

1 **Optimal Microbiome Networks:**
2 **Macroecological Characterization and**
3 **Criticality – Supplementary Information –**

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15 *Keywords:* microbiome, networks, species diversity, abundance, information
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17 Supplementary Table Captions

18 **Table S1. List of top ten abundant species, effect on health, and reference about**
19 **health effects.** The top ten abundant species are reported including their documented ben-
20 efcial, detrimental, unknown isolated effect for the human body. The most relevant reference
21 for these documented effects is reported.

22

23 Supplementary Figure Captions

24 **Figure S1. Abundance trajectories for all species.** The abundance of species is re-
25 ported over time independently of the microbiome state.

26

27 **Figure S2. Exceedance probability of abundance for all species.** The epdf of
28 abundance is plotted for the top 10 highest abundance, mid 10 abundance and top 10 lowest
29 abundance species. A power law is observed for the latter two abundance classes, while an
30 exponential for the former abundance class.

31

32 **Figure S3. Inferred maximum entropy and high-threshold networks.** Maximum
33 entropy microbial networks and high threshold networks are plotted as a function of the mi-
34 crobiome state. Network structure is lost for the transitory and unhealthy microbiome. The
35 color of each node is proportional to the sum of total outgoing TEs of the node (OTE) (the
36 higher OTE, the warmer the color).

37

38 **Figure S4. Top ten most abundant species for each microbiome group.** Abun-
39 dance is reported for the 10 most abundant species of the healthy, transitory and unhealthy
40 microbiome group. For the unhealthy and healthy group the top 10 most abundant species
41 are the most beneficial and detrimental species.

42

43 **Figure S5. Rank-entropy patterns.** The rank of total network entropy and Outgoing
44 Transfer Entropy is plotted in semi-log plots. Many more values of OTE and network entropy
45 are observed for the unhealthy and transitory group.

46

47 **Figure S6. Probability distribution of Outgoing Transfer Entropy.** The top,
48 intermediate and least 10 outgoing information fluxes are plotted considering their probabil-
49 ity distribution functions for the healthy, transitory and unhealthy groups. Spline function
50 fitting of the pdf is shown.

51

52 **Figure S7. Probability distribution of pairwise Transfer Entropy and abun-**
53 **dance.** The pdf for the top, intermediate and least 10 pairwise Transfer Entropy and abun-
54 dance classes are reported as a function of the microbiome group. Spline function fitting of
55 the pdf is shown.

56

57 **Figure S8. Probability distribution of structural and functional microbiome**
58 **networks.** Pdf of structural and functional network degree and distance are shown on the
59 left and right dependent on the microbiome group. Spline function fitting of the pdf is shown.

60

61 **Figure S9. Local species diversity as a function of microbiome network fea-**
62 **tures.** Polynomial functions are used to fit the relationship between macroecological indica-
63 tors and structural network features. Only data are shown for these relationships considering
64 functional network features since no clear fitting function is detected.

65

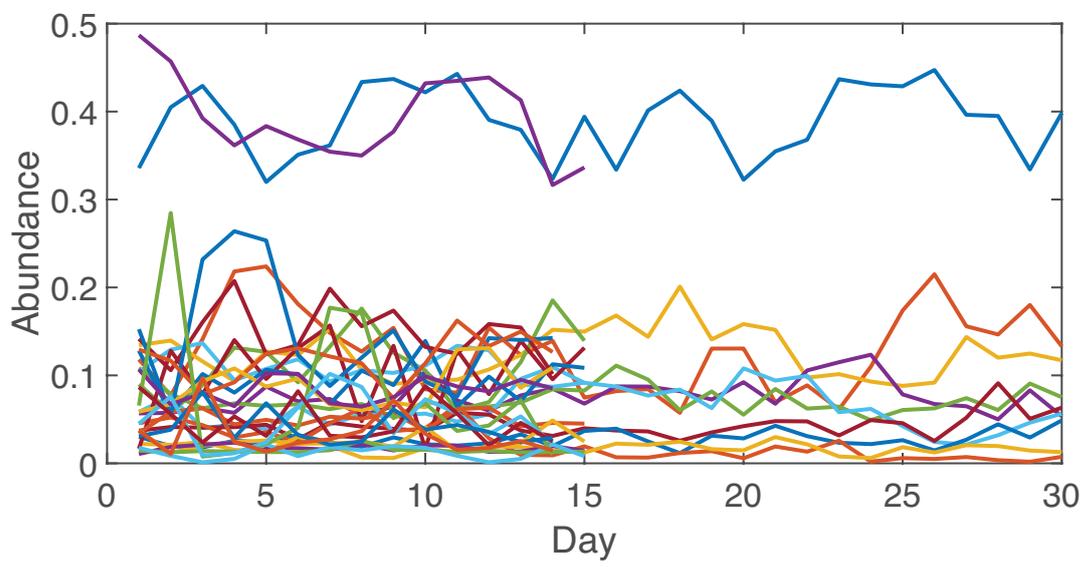


Figure S1:

