

Article

Wear and Friction of Tungsten-based Coatings of Steel under Sliding Contact

Matthew Marko ^{1*}

Naval Air Warfare Center Aircraft Division Joint-Base McGuire-Dix-Lakehurst, Lakehurst NJ 08733, USA ¹

* Correspondence: matthew.marko@navy.mil

Academic Editor: name

Version December 2, 2018 submitted to Entropy

Abstract: An investigation was made to determine the effects of tungsten surface coating on the coefficient of friction of sliding contact between lubricated steel surfaces. The four-ball test was modified, using a tungsten carbide ball bearing in the spindle to cause sliding contact onto three hard steel ball bearings coated with tungsten disulfide lamellar dry lubricant coating, with a coating of grease lubrication applied to the ball bearings. The coatings, loads, speed, and grease level was varied to best understand the impact of different conditions to the friction coefficient.

Keywords: Lubrication, Ball Bearings, Four-Ball, Tungsten Carbide, Grease, Tungsten Disulfide, Coatings, Surface Treatment, Friction

9 Introduction

10 The ability to reduce the coefficient of friction (COF) during sliding contact between two steel
11 surfaces is a capability with countless applications in mechanical engineering design. Often (but not
12 exclusively) friction is desired to be minimized between two surfaces in sliding contact, as friction can
13 cause a reduction in mechanical efficiency, physical and material damage to the surfaces, as well as
14 result in damaging heat from friction energy losses. Metals are unique for having a high non-lubricated
15 friction coefficient, and lubricants including oils, greases, and dry surface coatings [1–13] are often
16 used to reduce the friction during sliding contact.

17 Often in engineering, a hard-steel surface will be coated with tungsten carbide (WC) [14–16],
18 applied as a surface treatment, often using High Velocity Oxygen Fuel (HVOF) to apply the WC
19 coating as described in the standard AMS2448A [17]. The WC coating serves to protect the steel surface.
20 Inherently, WC is harder than steel; it has a Young's modulus of (typically) 500 to 700 GPa, significantly
21 higher than the 200 GPa for steel. With this increased stiffness, there is less expected deformation of
22 the surface, and thus due to the pattern of random asperities within the surface, the true contact area
23 (Figure 1) is reduced. As the friction force is determined as the product of the shear stress and the true
24 contact area [18–21]

$$F = \tau \cdot A, \quad (1)$$

25 the WC coating will reduce the COF marginally due to reduced true contact area. This has been
26 observed in published [22] COF for non-lubricated steel-steel contact (COF = 0.8) versus steel-WC
27 contact (COF = 0.6).

28 The second important surface treatment is the coating of tungsten disulfide WS_2 , a soft lamellar
29 material similar to graphite/ MoS_2 [23–27]. Solid lubrications by lamellar solids is commonly
30 used when liquid lubricants are impractical, such as in clean rooms, vacuum conditions, extreme
31 temperatures, and in outer space. Lamellar solids are defined as solids with a repeating molecular

¹ NAVAIR Public Release 2018-609 Distribution Statement A - "Approved for public release; distribution is unlimited"

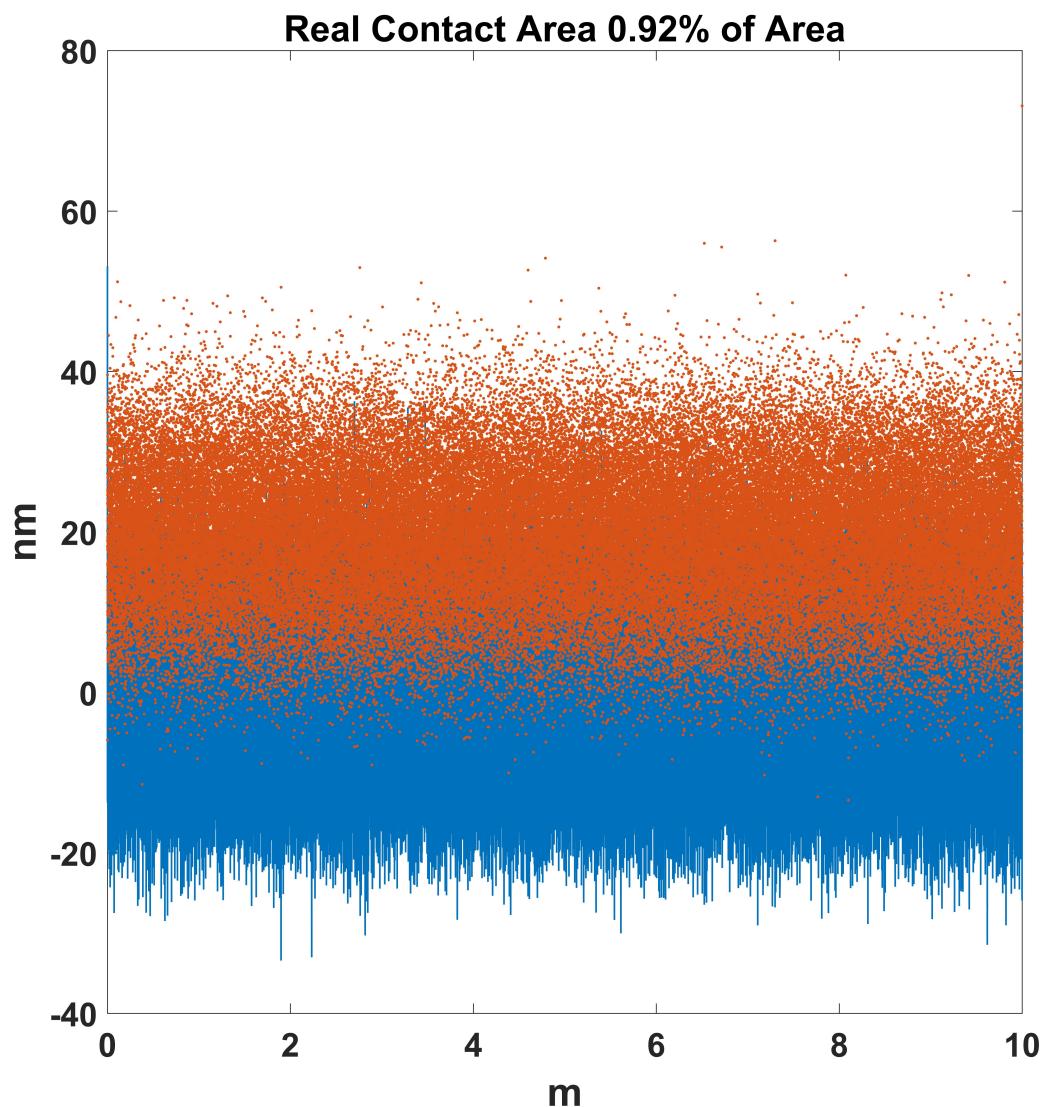


Figure 1. True Contact Area.

32 pattern, effectively sheets of molecules [18]. Because of this structure, they often have anisotropic
33 properties.

34 The most commonly used lamellar solids for solid lubrication are graphite and molybdenum
35 disulfide; tungsten disulfide operates on a very similar principle. One principle of the thin film
36 approach is to have a soft coating separating two hard objects in contact. When two objects are both
37 hard and inflexible, there is inherently little *true contact area*. The true contact area is defined as the
38 actual area of metal-on-metal contact (Figure 1). Even the smoothest surfaces have some asperities
39 and random surface roughness, and with less elastic deformation there is less true metal-on-metal
40 contact. Two hard surfaces in dry contact will have a small true contact area (m^2), but the shear stress
41 τ (Pa) will inherently be higher for hard materials, and thus the friction force $F = A \cdot \tau$ will be high.
42 The opposite of this can happen with a hard object and a soft object; the shear stress is reduced but the
43 true contact area is much higher, and therefore there is a large friction force. By applying a thin film
44 of a soft material, the hard material underneath prevents significant deflection, and thus decreasing
45 the true contact area, all the while the soft film has a low shear stress from sliding contact with a hard
46 metal substance. This low true contact area and low shear stress results in a low friction force, and
47 reduced coefficient of friction.

48 Lamellar solids such as WS_2 are defined as solids with a repeating molecular pattern, effectively
49 sheets of molecules. Because of this structure, they often have anisotropic properties. Other noteworthy
50 characteristics of using lamellar solids are their anisotropic properties; they will easily deform in very
51 low shear stress from the surfaces of contact, yet remain attached to the worn surface. This will allow
52 for low shear stresses during sliding contact, and if the coating is thin and unable to deform much
53 from the worn surfaces, the true contact area will be minimal even with a hard surface sliding against
54 it.

55 Finally, oils and greases are often used as a lubricant as well during sliding contact. Liquid
56 lubricants of varying viscosities serve to coat the metal surfaces, and protect the surfaces by forming a
57 lubricant film [28–30], and only the more-profound asperities can exceed the film thickness height and
58 be worn in metal-on-metal contact. At high enough pressures, the lubricant ceases to be a Newtonian
59 fluid, and the contact enters the elasto-hydrodynamic domain [18,21,31–35], where the viscosity
60 increases dramatically due to pressures, and the surfaces flatten due to high pressures. As a result, a
61 minimum film thickness at the interface can be expected, protecting surface asperities and reducing
62 the true contact area (Figure 1) by protecting the surfaces that do not protrude from the film thickness.
63 Grease has its unique challenges in modeling and predicting the film thickness, as grease is a distinct
64 lubricant that is a solid to semi-fluid mixture of a liquid lubricant and a thickening agent [36].

