency of the clock rate on the length scaling*

685 The model that assumes that GRT/SRT-based length dilations generally imply, as a secondary
686 effect, a proportional clock rate increase/decrease for the process that executes in the length-dilated
687 area of space requires a further non-trivial assumption. The additional rule is Conjecture 3.1 in Section
688 3.1: "All physical processes can ultimately be broken down to length-related state changes, and changes
689 in the length scaling, therefore, directly result in clock rate dilations of the affected process."
690 If it were possible to identify a process that is not accompanied by some spatial state change¹⁴, and
691 if it were possible to demonstrate that this process nevertheless adheres to GRT/SRT-predicted time
692 dilation, this would prove that the model that assumes that time dilation is always a consequence of
693 length dilation is wrong, or at least that it does not hold generally. The assumption that the rate of
694 state change of a clock process and of arbitrary other processes that show a regular rate of state change
695 depends in a predictable manner on the length scale of the space where the process executes is hard
696 to believe. If the assumption could be confirmed, it would indicate another, even tighter relationship
697 between time and space than is so far assumed with GRT.

698 6.5. *The role of computer simulations*

699 The development of the proposed causal model of spacetime and of QT/QFT has been
700 accompanied by extensive computer simulations. Especially in areas where the causal model requires
701 the determination of suitable algorithms computer simulations have been very useful. Mainly in
702 the following areas the task of determining suitable algorithms has been supported by computer
703 simulations:

- 704 1. The emergence of space from a single source with an increasing density of space points with
705 increasing distance from the gravitational source such that maximum compatibility with GRT is
706 provided (see Section 4.1).
- 707 2. The aggregation of space changes from multiple sources (see Section 4.2).
- 708 3. The assignment of in/out connections and of QFT particle types and particle attributes such that
709 maximum compatibility with QFT is provided (see Section 5.4).

710 In all three areas, the simulations resulted in useful findings.¹⁵

711 7. Conclusion

712 The model of spacetime dynamics and of QT/QFT described in this article does not aim at
713 providing another theory of the subjects. Rather, it has the goal of providing a special model, namely
714 a *causal model*, of these subjects for which a generally agreed upon theories exist. However, it is not
715 possible to derive a causal model of QT/QFT purely from existing QT/QFT. Nor is it possible to derive
716 a causal model of spacetime dynamics purely from GRT. QT/QFT and GRT establish a powerful base
717 for the development of the model, but supplementary statements and interpretations are required to
718 construct a somewhat complete (local) causal model of these areas of physics and their combination.
719 The described causal model is not claimed to be the only possible or valid model of the subjects.
720 Alternative models, possibly focusing on specific aspects, are imaginable. With those features of
721 the model that could not be directly derived from QT/QFT and/or GRT and where, therefore, new
722 solutions had to be invented, it may turn out that the solutions of the present model have to be replaced
723 by solutions that are in accordance with new experiments.

724 The two major items, where the proposed model deviates from the standard interpretations of
725 GRT and QFT are:

14 An example could be the decay of particles.

15 The author does not yet consider the computer simulations as closed. Further computer simulations may result in further improvements.

726 1. The assumption of the length dilation as the primary effect of space curvature that causes clock
727 rate dilation as a secondary effect.
728 2. The assignment of additional bosonic create operators for the out-connections of space points
729 (see Section 5).

730 Disregarding the uncertainties about the ultimate validity of certain details of the proposed model,
731 there are nevertheless a number of findings that the author believes are worth noticing:

732 • For an area of physics, it is mandatory that the construction of models of the complete dynamics
733 is feasible. The type of model that is best suited to describe the complete dynamics is the causal
734 model. The lack of feasibility of constructing a causal model of a theory of physics may be
735 considered as an indication of the incompleteness of the theory.
736 • As SRT and GRT show, space and time have to be viewed as integrated. The progression of time
737 can be described only in connection with spatial state changes. The length scaling within space
738 (including curvature) can only be described with reference to processes executing for a specific
739 time interval. However, besides this fundamental tight relation between space and time, it is also
740 necessary to point out the fundamental differences in the roles, structure, and properties of space
741 and time.

742 Further work is required to refine the model and make the ideas more solid. Dealing with discrete
743 space, time, and paths, refinements of the model may probably be achievable only with the help of
744 computer simulations.

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