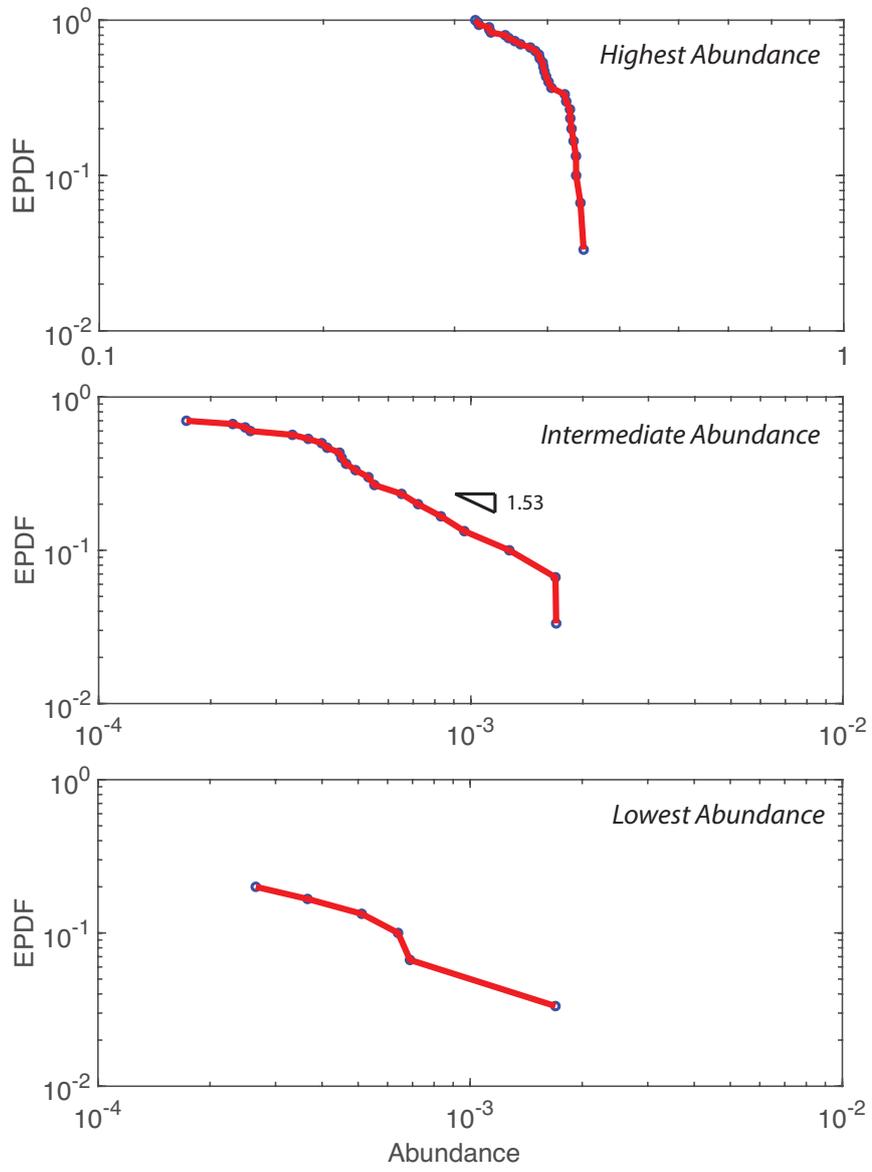


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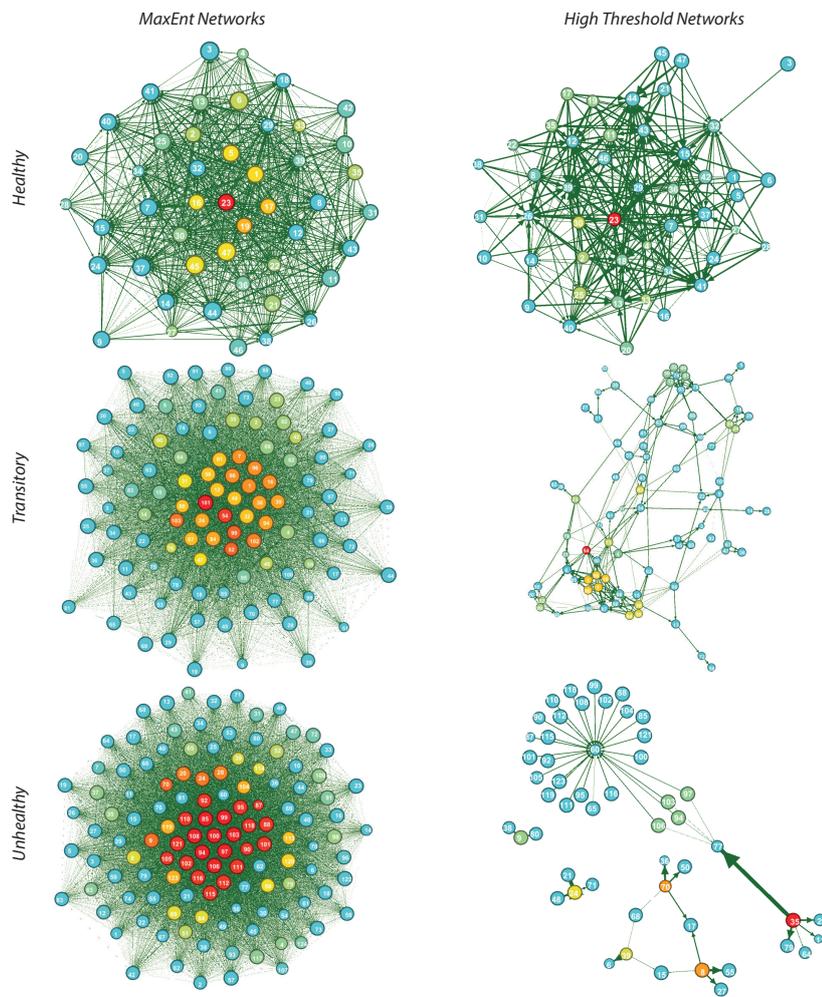