65 Experimental Approach

66 It is difficult to determine the average COF between two surfaces, and any COF will inherently
67 fluctuate with temperature, load, speed, and random surface asperities. In order to determine the
68 effects of these coatings and grease lubrication for sliding contact, a modified four-ball test will be
69 conducted. The four-ball tester is used for a standard test of lubricants as defined in ASTM D4172 [37]
70 and ASTM D2783 [38] for Extreme Pressure Tests. The four ball test utilizes four 1/2-inch diameter
71 G25 ball bearings [39–42]; three are locked into place in a cup, and the forth is connected to a spindle
72 pressed under a specified load into the 3 lower balls. The lower three balls are coated with the lubricant
73 of interest, which is heated and maintained at a specified temperature. The top ball spins under a
74 specified load, at a specified speed and for a specified duration, until a small circular (typically <1 mm
75 diameter) wear scar appears at the point of contact. The top ball spindle is connected to a load cell to
76 measure the torque, which can determine the friction force and track the COF in real time. The typical
77 settings for the ASTM D4172 are for a load of 40 kg, a speed of 1,200 RPM, a lubricant temperature of
78 74°C, maintained for 60 minutes; this standard is used to compare the wear and friction properties of
79 different lubricants.

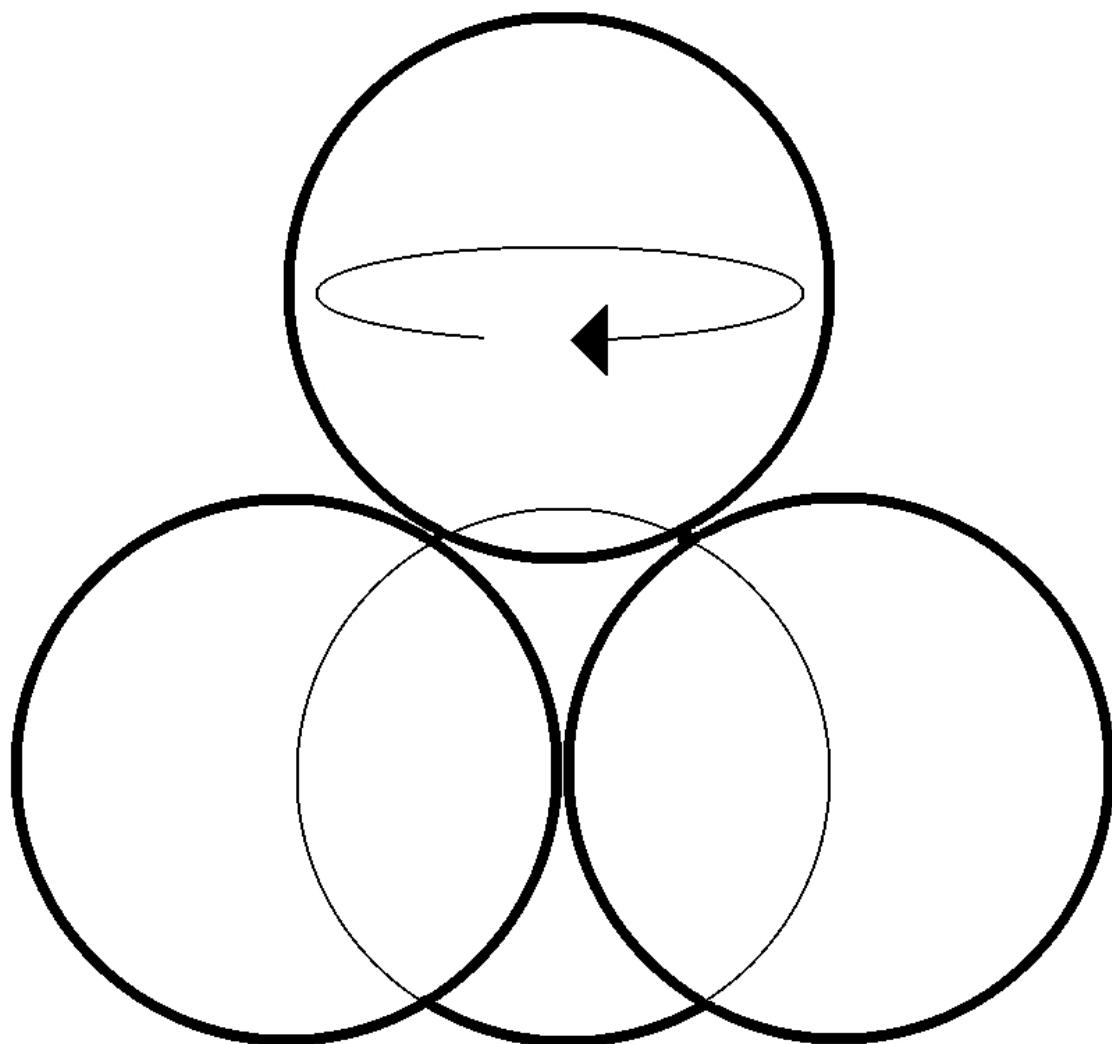


Figure 2. Four-ball configuration, from ASTM D4172 Standard

80 The four-ball test will deviate significantly from the ASTM D4172 standard in order to focus on
 81 tungsten-based lubricants. Of primary interest are the WS₂ coatings; the bottom ball bearings can
 82 easily and inexpensively receive a WS₂ coating; this lamella coating, under the brand name *Dicronite*,
 83 is used as a commercially available solid lubricant, and has an advertised COF of 0.03 tested with an
 84 incline plane test [43]. The steel balls used in the four-ball test have a Rockwell hardness of 64-66.

85 The WC coating, however, has its own unique challenges as the HVOF requires the part subjected
 86 to coating to be held down in place; a unique challenge for a 1/2-inch diameter ball bearing. It could
 87 not be expected that the ball bearings to get an even coating of WC, and therefore ball bearings of G25
 88 quality made of pure WC will be used instead for the top ball in the spindle; these ball bearings will
 89 be supplied by the manufacturer VXB. Because pure WC will inherently be harder than steel, this is
 90 expected to result in a slightly lower COF. Finally, trials of standard hard-steel G25 ball bearings will
 91 also be used to compare the friction changes with and without the WS₂ and / or the WC coatings.

92 The second important consideration is the speed of the test. The friction coefficient is inherently
 93 affected by speed; simplified COF tables will list the *static* and *dynamic* COF and the static will always
 94 be the greater of the two. The impacts from speed are inherently much more complex than simply
 95 static and dynamic, as speed affects both the bonding between surfaces as well as the generation of an
 96 elastic film thickness when there is a lubricant. In general, the friction coefficient is reduced with higher
 97 speeds, as faster speeds often result in thicker lubricant film thickness; this is clearly demonstrated in
 98 the Hamrock Dowson's empirical equation [18,31,36,44-48] for lubricant thickness

$$h_{min} = 3.63R'(U_n^{0.68})(G_n^{0.49})(W_n^{-0.073})(1 - \exp[-0.68\kappa_{ellipse}]), \quad (2)$$

$$h_c = 2.69R'(U_n^{0.67})(G_n^{0.53})(W_n^{-0.067})(1 - 0.61 \cdot \exp[-0.73\kappa_{ellipse}]), \quad (3)$$

$$U_n = \frac{\mu_0 U}{E' R'},$$

$$G_n = \alpha_{PVC} E',$$

$$W_n = \frac{W}{E' R'^2},$$

99 where h_{min} (m) is the minimum film thickness, h_c (m) is the central film thickness, U_n is the
 100 dimensionless speed parameter, G_n is the dimensionless material parameter, W_n is the dimensionless
 101 load parameter, $\kappa_{ellipse}$ is the ellipticity of the contact area, μ_0 (Pa·s) is the dynamic viscosity of the
 102 lubricant at atmospheric pressure, α_{PVC} (Pa⁻¹) is the pressure viscosity coefficient, E' (Pa) is the
 103 reduced Young's modulus, R' (m) is the reduced radius, W (N) is the load, and U (m/s) is the velocity
 104 of sliding contact of the four-ball test

$$U = \frac{1}{2} R \cdot \left(\frac{2\pi}{60} \right) \Omega_{RPM}, \quad (4)$$

105 where Ω_{RPM} is the rotation speed in revolutions per minute (r/min) of the four-ball test, and R (meters)
 106 is the radius of the ball bearing (0.25 inch). It is clear that before the pressure and film thickness profile
 107 can be realized, it is necessary to determine the dynamic viscosity and the minimum film thickness,
 108 so that a proper film thickness function can be realized and the wear rate analyzed. It is clear that as
 109 Ω_{RPM} increases, h_c and h_{min} increase, and thus the COF will decrease. The typical four-ball test is set
 110 to 1,200 RPM, and the maximum speed of most machines is 1,800 RPM. Throughout the test the speeds
 111 will be varied at the ranges of machine speeds, including 200 RPM, 1,200 RPM, and 1,800 RPM (the
 112 range of the machine), to better understand the impact of speed on the friction COF.