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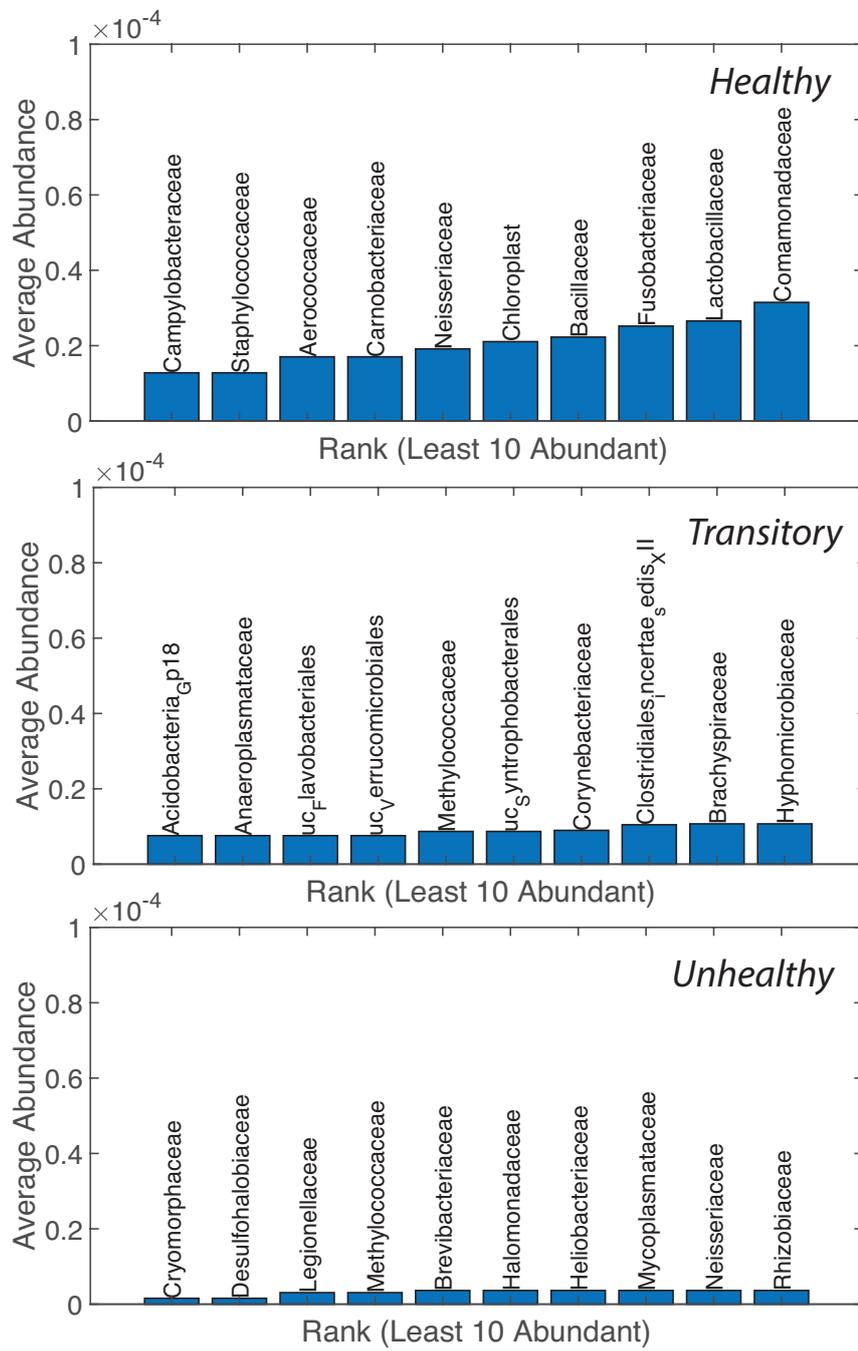


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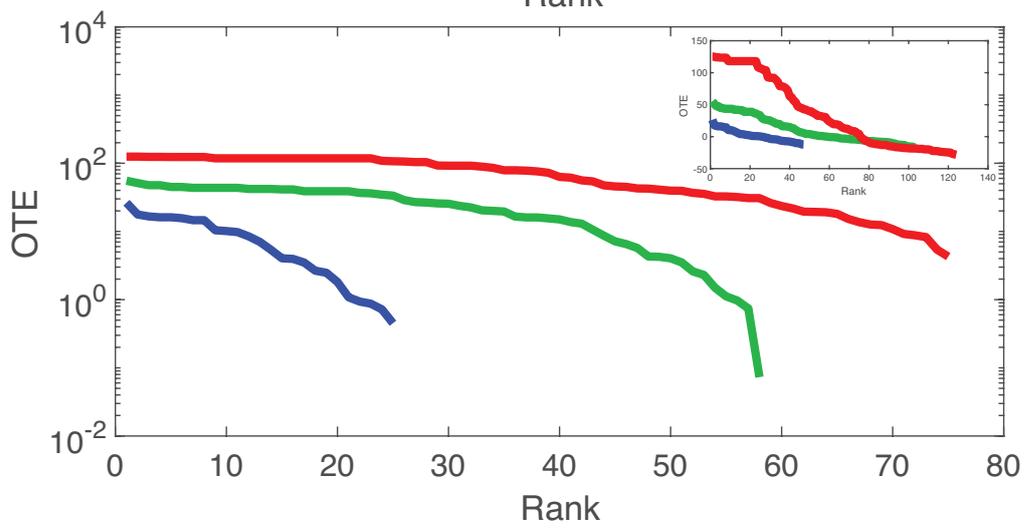
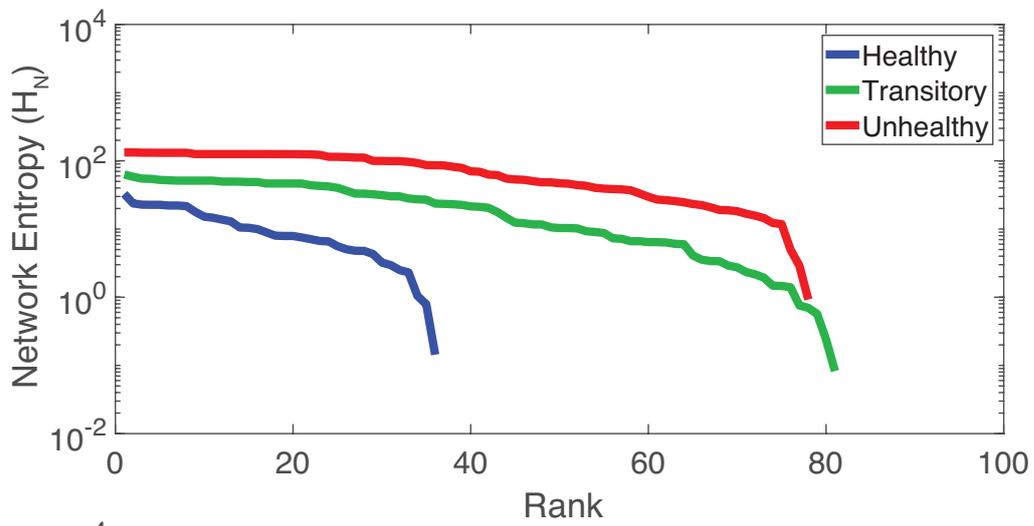