113 Next, the estimated pressure can be used to determine a desired load for the four-ball test. This
 114 load is determined with Hertz contact theory [14–16] for elastic deformation, where the average and
 115 maximum pressure of two identical spheres in elastic contact are

$$\begin{aligned} P_{avg} &= \frac{W}{\pi \cdot a^2} \\ P_{max} &= \frac{3}{2} \cdot P_{avg} \end{aligned} \quad (5)$$

116 where W (N) is the load and a (m) represents the radius of the circular region of elastic deformation

$$a = \left(\frac{3 \cdot W \cdot R'}{E'} \right)^{1/3}, \quad (6)$$

117 where R' (m) is the reduced radius

$$R' = \frac{R}{2}, \quad (7)$$

118 which is 0.125 inch for the four-ball test. The value of E' (psi) represents the reduced modulus of
 119 elasticity

$$E' = \frac{E_Y}{1 - p^2}, \quad (8)$$

120 where E_Y is the modulus of elasticity for steel (30,067 ksi) and p is the dimensionless Poisson's Ratio
 121 for steel (0.3); the reduced Young's modulus E' for two steel ball bearings is thus 33,000 ksi. If the
 122 top ball is WC, with a modulus of elasticity of 90,000 ksi and a Poisson's Ratio of 0.31, the reduced
 123 modulus of elasticity is 66,000 ksi.

$$E' = \frac{1}{2} \cdot \frac{E_{Y1}}{1 - p_1^2} + \frac{1}{2} \cdot \frac{E_{Y2}}{1 - p_2^2}, \quad (9)$$

124 If the average pressure is known, the load can be calculated as

$$W = P_{avg}^3 \cdot \left(\frac{2 \cdot R'}{E'} \right)^2 \cdot \pi^3. \quad (10)$$

125 For a four-ball test, the value of W needs to be multiplied by 3 because the load is spread evenly over
 126 all three balls being tested.

127 In general, the friction COF will usually (but not exclusively) decrease modestly with increasing
 128 loads, though overall the friction force still increases with increasing load. This makes physical sense, as
 129 an increase pressure often results (typically) in an elastic smoothing of surface asperities [49–54]. With
 130 a lubricant film thickness separating the two surfaces in elasto-hydrodynamic contact, the equivalent
 131 viscosity increases exponentially with increasing loads, which limits the true contact area, and overall
 132 reduces the increase in shear stress with increasing load.

133 One final source of risk with this test that needs to be recognized and mitigated is the unknown
 134 and random nature of the surface roughness [55–57]. The ASTM D4172 does not have stringent
 135 requirements for the test ball bearing other than a 1/2-inch diameter steel bearing with a Rockwell
 136 Hardness of 64–66 and a bearing quality of G25, which has a surface roughness maximum of 2.0
 137 μ -inch Ra \approx 2.2 μ -inch RMS. Time-controlled four-ball tests have previously been performed [58], with
 138 standard steel ball bearings coated with heavy viscosity mineral oil at both 51°C and 59°C, with a load
 139 of 40 kg, and varying run times of 10 seconds, 1 minute, 2 minutes, 5 minutes, 30 minutes, and 60
 140 minutes. After each test, the ball bearings were cleaned with both acetone and isopropyl alcohol, and
 141 the wear scar was characterized with a Zygo optical profilometer. By deducting the known volume of

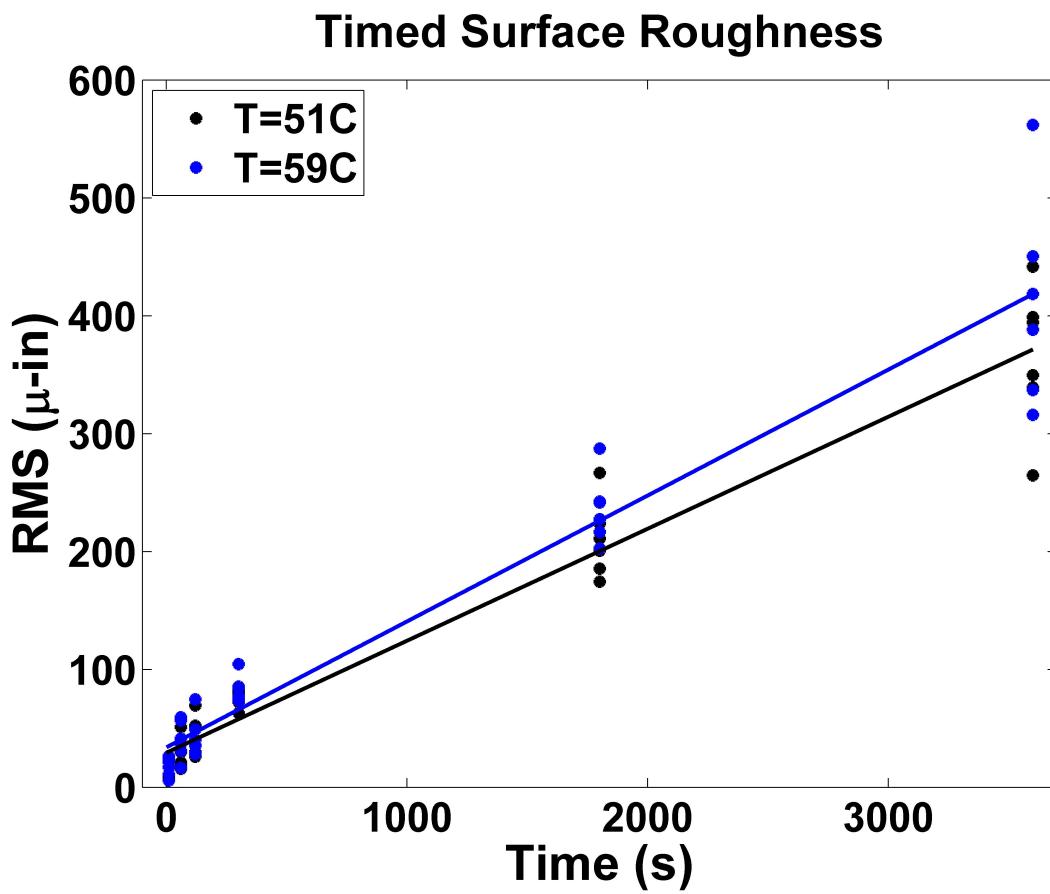


Figure 3. RMS surface roughness (μ -inch) after four-ball test.

142 the 1/2-inch diameter ball bearing, a wear scar surface roughness could be determined. Each time was
 143 tested twice, with each test yielding three test samples, resulting in six sample surface roughness for
 144 each time. Linear trend-lines were generated to determine the increase in surface roughness over time,
 145 and at both temperatures the surface roughness increase is linear.

146 It is clearly observed in Figure with the mineral oil studies that the RMS surface roughness starts
 147 at approximately 2 μ -inch for G25 bearings, and increases to 550 μ -inch. It is also clear in the data that
 148 this increase is linearly proportional to time. The only exception to this is during the first two minutes;
 149 friction and wear rates vary significantly due to the phenomenon of *running-in* [59]. At the conclusion
 150 of every test, the wear scars will be measured with an optical profilometer and the surface roughness
 151 will be recorded, and tests that have a final surface roughness that significantly exceeds the 125 μ -inch
 152 surface roughness will be discarded.

153 **Test Plan**

154 The test was conducted on an Extreme Pressure (EP) Falex four-ball tester (Serial Number:
 155 1100539). Trials of tests were conducted of steel-on-steel, steel-on-WS₂ (coated-steel), WC-on-steel, and
 156 WC-on-WS₂ (coated-steel). When the WC was used, it was a single top ball bearing, frequently used
 157 twice (flipped over). Mobilith SHC 460 PM synthetic grease was consistently used, where some trials
 158 used a light coating of grease; other trials used a heavy amount of grease. The four-ball tester was
 159 configured for three different loads, 13 kg, 47 kg, and 100 kg (practical range of the weights for the
 160 four-ball machine); these loads were achieved with hanging weights and a lever arm. Every test was
 161 run for 900 seconds of duration, and the friction data was consistently recorded with a sampling of

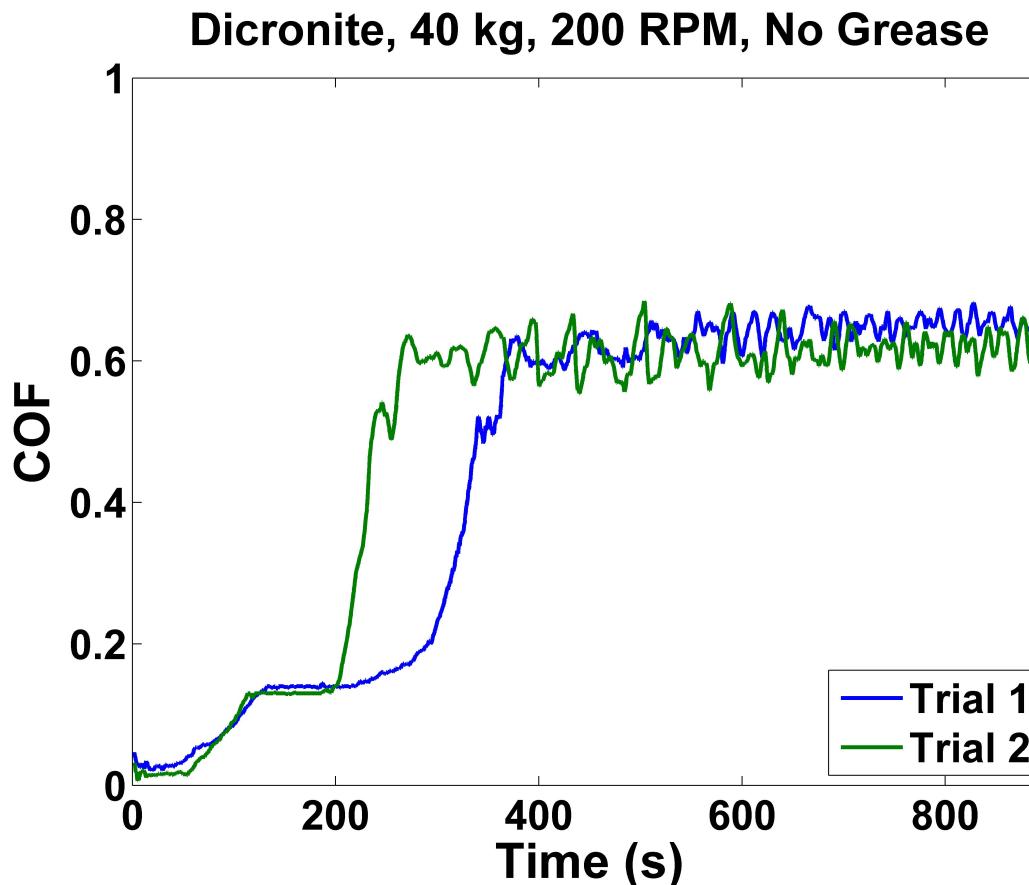


Figure 4. COF of WS₂-on-WS₂

162 approximately 2-3 Hz. Finally, every test was performed at least twice, to ensure the repeatability of
 163 the results.

164 All of the steel ball bearings were soaked for several days in Heptane (C₇H₁₆) to keep them
 165 grease-free. The tungsten carbide balls were cleaned by soaking them in a beaker filled with a mixture
 166 of acetone and isopropyl alcohol, and leaving this beaker in a Branson ultrasonic bath for 20 minutes.
 167 It was observed that the WS₂ coating would visibly appear to come off when the coated ball bearings
 168 were rubbed with either acetone or isopropyl alcohol, so a decision was made not to clean the coated
 169 ball bearings. This allows for the risk of contaminants, but will accurately reflect the conditions of the
 170 WS₂ coating. An effort was made to consistently wear rubber gloves while handling the coated ball
 171 bearings to minimize contamination.

172 At the beginning of the test, one test (using two repeated trials) of four WS₂-coated steel ball
 173 bearings was conducted without any grease lubricant. The published COF utilizing the inclined-plane
 174 method of DOD-L-85645A [43] yielded a typical COF of 0.03 for unlubricated WS₂-on-WS₂ sliding
 175 contact, with a surface roughness no greater than seven μ -inches RMS. This WS₂-on-WS₂ test was
 176 conducted to verify if this result could be obtained with the four-ball set-up, to validate the four-ball
 177 measurements as valid. Two trials were run, with a load of 40 kg and a speed of 200 RPM, with no
 178 grease at all. In both trials, a low COF of approximately 0.03 was observed for the first minute, then
 179 increasing to approximately 0.15 for a few minutes, and finally settling at approximately 0.6 for the
 180 duration of the test. This phenomenon is due to the increase in surface roughness that is inherently
 181 occurring with continued sliding contact. While individual measurements of COF are very noisy and
 182 variable, the lowest average COF over a minute of data collected was 0.0219, observed in the first
 183 minute of trial 2, validating this test as a reasonable representation of the COF of sliding friction.



Heavy Grease (HG)

Light Grease (LG)

Figure 5. HG vs LG

184 It is not typical for the four-ball test set-up to be used with grease; overwhelmingly the test is
185 used to test different liquid lubricants. To study grease, two configurations were used, Light Grease
186 (LG) and Heavy Grease (HG). With LG tests, the ball bearings are fully rubbed with an even coating of
187 grease. With the HG tests, heavy globs of grease are spooned into the specimen container, both below
188 the three balls and fully above it, to ensure the ball bearings are fully immersed in grease at all times.
189 Qualitative observations of the LG specimens after a 15 minute test demonstrate that the balls remain
190 coated with grease, but it is impossible to truly ascertain whether or not the area of contact remains
191 fully coated during the entire test; it is realistic that there are moments of pure metal-on-metal contact.
192 With the HG test, it can safely be assumed continual coverage of the lubricant over the area of contact.



Figure 6. LG after a test, before cleaning

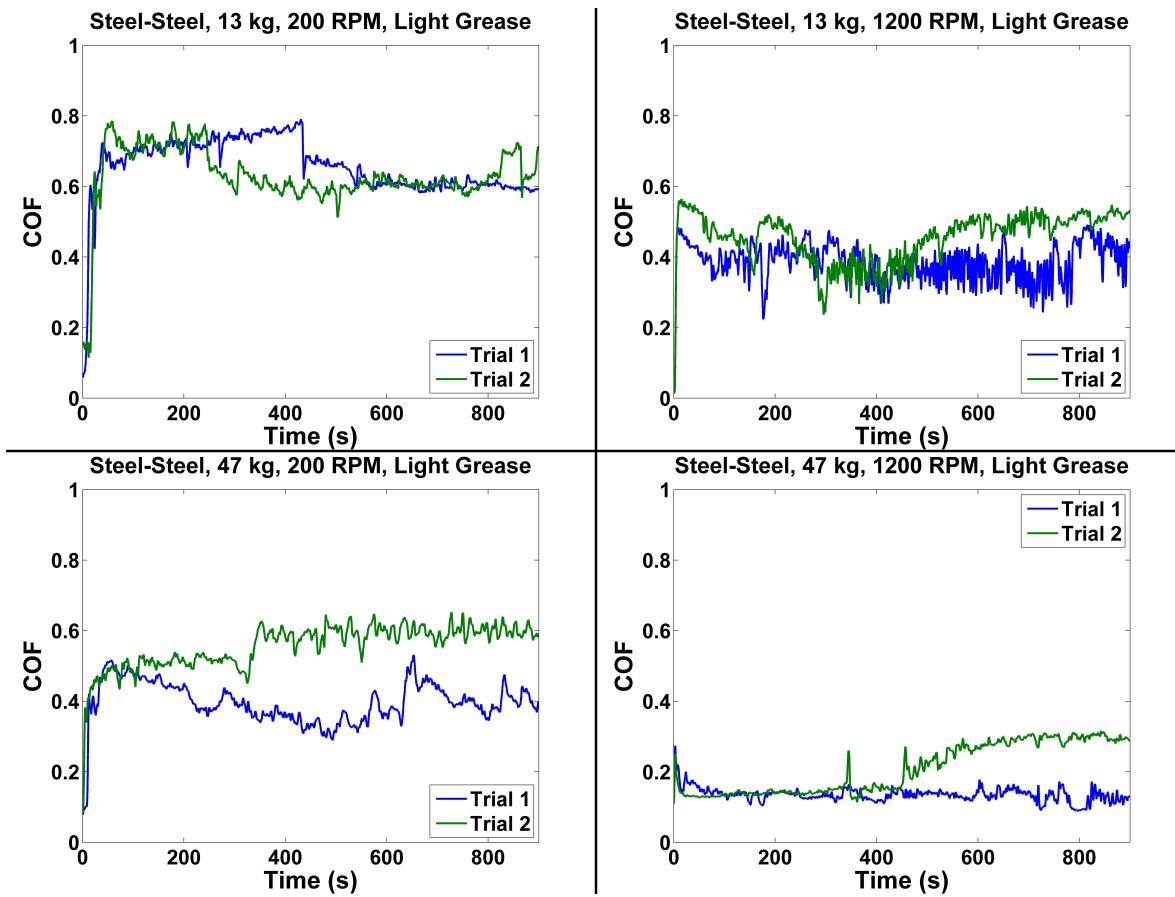


Figure 7. Steel-Steel COF data.

193 Test Results

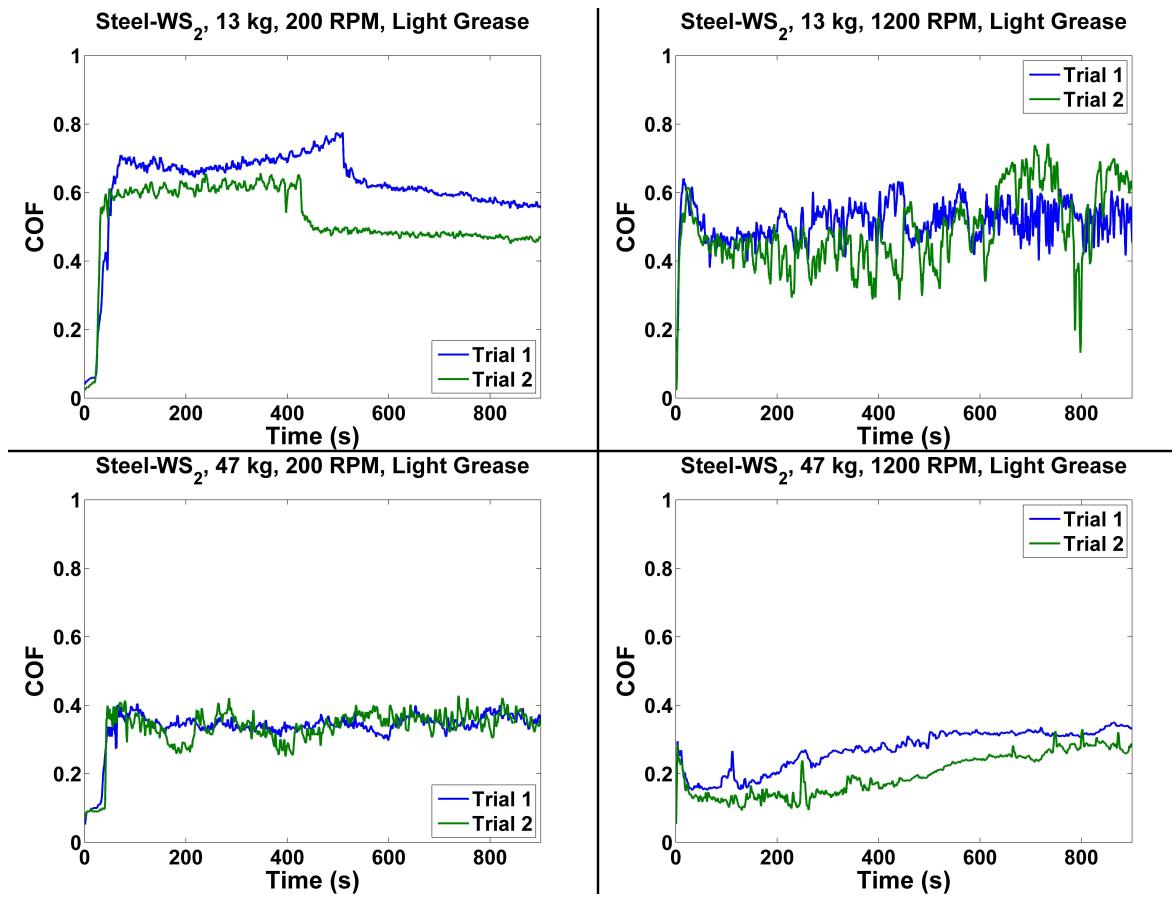
194 Steel-Steel

195 The first series of test utilized the LG configuration steel-on-steel, utilizing the hard steel ball
 196 bearings sold by Falex. The test was conducted for loads of 13 kg and 47 kg, and at speeds of 200
 RPM and 1,200 RPM. The measured friction is tabulated in Table 1. These COF results represent the

Table 1. Measured Friction, Steel-Steel

Grease	Material	Load	Speed	COF	Scar (mm)
LG	Steel-Steel	13 kg	200 RPM	0.5787	1.056166667
LG	Steel-Steel	47 kg	200 RPM	0.3212	0.829333333
LG	Steel-Steel	13 kg	1,200 RPM	0.3307	1.694916667
LG	Steel-Steel	47 kg	1,200 RPM	0.1091	0.984666667

197
 198 minimum average COF over 60 seconds for two 15 minute trials (first 15 seconds are discarded). These
 199 results are usually but not exclusively the first 15 to 75 seconds of the 900 second long test. It is clearly
 200 observed in the data that the COF ratio is observed to decrease (the overall friction force is higher)
 201 with the higher speed and the higher load with all-steel ball bearings.

Figure 8. Steel-WS₂ COF data.202 *Steel-WS₂*

203 The second series of test utilized the LG configuration steel-on-WS₂, utilizing the hard steel ball
 204 bearings sold by Falex on top, and using the hard steel ball bearings sold by Falex and later coated
 205 with *Dicronite* WS₂ as the three ball bearings on the bottom. The test was conducted for loads of 13
 206 kg and 47 kg, and at speeds of 200 RPM and 1,200 RPM. The measured friction is tabulated in Table
 2. Just like with the steel-on-steel configuration, these COF results represent the minimum average

Table 2. Measured Friction, Steel-Steel

Grease	Material	Load	Speed	COF	Scar (mm)
LG	Steel-WS ₂	13 kg	200 RPM	0.4251	1.049916667
LG	Steel-WS ₂	47 kg	200 RPM	0.248	0.818416667
LG	Steel-WS ₂	13 kg	1,200 RPM	0.3068	1.351083333
LG	Steel-WS ₂	47 kg	1,200 RPM	0.1170	1.267166667

207
 208 COF over 60 seconds for two 15 minute trials (first 15 seconds are discarded). These results are usually
 209 but not exclusively the first 15 to 75 seconds of the 900 second long test. It is clearly observed in the
 210 data that the COF ratio is observed to decrease (the overall friction force is higher) with the higher
 211 speed and the higher load with all-steel ball bearings. These results also show an expected decrease in
 212 minimum COF when compared to the same conditions with steel-on-steel, demonstrating that the
 213 WS₂ coating serves to reduce the COF.

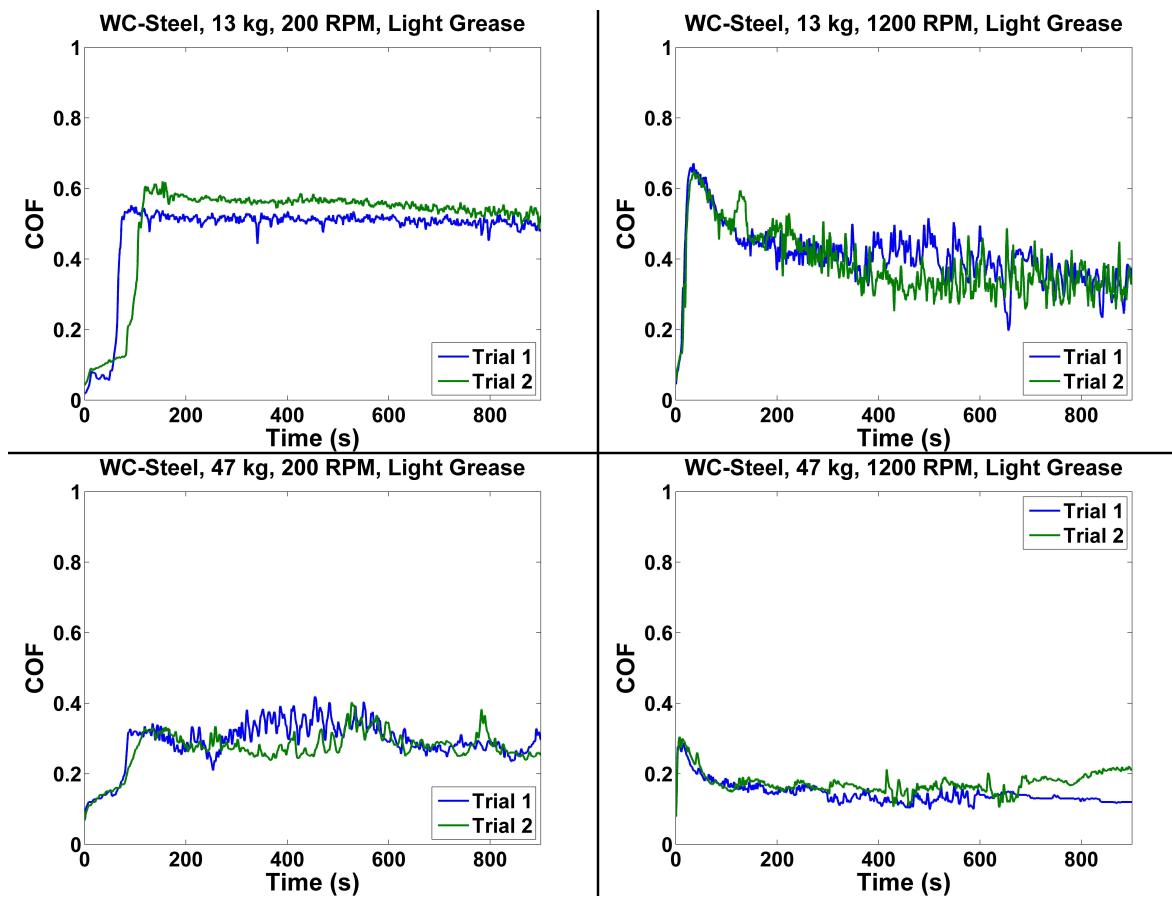


Figure 9. Steel-WC COF data.

214 WC-Steel

215 The third series of test utilized the LG configuration WC-on-steel, utilizing the tungsten carbide
 216 ball bearing sold by VBX on top, and using the hard steel ball bearings sold by Falex on the bottom.
 217 The test was conducted for loads of 13 kg and 47 kg, and at speeds of 200 RPM and 1,200 RPM.
 The measured friction is tabulated in Table 3. Just like with the steel-on-steel and the steel-on-WS₂

Table 3. Measured Friction, Steel-WC

Grease	Material	Load	Speed	Min COF	Min COF (300-900 s)	Scar (mm)
LG	WC-Steel	13 kg	200 RPM	0.1052	0.4950	0.7089
LG	WC-Steel	47 kg	200 RPM	0.1427	0.2532	0.838
LG	WC-Steel	13 kg	1,200 RPM	0.3166	0.3166	1.186
LG	WC-Steel	47 kg	1,200 RPM	0.1176	0.1176	1.1885

218 configuration, these COF results represent the minimum average COF over 60 seconds for two 15
 219 minute trials (first 15 seconds are discarded). It was observed in the 200 RPM cases that the friction
 220 was oddly lower when considering the first 300 seconds; this is believed as due to the lower speed it
 221 will take longer than the initial 15 seconds break-in to have a reasonable amount of wear and surface
 222 roughness at the point of contact; therefore it is observed that for 200 RPM trials the minimum possible
 223 COF is lower than for 1,200 RPM. After 300 seconds of sliding contact, however, it is clearly observed
 224 in the data that the COF ratio is observed to decrease (the overall friction force is higher) with the
 225 higher speed and the higher load with all-steel ball bearings.

227 WC-WS₂

228 The final stage of the LG study involved a tungsten carbide ball in the spindle and three
 229 WS₂-coated steel balls on the bottom. The test was conducted for loads of 13 kg and 47 kg, and
 230 at speeds of 200 RPM and 1,200 RPM; in addition, speeds of 200 RPM and 1,800 RPM were conducted
 for a load of 100 kg. The measured friction is tabulated in Table 4. The phenomenon of a lower COF

Table 4. Measured Friction, WC-WS₂

Grease	Material	Load	Speed	Min COF	Min COF (300-900 s)	Scar (mm)
LG	WC-WS ₂	13 kg	200 RPM	0.0883	0.4075	0.757416667
LG	WC-WS ₂	13 kg	1,200 RPM	0.2189	0.2189	0.740916667
LG	WC-WS ₂	47 kg	200 RPM	0.1355	0.2218	1.21125
LG	WC-WS ₂	47 kg	1,200 RPM	0.1149	0.1149	1.4375
LG	WC-WS ₂	100 kg	200 RPM	0.1983	0.1983	1.004166667
LG	WC-WS ₂	100 kg	1,800 RPM	0.0415	0.0415	1.12225

231
 232 for 200 RPM with loads and speeds has been observed in the WC-WS₂ tests for the 13 kg and 47 kg
 233 studies; same as with the WC-Steel tests; the proper trend of lower COF ratio with increasing load and
 234 speed is observed after 300 seconds of contact, when the WC starts to get sufficient surface roughness.
 235 This is not observed at the 100 kg tests, which has the lowest COF when spun at the high 1,800 RPM
 236 speed.

237 *Heavy Grease* WC-WS₂

238 The friction of sliding contact in the presence of heavy Mobilith SHC 460 grease was also studied
 239 with the tungsten carbide – tungsten disulfide (WC-WS₂) configuration, for loads of 13 kg, 47 kg,
 240 and 100 kg, and for speeds of 200 RPM, 1,200 RPM, and 1,800 RPM. The COF results representing
 241 the minimum average COF over 60 seconds for two 15 minute trials (first 15 seconds are discarded)
 is tabulated in Table 5. It is clear that the minimum COF ratio is significantly less for heavy grease

Table 5. Measured Friction, WC-WS₂, Heavy Grease.

Grease	Material	Load	Speed	Min COF	Scar (mm)
HG	WC-WS ₂	13 kg	200 RPM	0.0201	0.265333333
HG	WC-WS ₂	13 kg	1,200 RPM	0.0301	0.2535
HG	WC-WS ₂	13 kg	1,800 RPM	0.0101	0.3005
HG	WC-WS ₂	47 kg	200 RPM	0.0700	0.419
HG	WC-WS ₂	47 kg	1,200 RPM	0.0692	0.56125
HG	WC-WS ₂	47 kg	1,800 RPM	0.0652	0.67375
HG	WC-WS ₂	100 kg	200 RPM	0.0899	0.461083333
HG	WC-WS ₂	100 kg	1,200 RPM	0.0646	1.0535
HG	WC-WS ₂	100 kg	1,800 RPM	0.0600	0.651

242 than for the light grease trials. Also apparent in the qualitative data is the fact that the COF remains
 243 relatively consistent during the entire trial; the light grease trials all show an increase in friction (or the
 244 friction was high to begin with) from the minimum over time.

246 **Optical Profilometer Measurements**

247 After every test, where the sliding friction ran continuously for 900 seconds, the wear scars were
 248 scanned with optical profilometry. Because of the larger wear scars during the LG testing, it was often
 249 difficult to measure the complete wear scar without stitching as no wide angle lens was available. As
 250 there was no available software to mathematically remove the ball bearing volume and figure out
 251 the true surface roughness, each sample received a single scan at the center of the wear scar, whether

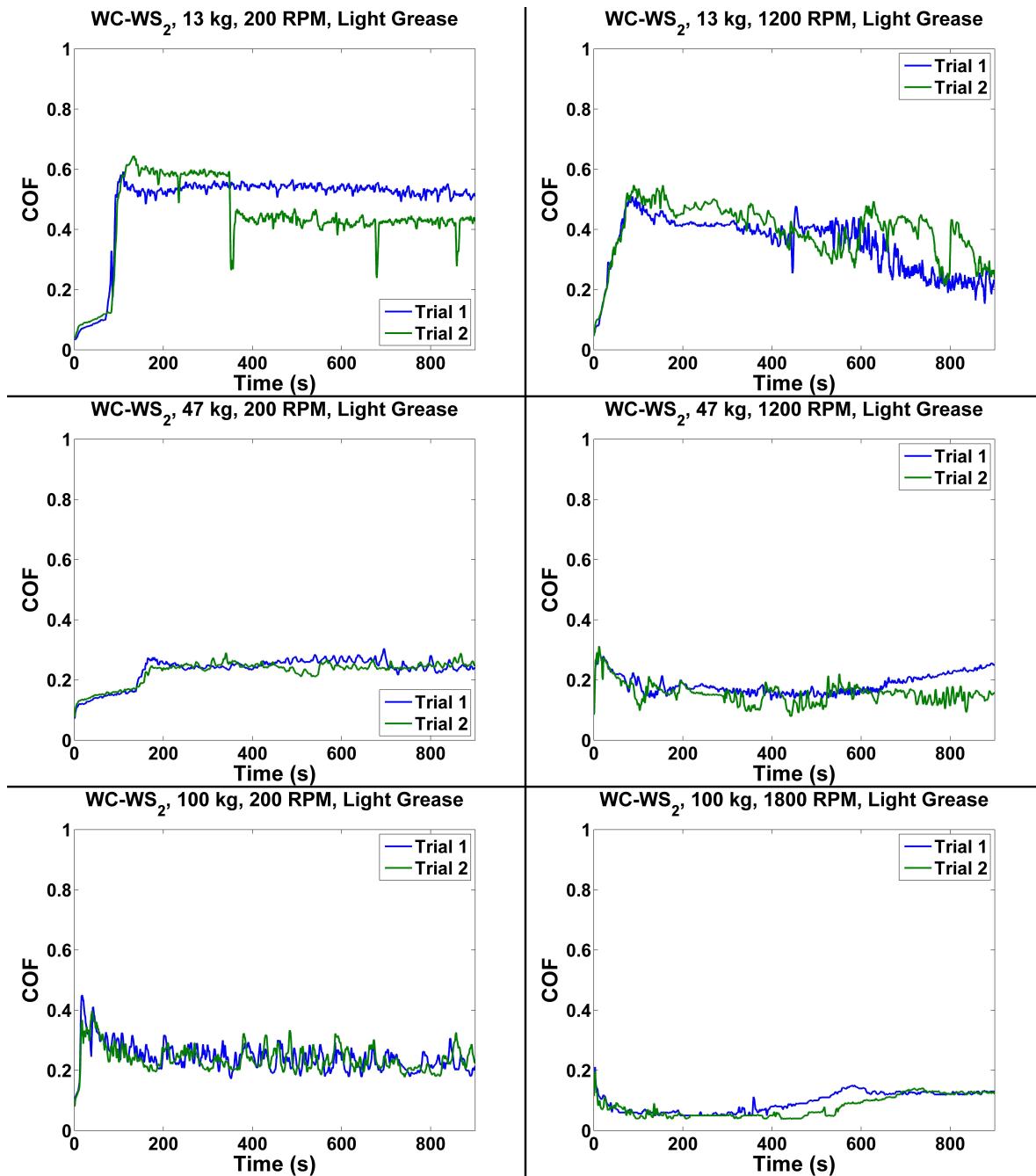


Figure 10. WC-WS₂ COF data.

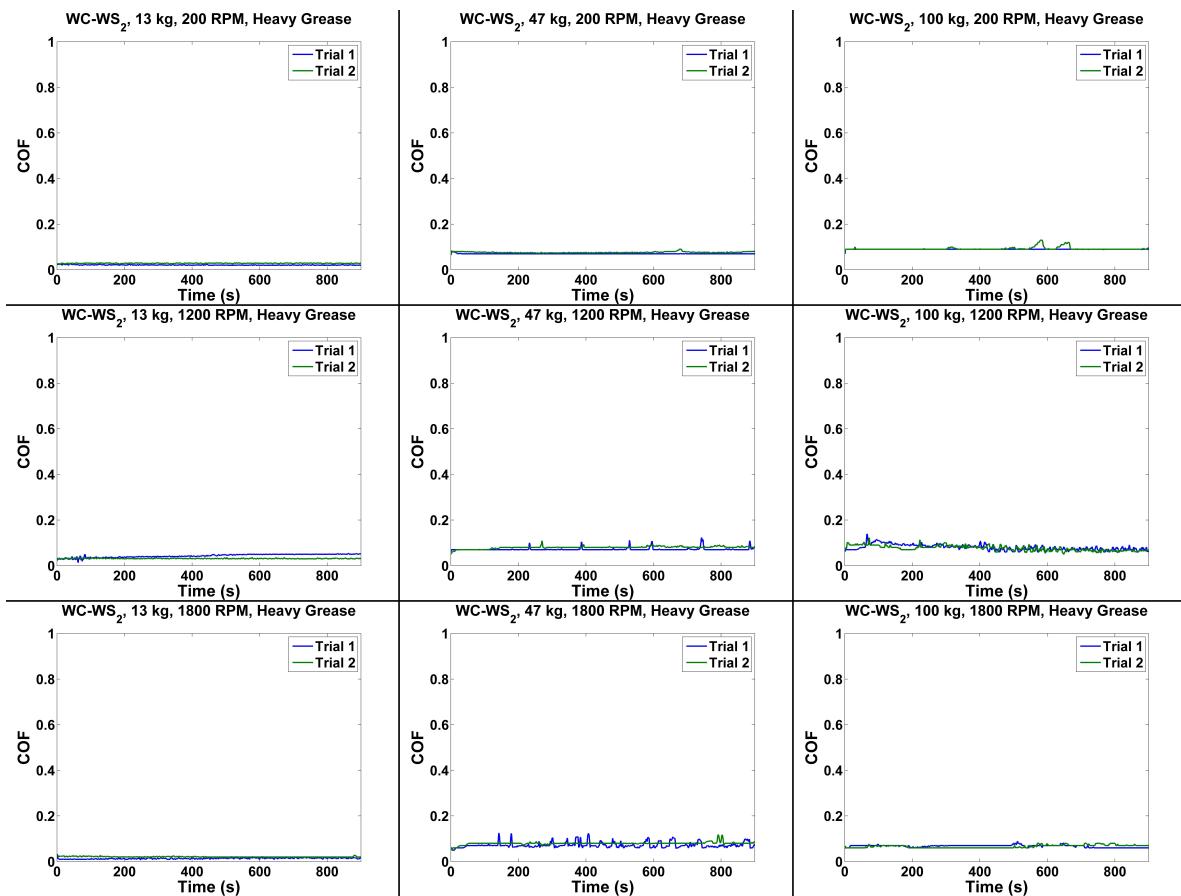


Figure 11. WC-WS₂ Heavy Grease COF data.

252 the entire wear scar was captured or not. While the software was not available to determine the
253 true surface roughness over the entire wear scar, the software did collect the average asperities size
254 over a straight 1D line arbitrarily selected. After each scan, the surface roughness (in μ -inch Ra) was
255 collected over an arbitrary line across the wear scar; the line was adjusted to give the maximum surface
256 roughness possible.

257 The goal of optical profilometry was to confirm that the surface roughness never significantly
258 exceeded 125 RMS (average manufacturing finish); an excessive increase in surface roughness will
259 significantly affect the results. A scan of an arbitrary initial ball bearing showed that the initial surface
260 roughness of the ball bearing without a WS_2 coating to be $Ra = 1.10374 \mu$ -inch, and $Ra = 1.4219 \mu$ -inch
261 for a WS_2 coated ball bearing; both of these surface roughness are even smoother than the required Ra
262 = 2μ -inch required for the G25 bearing standard that is specified for the ASTM D4172 four-ball test.
263 With a total of 67 total four-ball tests (3 balls each for a total of 201 wear scar samples), only 11 had a
264 surface roughness that exceeded $Ra = 113 \mu$ -inch (125 RMS). The average surface roughness was $Ra =$
265 58.24μ -inch, and the median was $Ra = 56.92 \mu$ -inch.

266 Determining the exact impact of surface roughness to the COF measurements is nearly impossible,
267 though obviously a smoother surface will have a lower COF. It is also noticed that overwhelmingly the
268 minimum minute of COF data is usually within the first 15 seconds, when the ball bearing is smoothest;
269 the few examples where this trend is not noticed often have a much higher COF. This experimental
270 data on the wear scar surface roughness serves to demonstrate that, in general, the surface roughness
271 of the ball bearings under test were usually smoother than standard manufactures finish of 125 RMS.

272 Conclusion

273 This effort demonstrated the effectiveness of using both tungsten carbide and tungsten disulfide
274 as a means to reduce the friction during grease-lubricated sliding contact. A parametric study of
275 four ball tests with WS_2 coated steel ball bearings in sliding contact with a pure WC ball bearing was
276 conducted, with Mobilith SHC 460 PM grease. A clear reduction in the minimum coefficient of friction
277 is observed both by switching to tungsten carbide, as well as by using the WS_2 coating. The existence
278 of grease can clearly add to the reduction in friction, but in applications where changing the grease is
279 difficult, the dry coating is a viable alternative. The surface friction was continually tracked and was
280 observed to increase as expected over 15 minutes of run-time. This friction increase was expected to
281 increase with increasing surface roughness from wear; the surface roughness of the samples under
282 test never exceeded an average manufacturer finish of 125 RMS. This effort clearly demonstrated that
283 low friction coefficients under 0.2 are practical with metal in sliding contact and limited grease or oil
284 lubrication.

285 **Acknowledgments:** The authors thank Lou Vocaturo, Kevin Larkins, James McDonnell, Caleb Bonilla, Jeff Ewin,
286 and Jennifer Jensen for useful discussions.

287 **Author Contributions:** M.M. is the sole author of this manuscript.

288 **Conflicts of Interest:** The founding sponsors had no role in the design of the study; in the collection, analyses, or
289 interpretation of data; in the writing of the manuscript, and in the decision to publish the results.

290 Abbreviations

291 The following abbreviations are used in this manuscript:

292 MDPI Multidisciplinary Digital Publishing Institute

DOAJ Directory of open access journals

293 BB Ball Bearing

L_{10} Number of revolutions before 10% chance of failure

COF Coefficient of Friction

294 Bibliography

295 1. Mudhivarthi, S. Dry sliding tribological characteristics of hard, flat materials with low surface roughness. *University of South Florida 2003, Master of Science Thesis*.

296 2. Holmberg, K.; Matthews, A. *Coatings Tribology, Properties, Mechanisms, Techniques and Applications in Surface*
297 *Engineering, Second Edition*; Elsevier: Amsterdam, 2009.

298 3. Wanstrand, O. Wear Resistant Low Friction Coatings for Machine Elements, Possibilities and Limitations. *Uppsala University 2000, PhD Thesis*.

299 4. Erdemir, A.; Donnet, C. Tribology of diamond-like carbon films: recent progress and future prospects. *Journal of Physics D: Applied Physics* **2006**, *39*, 311–327.

300 5. Sullivan, J.; Friedmann, T.; Hjort, K. Diamond and amorphous carbon MEMS. *Materials Research Society*
301 (*MRS Bulletin* **2001**, *26*, 309–311).

302 6. Gupta, B.; Malshe, A.; Bhushan, B.; Subramaniam, V. Friction and wear properties of chemomechanically
303 polished diamond films. *Journal of Tribology* **1994**, *116*, 445–453.

304 7. Miyoshi, K.; Wu, R.; Garscadden, A.; Barnes, P.; Jackson, H. Friction and wear of plasma deposited
305 diamond films. *Journal of Applied Physics* **1993**, *74*, 4446.

306 8. Donnet, C.; Fontaine, J.; Le-Mogne, T.; Belin, M.; Heau, C.; Terrat, J.; Vaux, F.; Pont, G. Diamond-like
307 carbon-based functionally gradient coatings for space tribology. *Surface and Coating Technology* **1999**,
308 *120-121*, 548–554.

309 9. Scharf, T.; Ohlhausen, J.; Tallant, D.; Prasad, S. Mechanisms of friction in diamond-like nanocomposite
310 coatings. *Journal of Applied Physics* **2007**, *101*, 063521–1–063521–11.

311 10. Gardos, M.; Soriano, B. The effect of environment on the tribological properties of polycrystalline diamond
312 films. *Journal of Material Research* **1990**, *5*, 2599–2609.

313 11. Endo, K.; Kotani, S. Observations of Steel Surfaces Under Lubricated Wear. *Wear* **1973**, *26*, 239–251.

314 12. Nanbu, T.; Yasuda, Y.; Ushijima, K.; Watanabe, J.; Zhu, D. Increase of Traction Coefficient due to Surface
315 Microtexture. *Tribology Letters* **2008**, *29*, 105–118. <https://doi.org/10.1007/s11249-007-9287-9>.

316 13. Wong, P.; Huang, P.; Wang, W.; Zhang, Z. Effect of geometry change of rough point contact due to lubricated
317 sliding wear on lubrication. *Tribology Letters* **1998**, *5*, 265–274. <https://doi.org/10.1023/A:1019162212773>.

318 14. Saini, B.; Gupta, V.K. Effect of WC/C PVD coating on fatigue behaviour of case carburized SAE8620 steel. *Surface and Coatings Technology* **2010**, *205*, 511–518. DOI: 10.1016/j.surfcoat.2010.07.022.

319 15. Abad, M.D.; Munoz-Marquez, M.A.; Mrabet, S.E.; Justo, A.; Sanchez-Lopez, J.C. Tailored synthesis of
320 nanostructured WC/aC coatings by dual magnetron sputtering. *Surface and Coatings Technology* **2010**,
321 *204*, 3490–3500. DOI: 10.1016/j.surfcoat.2010.04.019.

322 16. Baragetti, S.; Gerosa, R.; Villa, F. WC/C Coating Protection Effects on 7075-T6 Fatigue Strength in an
323 Aggressive Environment. *Procedia Engineering* **2014**, *74*, 33–36. DOI: 10.1016/j.proeng.2014.06.219.

324 17. International, S. Application of Tungsten Carbide Coatings on Ultra High Strength Steels High Velocity
325 Oxygen / Fuel Process. *SAE International* **2004**, *AMS 2448B*.

326 18. Stachowiak, G.; Batchelor, A. *Engineering Tribology 4th Edition*; Butterworth-Heinemann: Oxford, UK, 2005.

327 19. Hu, Y.; Li, N.; Tønder, K. A Dynamic System Model for Lubricated Sliding Wear and Running-in. *Journal*
328 *of Tribology* **1991**, *113*, 499–505.

329 20. Johnson, K. *Contact Mechanics*; Cambridge University Press: 40 W 20th St, New York NY 10011, 1987.

330 21. Gohar, R. *Elastohydrodynamics*; World Scientific Publishing Company: Singapore, 2002.

331 22. Engineering ToolBox. Friction and Friction Coefficients. https://www.engineeringtoolbox.com/friction-coefficients-d_778.html, 2004. Accessed 16 August 2018.

332 23. Xu, S.; Gao, X.; Hu, M.; Sun, J.; Jiang, D.; Wang, D.; Zhou, F.; Weng, L.; Liu, W. Dependence of atomic
333 oxygen resistance and the tribological properties on microstructures of WS₂ films. *Applied Surface Science*
334 **2014**, *298*, 36–43. DOI: 10.1016/j.apsusc.2014.01.002.

335 24. Xu, S.; Gao, X.; Sun, J.; Hu, M.; Wang, D.; Jiang, D.; Zhou, F.; Weng, L.; Liu, W. Comparative study of
336 moisture corrosion to WS₂ and WS₂/Cu multilayer films. *Surface Coating and Technology* **2014**, *247*, 30–38.
337 DOI: 10.1016/j.surfcoat.2014.03.001.

338 25. Quan, X.; Hu, M.; Gao, X.; Fu, Y.; Weng, L.; Wang, D.; Jiang, D.; Sun, J. Friction and wear performance of
339 dual lubrication systems combining WS₂ – MoS₂ composite film and low volatility oils under vacuum
340 condition. *Tribology International* **2016**, *99*, 57–66. DOI: 10.1016/j.triboint.2016.03.009.

341 342 343 344 345

346 26. Quan, X.; Zhang, S.; Hu, M.; Gao, X.; Jiang, D.; Sun, J. Tribological properties of WS_2/MoS_2 – Ag composite
347 films lubricated with ionic liquids under vacuum conditions. *Tribology International* **2017**, *115*, 389–396.
348 DOI: 10.1016/j.triboint.2017.06.002.

349 27. Maharaj, D.; Bhushan, B. Effect of Mo_2 and WS_2 Nanotubes on Nanofriction and Wear Reduction in Dry
350 and Liquid Environments. *Tribology Letters* **2013**, *49*, 323–339.

351 28. Cann, P.; Spikes, H. In-contact IR spectroscopy of hydrocarbon lubricants. *Tribology Letters* **August 2005**,
352 *19*, 289–297. <https://doi.org/10.1007/s11249-005-7446-4>.

353 29. Jiang, P.; Li, X.M.; Guo, F.; Chen, J. Interferometry Measurement of Spin Effect on Sliding EHL. *Tribology*
354 *Letters* **2009**, *33*, 161–168. <https://doi.org/10.1007/s11249-008-9399-x>.

355 30. Reddyhoff, T.; Spikes, H.A.; Olver, A.V. Compression Heating and Cooling in Elastohydrodynamic
356 Contacts. *Tribology Letters* **2009**, *36*, 69–80. <https://doi.org/10.1007/s11249-009-9461-3>.

357 31. Hamrock, B.; Dowson, D. Isothermal Elastohydrodynamic Lubrication of Point Contacts, III Fully Flooded
358 Results. *NASA Technical Note* **1976**, *D-8317*.

359 32. Ranger, A.; Ettles, C.; Cameron, A. The Solution of the Point Contact Elasto-Hydrodynamic Problem.
360 *Proceedings of the Royal Society of London. Series A, Mathematical and Physical Sciences* **1975**, *346*, 227–244.

361 33. Fillot, N.; Berro, H.; Vergne, P. From Continuous to Molecular Scale in Modelling Elastohydrodynamic
362 Lubrication: Nanoscale Surface Slip Effects on Film Thickness and Friction. *Tribology Letters* **September**
363 **2011**, *43*, 257–266. <https://doi.org/10.1007/s11249-011-9804-8>.

364 34. Guo, F.; Wong, P.L.; Geng, M.; Kaneta, M. Occurrence of Wall Slip in Elastohydrodynamic Lubrication
365 Contacts. *Tribology Letters* **May 2009**, *34*, 103–111. <https://doi.org/10.1007/s11249-009-9414-x>.

366 35. Krupka, I.; Bair, S.; Kumar, P.; Svoboda, P.; Hartl, M. Mechanical Degradation of the Liquid in an Operating
367 EHL Contact. *Tribology Letters* **2011**, *41*, 191–197. <https://doi.org/10.1007/s11249-010-9698-x>.

368 36. Automotive Lubricating Greases. *SAE International* **2005**, *J310*.

369 37. Standard Test Method for Wear Preventive Characteristics of Lubricating Fluid (Four-Ball Method). *ASTM*
370 *International* **2016**, *D4172-94*. DOI: 10.1520/D4172-94R16.

371 38. Standard Test Method for Measurement of Extreme-Pressure Properties of Lubricating Fluids (Four-Ball
372 Method). *ASTM International* **2014**, *D2783-03*(2014). DOI: 10.1520/D2783-03R14.

373 39. Marko, M.D.; Kyle, J.P.; Branson, B.; Terrell, E.J. Tribological Improvements of Dispersed Nano-Diamond
374 Additives in Lubricating Mineral Oil. *Journal of Tribology* **2015**, *137*, 011802.

375 40. Marko, M.D.; Kyle, J.P.; Wang, Y.S.; Branson, B.; Terrell, E.J. Numerical and Experimental Tribological
376 Investigations of Diamond Nanoparticles. *Journal of Tribology* **2016**, *138*(3), 032001.

377 41. Marko, M.; Kyle, J.P.; Wang, Y.S.; Terrell, E.J. Tribological investigations of the load, temperature, and time
378 dependence of wear in sliding contact. *PLOS One* **2017**, *12*. DOI:10.1371/journal.pone.0175198.

379 42. Spanu, C.; Ripa, M.; Ciortan, S. Study of Wear Evolution for a Hydraulic Oil Using a Four-Ball Tester. *The*
380 *Annals of University Dunarea de Jos of Galati* **2008**, *8*, 186–189.

381 43. DOD-L-85645A. Inclined Plane Test Specification: Lubricant, Dry Thin Film, Molecular Bonded. *Military*
382 *Specification* **1988**.

383 44. Hamrock, B.; Dowson, D. Isothermal Elastohydrodynamic Lubrication of Point Contacts, I Theoretical
384 Formulation. *NASA Technical Note* **1975**, *D-8049*.

385 45. Hamrock, B.; Dowson, D. Isothermal Elastohydrodynamic Lubrication of Point Contacts, IV Starvation
386 Results. *NASA Technical Note* **1976**, *D-8318*.

387 46. Dowson, D. Elastohydrodynamic and micro-elastohydrodynamic lubrication. *Wear* **1995**, *190*, 125–138.

388 47. Cameron, A.; Gohar, R. Theoretical and Experimental Studies of the Oil Film in Lubricated Point Contact.
389 *Proceedings of the Royal Society of London. Series A, Mathematical and Physical Sciences* **1966**, *291*, 520–536.

390 48. Archard, J. Contact and Rubbing of Flat Surfaces. *Journal of Applied Physics* **1953**, *24*, 981–988.

391 49. Greenwood, J.; Williamson, J. Contact of Nominally Flat Surfaces. *Proceedings of the Royal Society of London*
392 *A* **1966**, *295*, 300–319.

393 50. Bush, A.; Gibson, R.; Keogh, G. The Limit of Elastic Deformation in the Contact of Rough Surfaces.
394 *Mechanics Research Communication* **1976**, *3*, 169–174.

395 51. Carbone, G. A slightly corrected Greenwood and Williamson model predicts asymptotic linearity between
396 contact area and load. *Journal of the Mechanics and Physics of Solids* **2009**, *57*, 1093–1102.

397 52. McCool, J. Comparison of Models for the Contact of Rough Surfaces. *Wear* **1986**, *107*, 37–60.

398 53. Bush, A.; Gibson, R.; Thomas, T. The Elastic Contact of a Rough Surface. *Wear* **87-111**, *35*, 1975.

399 54. Persson, B. Contact mechanics for randomly rough surfaces. *Surface Science Reports* **2006**, *61*, 201–227.

400 55. Golden, J. The Evolution of Asperity Height Distributions of a Surface Seesoed to Wear. *Wear* **1976**,

401 39, 25–44.

402 56. Bayer, R.; Sirico, J. The Influence of Surface Roughness on Wear. *Wear* **1975**, *35*, 251–260.

403 57. Shafia, M.; Eyre, T. The Effect of Surface Topography on the Wear of Steel. *Wear* **1980**, *61*, 87–100.

404 58. Marko, M. The Tribological Effects of Lubricating Oil Containing Nanometer-Scale Diamond Particles.

405 *Columbia University* **2015**, *PhD Thesis*. DOI: 10.7916/D8FF3R6G.

406 59. Blau, P. On the nature of running-in. *Tribology International* **2005**, *38*, 1007–1012.