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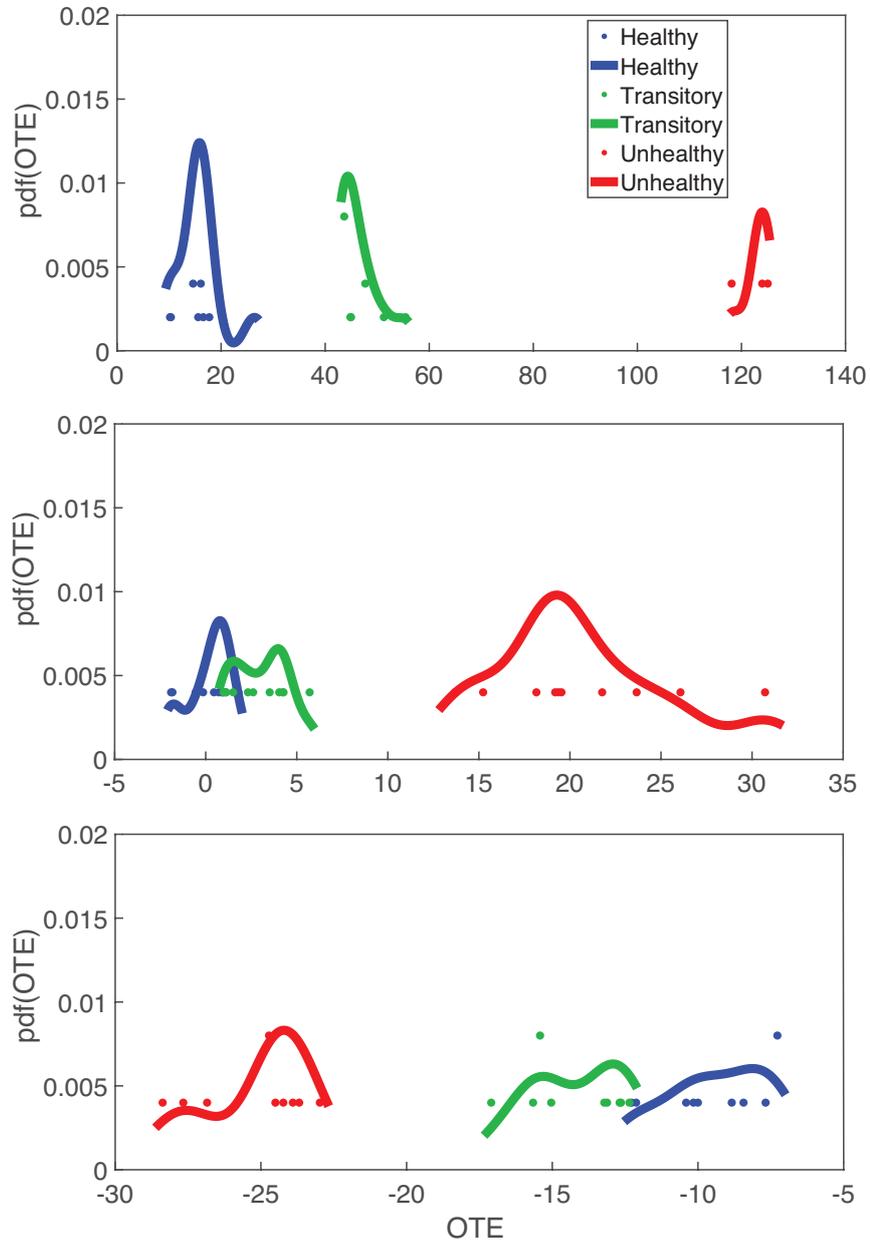


Figure S6:

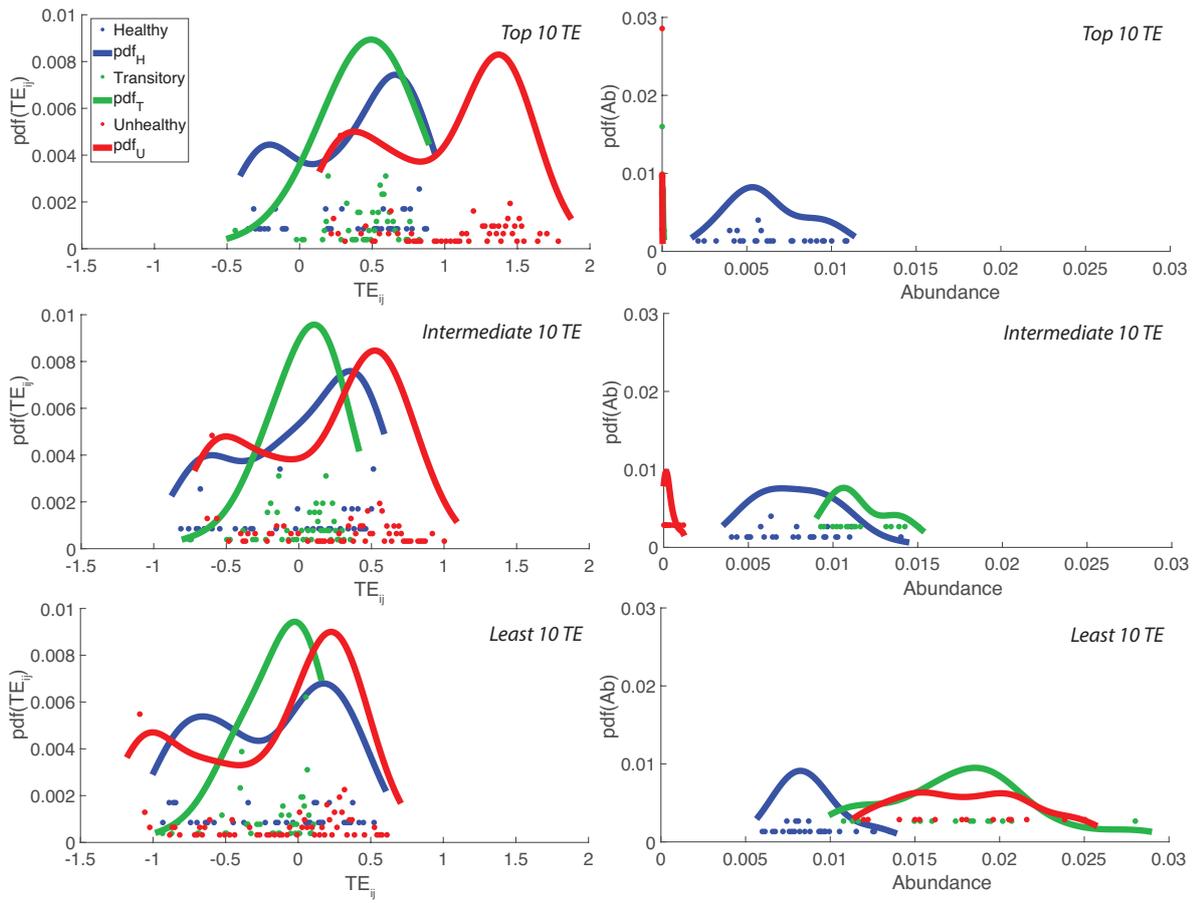


Figure S7:

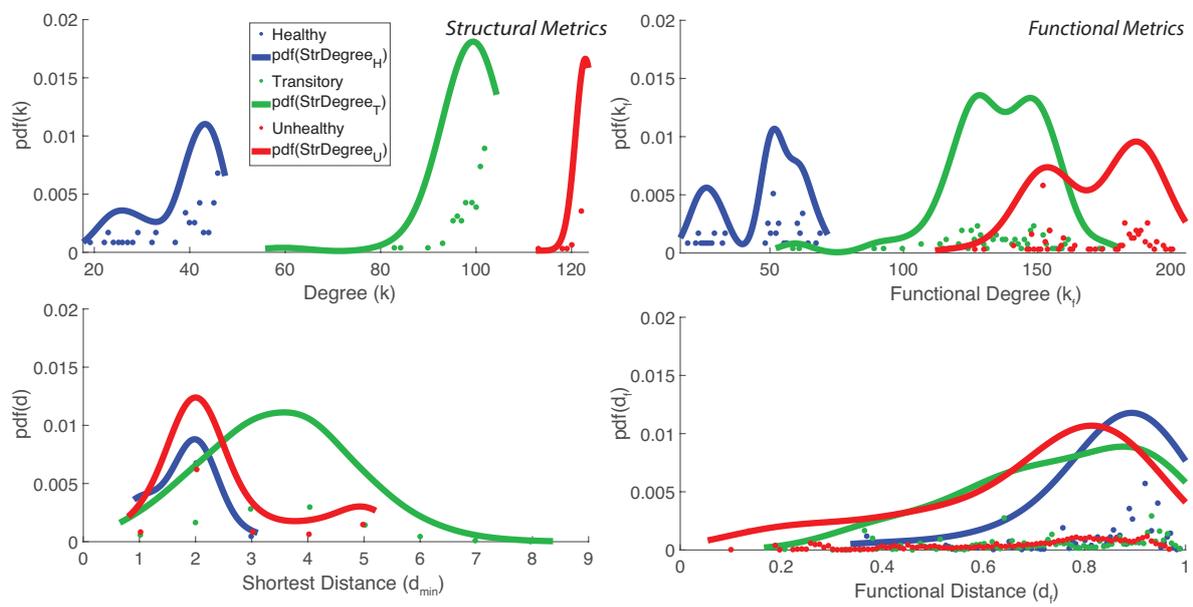


Figure S8:

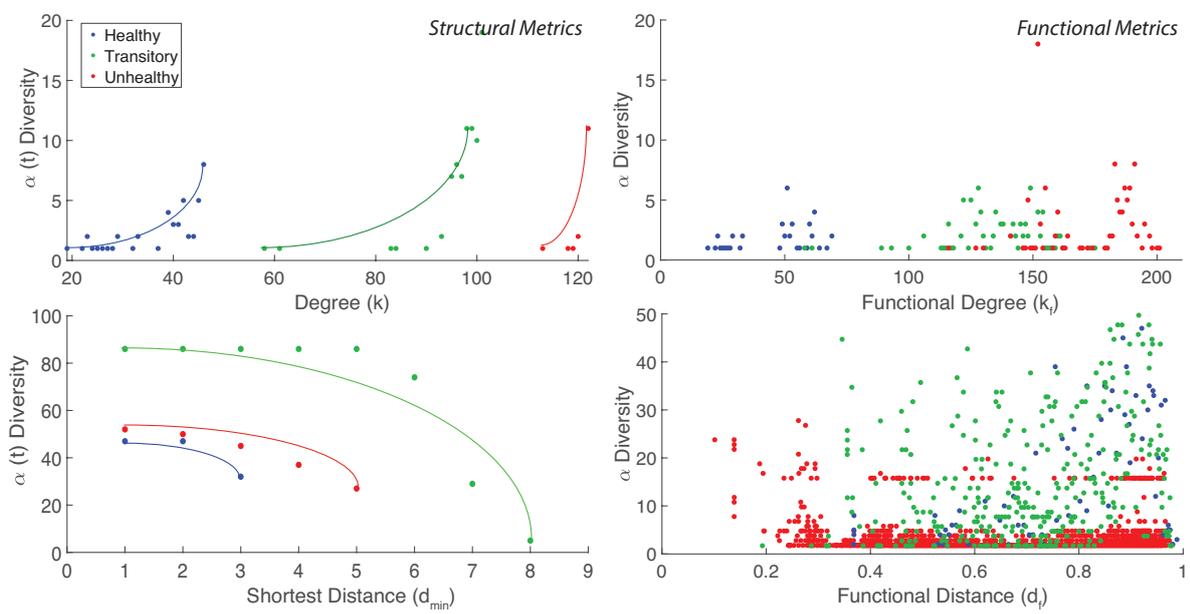


Figure S9: