

Article

# Kinetics of Deformation and Recovery in Quasi-Stationary Deformation of Particle-Hardened Ultrafine-Grained Cu-Zr at $0.5 T_m$ Studied by Load Changes

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**Abstract:** During quasi-stationary tensile deformation of ultrafine-grained Cu-0.2 mass%Zr at 673 K and a deformation rate of about  $10^{-4} \text{ s}^{-1}$  load changes were performed. Relative load reductions by more than about 25% to relative loads  $R < 0.75$  initiate anelastic back flow. Subsequently the creep rate turns positive again and goes through a relative maximum. This is interpreted by a strain rate contribution  $\dot{\epsilon}^-$  from recovery of dislocations. Back extrapolation indicates that  $\dot{\epsilon}^-$  contributes about  $(20 \pm 10)\%$  to the quasi-stationary strain rate. The stress dependences of the recovery-strain rate  $\dot{\epsilon}^-$  and the rate  $\dot{\epsilon}^+$  related with generation and storage of dislocations are discussed in terms of thermally activated processes characterized by different kinetics.

**Keywords:** Cu-Zr; ECAP; ultrafine-grained; deformation; dynamic recovery; transient; load change tests

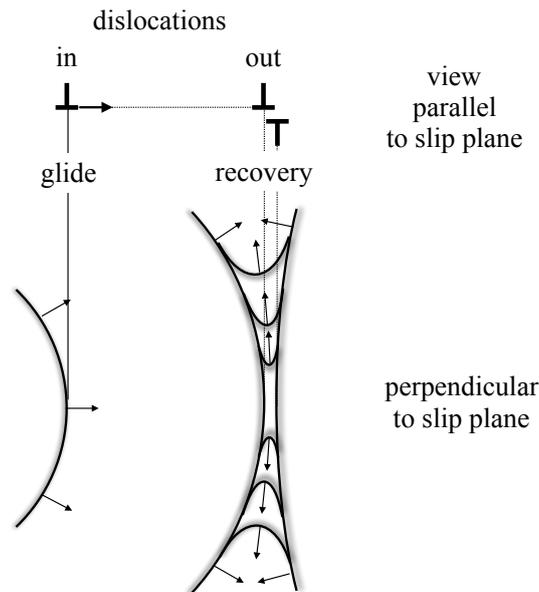
## 1. Introduction

In a companion paper the quasi-stationary (qs) deformation strength of ultrafine-grained Cu-Zr has been described. In qs deformation storage and recovery of dislocations approximately balance each other so that the dislocation density  $\rho$  remains approximately constant, *i.e.*

$$\dot{\rho}^+ \approx \dot{\rho}^- \quad (1)$$

Storage occurs after expansion of dislocation loops on slip planes (Fig. 1: 'dislocations in'). Dynamic recovery is coagulation of dislocation loops after dipole capture (Fig. 1: 'dislocations out'). The recovery processes may be spatially concentrated at (cell, low-angle, high-angle) boundaries or may be more equally distributed as in solid solutions of class I-type with solute drag on dislocations [1,2]. Recovery generally requires dislocation motion outside the primary slip plane by climb or cross slip [3].

In the view in a direction parallel to the glide plane, where dislocations appear as points (Fig. 1), recovery seems to make a negligible contribution to strain during annihilation of dislocation dipoles. Therefore dynamic recovery is usually not considered as a process generating strain. Rather, the models regard strain as a result of thermally activated expansion of slipped areas bounded by dislocation lines with positive curvature that have to overcome a significant athermal stress component (forest dislocations, long-range back stresses from boundaries). In this picture the existing dislocations act as *obstacles* to dislocation glide. However, the view in direction perpendicular to the slip plane shows



**Figure 1.** Scheme of dislocation glide with generation and storage of dislocations ('dislocations in') and dynamic recovery of dislocations ('dislocations out') viewed perpendicular and parallel to glide plane.

that strain may well be generated during the process of coagulation of dislocation loops in recovery as negatively curved dislocation segments straighten [4,5]. Here the interaction of dislocations *supports* the expansion of slipped areas by glide rather than opposing it. The difference in driving forces means that the kinetics of generation of dislocation length by glide of positively curved dislocations moving through the existing dislocation structure differs from that of decrease of dislocation length by motion of negatively curved dislocations. Therefore it makes sense to treat the rate  $\dot{\epsilon}_{pl}$  of plastic deformation as sum of storage strain occurring at a rate  $\dot{\epsilon}^+$  and recovery-strain occurring at a rate  $\dot{\epsilon}^-$  [4,5]:

$$\dot{\epsilon}_{pl} = \dot{\epsilon}^+ + \dot{\epsilon}^- . \quad (2)$$

In the literature there is a couple of examples of processes of type  $\dot{\epsilon}^-$ , where recovery is coupled with glide or glide is associated with recovery (class I alloys with viscously moving dislocations [1,2,6], knitting-out of dislocations from low-angle subgrain boundaries [7–9], accommodation processes at high-angle boundaries [10], strain coupled with migration of low-angle (*e.g.*[11]) and high-angle (*e.g.*[12]) boundaries. But compared to  $\dot{\epsilon}^+$  the recovery-strain rate  $\dot{\epsilon}^-$  has received little attention (see *e.g.* [3,13]). In monotonic qs deformation the two terms  $\dot{\epsilon}^+$  and  $\dot{\epsilon}^-$  are coupled via condition Eq. (1). To investigate recovery of dislocation lines separately from storage of dislocations, one must decouple the two processes. This can be done by a sudden change of the force  $F$  at which the specimen deforms. Such a perturbation abruptly changes the forces exerted per length of dislocations and triggers reversible time-dependent dislocation motions (*e.g.* bowing/unbowing). The strains caused by those motions are called anelastic. So the total inelastic strain rate is

$$\dot{\epsilon}_{inel} = \dot{\epsilon}_{pl} + \dot{\epsilon}_{anel} . \quad (3)$$

17 Figure 2 schematically shows the response to a change from  $F_0$  to  $F_r \equiv R F_0$  at a time  $t_0$  and an inelastic  
 18 strain  $\epsilon_{r,0}$ . Consider relatively small changes of the relative load  $R$  (cases a and b in Fig. 2). These cause  
 19 relatively small changes in inelastic deformation rates from the value  $\dot{\epsilon}_{r,0}$  before the  $R$ -change to a new  
 20 value  $\dot{\epsilon}_{r,1}$ . Anelastic strains are negligible. Just after the  $R$ -change, the dislocation structure and the  
 21 rest of the microstructure are virtually the same as before ('constant structure'), but the glide velocity  
 22 of dislocations has changed due to the change of the stresses acting on the dislocations. The ratio  
 23  $\dot{\epsilon}_{r,1}/\dot{\epsilon}_{r,0}$  is widely used to get a measure of the activation volume  $V^+$  of thermally activated dislocation

24 glide as described in more detail in section B. A particularly large body of 'constant structure' data of  
 25  $\dot{\epsilon}_{r,1}/\dot{\epsilon}_{r,0}$  has been collected for various metals and alloys by Milička in stress change tests during creep  
 26 at elevated temperatures [14–16].

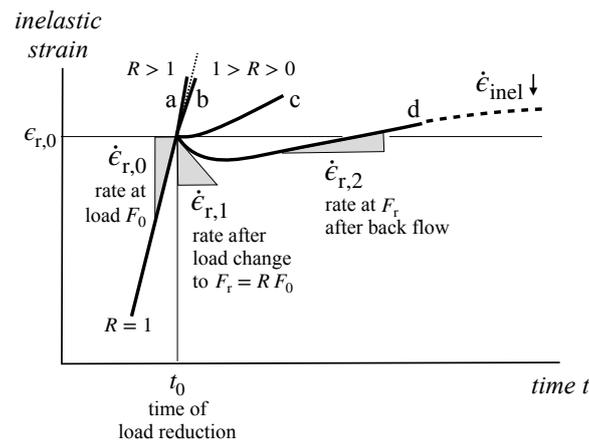
27 Now we consider relatively large  $F$ -changes (cases c and d in Fig. 2). Anelastic strains are no  
 28 longer negligible and diminish  $\dot{\epsilon}_{inel}$  compared to  $\dot{\epsilon}_{pl}$  (Eq. (3)). At sufficiently low  $R$  the forces acting on  
 29 the dislocations initially get negative so that  $\dot{\epsilon}_{inel}$  becomes negative directly after the  $R$ -reduction [17].  
 30 This is a consequence of internal stresses of short- and long-range nature acting on the dislocations  
 31 [17] and opposing thermally activated glide of type  $\dot{\epsilon}^+$ . As the back flow relaxes the internal back  
 32 stresses created before the  $R$ -reduction, the absolute magnitude of the rate  $\dot{\epsilon}_{anel}$  declines,  $\dot{\epsilon}_{pl}$  becomes  
 33 dominant again, and forward deformation is reestablished at a rate  $\dot{\epsilon}_{pl} = \dot{\epsilon}_{r,2}$ . The preceding anelastic  
 34 back flow is expected to cause only subtle changes of the dislocation arrangement and the rest of the  
 35 microstructure; therefore the rate  $\dot{\epsilon}_{r,2}$ , measured short after the period of back flow, has also been  
 36 addressed as 'constant structure' rate. However, it is clear that this is not fully correct (see Section 4).

37 In the further course of the transient after large  $R$ -reductions,  $\dot{\epsilon}_{anel}$  becomes negligible so that  
 38  $\dot{\epsilon}_{inel} \approx \dot{\epsilon}_{pl}$ . A remarkable result is that  $\dot{\epsilon}_{inel}$  generally *decreases* for long times as schematically indicated  
 39 by the dashed curve. This behavior is not well known in the community, although it is regularly found  
 40 whenever investigated, independent of materials and pretreatment. It is distinct from the so-called  
 41 inverse transient behavior where the decrease of  $\dot{\epsilon}_{inel}$  with strain after  $R$ -reduction occurs in the whole  
 42 interval  $0 < R < 1$ , and not only at small  $R$ . One reason for the lack of knowledge about decreasing  
 43  $\dot{\epsilon}_{inel}$  after large  $R$ -reductions is, that long-term tests are required for such observations, covering test  
 44 times distinctly beyond the extended period of back flow. Such tests have been done by Blum and  
 45 coworkers on a number of materials including *e.g.* Al-5Mg (class I alloy) [18,19], Al-Zn (class II alloy)  
 46 [20], and pure LiF [21] and by Van Swygenhoven and coworkers on nanocrystalline Ni and Ni-Fe  
 47 [10,22,23]. In these tests direct evidence for ongoing net recovery of dislocations was obtained. A  
 48 natural explanation of the decrease of  $\dot{\epsilon}_{inel}$  after perturbation of plastic flow by a large  $R$ -reduction is  
 49 that the recovery rate component  $\dot{\epsilon}^-$  decreases, because the driving force for recovery declines during  
 50 the decrease of  $\rho$  and other crystal defects to the lower level in the new qs state at the lower stress.

51 The same process of net recovery must also be expected when a deformed specimen is simply  
 52 unloaded to  $R = 0$  and subsequently annealed at elevated temperature higher than the deformation  
 53 temperature. This type of experiment has been done by Hasegawa, Yakou and Kocks on pure Al  
 54 [24,25] that was deformed at ambient temperature and then quickly heated to elevated temperature.  
 55 The result was qualitatively the same as the result of unloading at fixed temperature described before:  
 56 net *back* flow due to anelastic strains was followed by net *forward* flow at declining rate. This forward  
 57 flow at zero stress after predeformation was interpreted by the authors as consequence of recovery;  
 58 the recovery was suggested to result from reaction of neighboring polarized dislocation walls.

59 So far, comprehensive studies of transient behavior of ultrafine-grained and nanocrystalline (nc)  
 60 are relatively rare. A first report of decreasing recovery-strain rate after relative stress reductions to  
 61  $R = 0.77$  and  $0.70$  was presented in [26] for ufg Cu at 375 K. The present study of transient deformation  
 62 after qs deformation of ufg Cu-Zr aims to

- 63 • advertise an overview plot [27] displaying the full time histories of all transients (see Fig. 5) at  
 64 reasonable resolution,
- 65 • demonstrate that the transient behavior in response to perturbations can be studied in standard  
 66 tensile creep machines of normal accuracy,
- 67 • confirm that typical transient behavior including recovery-strain is found in qualitatively same  
 68 form as in simple, coarse-grained materials,
- 69 • highlight once again the potential of perturbation tests with load changes in deconvoluting the  
 70 submechanisms coupled in monotonic deformation, and
- 71 • make the connection to Milička's constant structure results for  $\dot{\epsilon}_{r,1}$  cited above.



**Figure 2.** Response of inelastic strain to fast changes of creep load from  $F_0$  to  $F_r = R F_0$  during deformation at time  $t_0$  and strain  $\epsilon_{r,0}$  for (a) small  $R$ -increase, (b) small  $R$ -decrease, (c) medium  $R$ -decrease causing  $\dot{\epsilon}_{r,1} = 0$ , (d) large  $R$ -decrease causing net back flow.

## 72 2. Experimental details

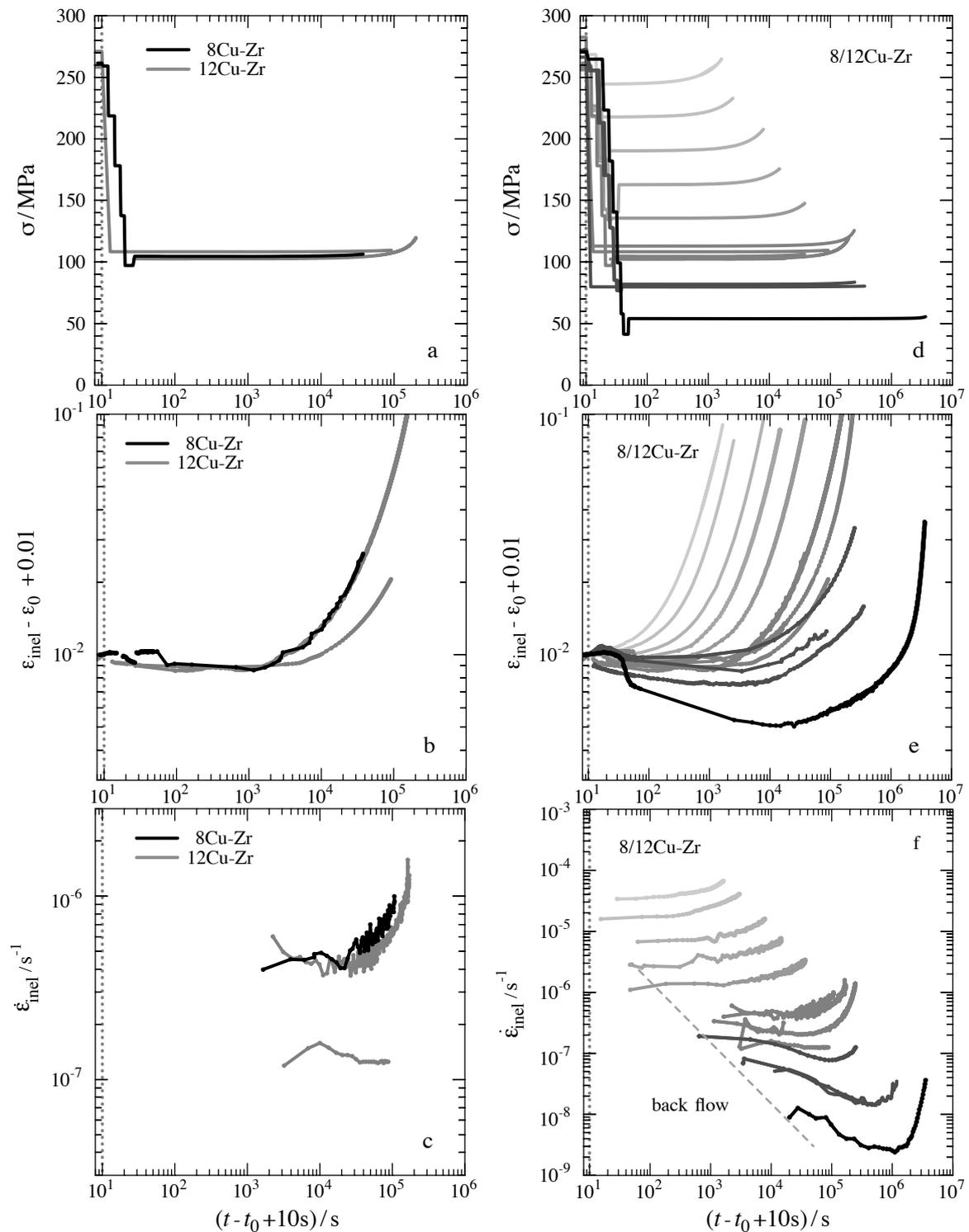
73 As described in more detail in the companion paper [28], our ultrafine-grained particle-stabilized  
 74 material, called  $p$ Cu-Zr, was produced by severe predeformation at ambient temperature in  $p$  passes  
 75 of equal channel angular pressing (ECAP) on route B<sub>C</sub>. Its material parameters are approximated  
 76 by those of pure Cu provided in the data compilation of Frost and Ashby [29]: Burgers vector  
 77  $b = 2.56 \times 10^{-10}$  m, elastic shear modulus  $G = 3.58 \times 10^4$  MPa, melting point  $T_m = 1356$  K. The test  
 78 temperature was  $T = 673$  K =  $0.5 T_m$ .

79 Deformation was started by applying tensile loads  $F$  to flat specimens with initial values of gauge  
 80 length  $l_0 = 10$  mm and cross section  $S_0$  of usually  $\approx 12$  mm<sup>2</sup>. The standard creep machines used in  
 81 this work were designed for long-term measurements of creep strain accumulation at *constant* load, not  
 82 for precisely following small strain changes after load changes. The reproducibility of measurements  
 83 of back flow was worse than in Miliča's tests [14–16], but better than originally expected, although  
 84 some artifacts from unmotivated jumps in the extensometer system or errors in  $\sigma_{\text{eng}}$  occasionally seem  
 85 to have occurred (see e.g. the black curve in Fig. 3b after unloading). In the periods of deformation  
 86 (creep) at constant load the inelastic strain rate is practically identical to the measured total strain rate  
 87  $\dot{\epsilon}_{\text{tot}}$  as the elastic strain rate  $\dot{\epsilon}_{\text{el}}$  is negligible. In the periods of fast changes of load  $F$  this is no longer so.  
 88 Appendix A explains the procedure taken to get the inelastic strain  $\epsilon_{\text{inel}}$  at acceptable accuracy. The  
 89 inelastic strain rate follows from  $\epsilon_{\text{inel}}$  as  $\dot{\epsilon}_{\text{inel}} = \Delta\epsilon_{\text{inel}}/\Delta t$  where  $\Delta\epsilon_{\text{inel}}$  must be chosen larger than the  
 90 experimental noise. This was achieved by data smoothing with the open software SmooMuDS [30].

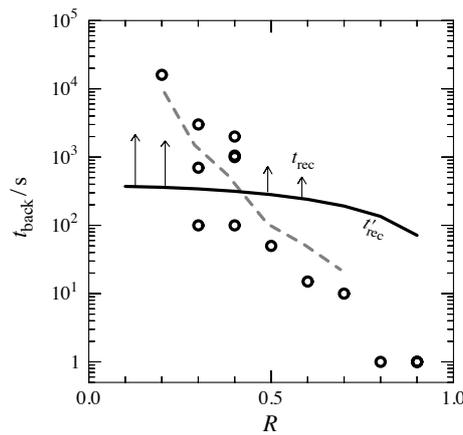
## 91 3. Results

### 92 3.1. Transients as function of time

93 A change of load from a start value  $F_0$  corresponding to an engineering stress  $\sigma_{\text{eng}} = F_0/S_0$  to  
 94 a new value  $F = R F_0$  at time  $t_0$  and inelastic strain  $\epsilon_0$  initiates a transient response. To display all  
 95 transients of largely different durations in the same plot, a logarithmic time scale is used in Fig. 3; the  
 96 constants 10 s in the time-scale and 0.01 in the  $\epsilon_{\text{inel}}$ -scale serve to bring the start of transient into the field  
 97 of view. Fig. 3a-c shows three tests with relative load reductions to by 60% to  $R = 0.4$ . The reductions  
 98 deliberately were performed in steps to explore the behavior at intermediate stresses (Fig. 3a). The  
 99 strain evolution varies with step height and length. In some cases net forward deformation continued  
 100 during the first unloading steps (Fig. 3b). However, the strains accumulated there were small and  
 101 no significant effect on the values of  $\dot{\epsilon}_{\text{inel}} > 0$  after the reductions was observed. This is different in  
 102 the periods of back flow ( $\dot{\epsilon}_{\text{inel}} < 0$ ). Such a difference must be expected because back flow relaxes



**Figure 3.** a) Stress  $\sigma$ , b) strain  $\epsilon_{inel}$ , and c) strain rate  $\dot{\epsilon}_{inel}$  as function of time  $t$  in tests for 8Cu-Zr and 12Cu-Zr with stepwise load reduction to (a,b,c)  $R = 0.4$  and (d,e,f) all  $R$ ; dashed line in (f) approximates boundary of back flow.



**Figure 4.** Times  $t_{\text{back}}$  for anelastic back flow (circles, from Fig. 4e) compared to lower bound  $t'_{\text{rec}}$  of times  $t_{\text{rec}}$  for dynamic recovery toward the new qs state as function of  $R$  for  $\sigma_{r,0} = 275$  MPa; dashed line corresponds to dashed line in Fig. 3f.

103 the internal stresses driving it. However, our work does not focus on back the flow triggered by the  
 104 perturbation by  $R$ -reductions, but on the subsequent forward flow (see Fig. 3b). Figure 3c displays the  
 105 forward strain rates  $\dot{\epsilon}_{\text{inel}} > 0$  after  $R$ -reduction that reappear after about 20 to 30 ks when back flow has  
 106 faded,  $\dot{\epsilon}_{\text{anel}}$  has become negligible and  $\dot{\epsilon}_{\text{inel}} \approx \dot{\epsilon}_{\text{pl}}$ . In the beginning, the uncertainty in  $\dot{\epsilon}_{\text{inel}}$  is large,  
 107 because relatively small strain intervals  $\Delta\epsilon_{\text{inel}}$  were used in determination of  $\dot{\epsilon}_{\text{inel}}$  (compare Section 2).

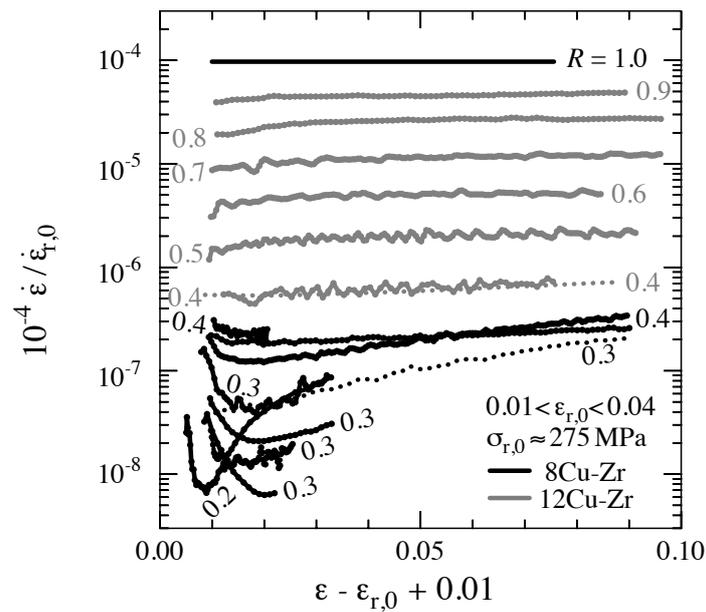
108 Two of the  $\dot{\epsilon}_{\text{inel}}$ -curves in Fig. 3c still appear somewhat noisy. Yet further smoothing of data was  
 109 avoided because the  $\dot{\epsilon}_{\text{inel}}$ -variations seem to have a real origin in slow  $T$ -fluctuations caused by the  
 110 control system. The two gray curves for 8Cu-Zr in subfigure b show the measured  $\dot{\epsilon}_{\text{inel}}$ -extremes. They  
 111 differ by a factor of 3 to 4 in  $\dot{\epsilon}_{\text{inel}}$ . We ascribe that to the aforementioned inhomogeneity of the grain  
 112 structure of 8Cu-Zr. The upper gray curve for 8Cu-Zr is quite similar to the black curve for 12Cu-Zr.  
 113 We conclude from this result that, apart from the scatter of the initial microstructure produced by the  
 114 thermomechanical history, there is no significant difference between the ufg materials 8Cu-Zr and  
 115 12Cu-Zr.

116 Figure 3d-f gives the overview of all  $R$ -reduction tests performed in this work. Again, we focus on  
 117 the forward flow observed after the anelastic back flow. The curves in Fig. 3f derived from Fig. 3e are  
 118 arranged in a fairly consistent sequence corresponding to the loads shown in Fig. 3d. This underscores  
 119 the quality of the length measurements in our creep machines although these were not built for load  
 120 change tests. For  $R \leq 0.3$  a transient decrease of the (forward) strain rate  $\dot{\epsilon}_{\text{inel}} > 0$  is evident.

121 Figure 4 shows the times  $t_{\text{back}}$  (circles) for anelastic back flow taken from the length-time  
 122 recordings. Due to differences in unloading histories and uncertainties in length measurement the  
 123 scatter is large. The dashed line corresponds to the dashed curve from Fig. 3f approximating the  
 124 boundary of back flow. For  $R > 0.75$  the time interval of back flow is immeasurably small. So back  
 125 flow becomes negligible here and deformation goes on at positive rate directly after the load reduction.

### 126 3.2. Transients as function of strain

127 Dislocation generation needs strain. Therefore the strain  $\epsilon_{\text{inel}}$  is much more closely related to the  
 128 microstructural evolution than the testing time  $t$ . So the evolution of deformation strength ( $\sigma, \dot{\epsilon}_{\text{inel}}$ ) is  
 129 commonly displayed on a strain scale. Fig. 5 exhibits the transients of Fig. 3f as function of  $\epsilon_{\text{inel}}$ . As  
 130  $\sigma$  increases at constant load  $F$ ,  $\dot{\epsilon}_{\text{inel}}$  increases even if the microstructure is constant. This effect was  
 131 eliminated by correcting  $\dot{\epsilon}_{\text{inel}}$  (see caption). The corrected curves in Fig. 5 should be horizontal in the  
 132 qs state if the grain and phase structure remains constant. This is indeed found for large  $R$  near 1.  
 133 For smaller  $R$  the curves exhibit a positive slope in the whole strain interval. This means that slow  
 134 microstructural changes are going on throughout the test. Comparison of the dotted and the solid



**Figure 5.** Normalized strain rate as function of normalized strain after load reduction from  $\sigma_{\text{eng}} = 250$  MPa to a relative load  $R$  for 12Cu-Zr (grey lines) and 8Cu-Zr (black lines); the increase of  $q_s \dot{\epsilon} \propto \sigma^{n_{qs}}$  was eliminated with  $n_{qs} = 6$  from [28].

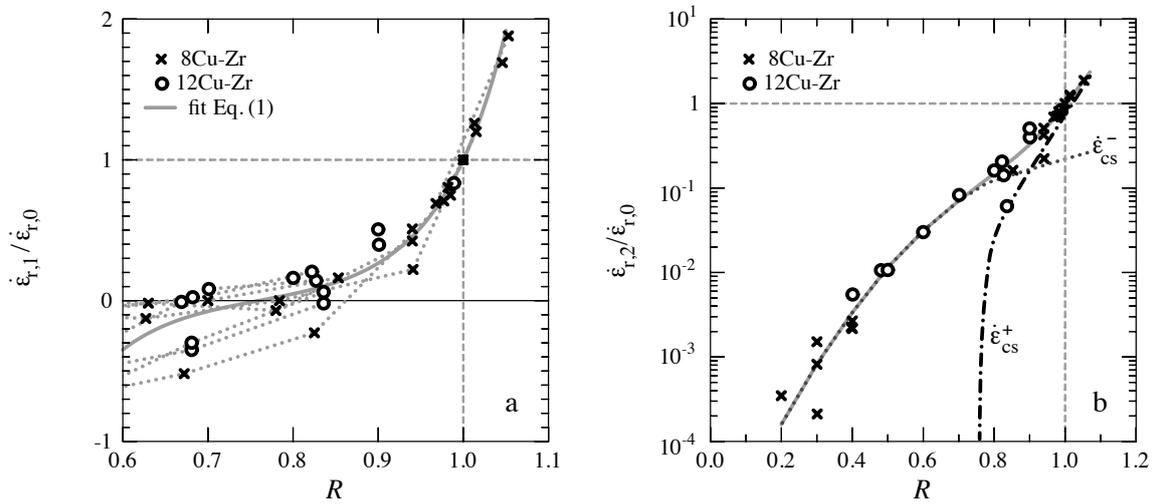
135 curves at  $R = 0.4$  and  $0.3$  shows that these changes are the same in tests with and without  $R$ -reduction.  
 136 At the lowest  $R$  of  $0.2$  (80% unloading) deformation is slowest and the structural changes including  
 137 dislocations are largest. Consequently, softening is most pronounced here. The curve for  $R = 0.2$   
 138 was followed for 42 d before it was interrupted without any indications of fracture; note that the  $\dot{\epsilon}(\epsilon)$   
 139 curve is concave, not convex as in fracture. In [28] the softening has been shown to be a consequence  
 140 of microstructural coarsening, in particular grain coarsening. This means that only the short-term  
 141 portions of the curves after  $R$ -reduction show the transient response to perturbation of the dynamic  
 142 equilibrium of storage and recovery of dislocations in the  $qs$  state at  $t_0$ .

143 Note that the character of this short-term portion of the transients changes significantly with  $R$ .  
 144 For small  $R$ -reductions to  $R \geq 0.5$  there is a relative *increase* of  $\dot{\epsilon}_{\text{inel}}$  compared to the  $qs$  curve at reduced  
 145  $R$ . This is known as normal transient behavior: the material softens due to coarsening of the cellular  
 146 dislocation structure towards the new dynamic equilibrium state. However, for large  $R$ -reductions to  
 147  $R < 0.5$  and  $\dot{\epsilon}_{\text{inel}} \leq 10^{-7} \text{ s}^{-1}$  there is an initial *decrease* of  $\dot{\epsilon}_{\text{inel}}$ .

Figure 6 displays the constant structure rates  $\dot{\epsilon}_{r,1}$  and  $\dot{\epsilon}_{r,2}$  that were measured at the beginning of the transients with and after without anelastic back flow, respectively (see Fig. 2). Figure 6a shows that  $\dot{\epsilon}_{r,1}$  falls to zero near  $R = 0.76$  and becomes negative (back flow) for lower  $R$ . Following Milicka [14], the data were approximated by a sinh-expression

$$\dot{\epsilon}_{r,1} = k_1 \sinh(V(\sigma - \sigma_i)/(M k_B T)) \quad k_1 = 0.0885, \sigma_i = 0.76 \sigma_{r,0}, \quad (4)$$

148 giving the solid grey line. Figure 6b shows the positive rates  $\dot{\epsilon}_{r,2}$  after back flow.



**Figure 6.** Normalized creep constant structure strain rate  $\dot{\epsilon}_r$  after qs deformation at  $\sigma_{r,0} \approx 275$  MPa as function of relative creep load  $R$ : (a)  $\dot{\epsilon}_{r,1}$ , grey dotted lines connect data from same test with stepwise load reduction, (b)  $\dot{\epsilon}_{r,2}$  on log scale with estimates of  $\dot{\epsilon}_{cs}^-$  (dotted black) and  $\dot{\epsilon}_{cs}^+$  (solid black); see text.

## 149 4. Discussion

150 Our results for ufg Cu-Zr are qualitatively quite similar to the general behavior observed for  
 151 crystalline materials after a perturbation of monotonic plastic flow by load changes. For small  
 152  $R$ -reductions deformation goes on at reduced rate in forward direction according to the applied  
 153 stress and the material softens with strain in parallel to the recovery of the dislocation structure. For  
 154 large  $R$ -reductions deformation first goes backward before it returns to positive direction again and  
 155 then continues at decreasing rate. As mentioned in Section 1, this rate decrease parallels the decreasing  
 156 rate of recovery and therefore may be directly linked to dynamic recovery. This can be understood  
 157 from the view that the strain rate term  $\dot{\epsilon}^+$  leading to storage of dislocations disappears for small  $R$  so  
 158 that the strain rate term  $\dot{\epsilon}^-$  related with dynamic recovery dominates. These transient phenomena  
 159 disappear while the new qs state corresponding to  $R$  is approached.

160 The two terms  $\dot{\epsilon}^+$  and  $\dot{\epsilon}^-$ , corresponding to the cases 'dislocations in' and 'dislocations out' of  
 161 Fig. 1, have different kinetics. This difference should become apparent in those ranges of  $R$  where  
 162 either  $\dot{\epsilon}^+$  or  $\dot{\epsilon}^-$  dominate. This is in line with the different  $R$ -dependences of the lines for  $\dot{\epsilon}^+$  and  $\dot{\epsilon}^-$   
 163 in Fig. 6b. Milička [14–16] restricted his measurements to the  $R$ -range with  $\dot{\epsilon}_{r,1} \geq 0$ . In spite of this  
 164 restriction, he discovered that a single mechanism of deformation obeying Eq. (4) is not sufficient  
 165 to describe the variation of  $\dot{\epsilon}_{r,1}$  with  $R$ . So he proposed to express  $\dot{\epsilon}_{r,1}$  as a sum of two terms [15,16].  
 166 This parallels the separation of  $\dot{\epsilon}_{pl}$  into  $\dot{\epsilon}^+$  and  $\dot{\epsilon}^-$  in Eq. (2). Preliminary evaluations showed that the  
 167 parallelity holds not only in qualitative, but also quantitative respect, noting that the separation is  
 168 somewhat ambiguous due to uncertainties in those  $R$ -ranges where one of the two terms dominates.

### 169 4.1. Strain related with storage of defects

170 From the preceding discussion we surmise that for  $R \leq 0.7$  the rate  $\dot{\epsilon}_{r,2}$  approximately equals  $\dot{\epsilon}^-$ .  
 171 Extrapolating the  $\dot{\epsilon}_{r,2}$ -curve for  $R < 0.7$  in Fig. 6 yields  $\dot{\epsilon}_{qs}^-$ -values at  $R = 1$  in the range of 10% and  
 172 30% of  $\dot{\epsilon}_{r,0}$ . In other words: the recovery-strain rate  $\dot{\epsilon}_{qs}^-$  contributes about  $(20 \pm 10)\%$  to the qs strain  
 173 rate.  $\dot{\epsilon}_{cs}^+$  follows as the difference of  $\dot{\epsilon}_r$  and  $\dot{\epsilon}_{cs}^-$  (Eq. (2)). The stress exponent of this curve at  $R = 1$  is  
 174  $n_{cs}^+ = 17$  at  $R = 1$ . This is close to the estimate 21 derived from the theory of thermally activated glide  
 175 (Eq. (A15)). In view of the simplifications and assumptions involved, we conclude from this result that  
 176 an interpretation of  $\dot{\epsilon}_{cs}^+$  in terms of the classical theory of thermally activated glide over fixed repulsive  
 177 obstacles in pure materials (e.g. forest dislocations) may be possible.

### 178 4.2. Strain related with recovery of defects

179 We now turn attention to the recovery-strain rate  $\dot{\epsilon}^-$ . Figure 7a compares the recovery-strain  
 180 rates  $\dot{\epsilon}_{cs}^-$  at (approximately) constant structure from Fig. 6b (dotted line) to the recovery-strain rate  
 181  $\dot{\epsilon}_{qs}^-$  at qs structure (solid line) as function of stress  $\sigma$ . The latter is obtained from the qs strain rates  
 182  $\dot{\epsilon}_{qs} \propto \sigma^6$  reported in the companion paper [28] under the assumption that the fraction  $\dot{\epsilon}_{qs}^-/\dot{\epsilon}_{qs}$  in  
 183 qs deformation equals  $\approx 0.2$  independent of stress.  $\dot{\epsilon}_{cs}^-$  is higher than  $\dot{\epsilon}_{qs}^-$ . This can be qualitatively  
 184 explained by the higher defect density and higher local stresses in the cs states inherited from the  
 185 preceding deformation at the high stress  $\sigma_{r,0} \approx 275$  MPa compared to the qs states established at lower  
 186 stresses  $\sigma < \sigma_{r,0}$ . So far there is no accepted detailed model of dynamic recovery and its strain rate  
 187 contribution  $\dot{\epsilon}^-$ . Strain contributions from recovery of individual dislocations stored at recovery sites,  
 188 probably internal crystal boundaries of low- and high-angle type, and from recovery of boundaries by  
 189 migration need to be considered.

One may ask to which extent the recovery-strain rate gets reduced in the period of back flow  
 before  $\dot{\epsilon}_{r,2}$  is measured. It is clear that anelastic back flow relaxes internal stresses. Also, some fast  
 recovery processes of the kind shown in Fig. 1 will happen already during the period of net back flow  
 and thereby reduce the density of recovery sites. This indicates that use of the term 'constant structure'  
 for  $\dot{\epsilon}_{cs}^-$  becomes increasingly problematic with declining  $R$  with regard to the dislocation structure and  
 raises the question whether the constant structure assumption is wrong and anelastic back flow may

even be lasting long enough to modify not only the internal stresses, but also allow the dislocation structure to evolve close to the new qs state at reduced stress. To answer this question we estimate a lower limit  $t'_{\text{rec}}$  of the time  $t_{\text{rec}}$  for full recovery into the new qs state. The estimate is based on the assumptions that (i) no dislocation generation takes place during the anelastic back flow even though the new qs state is based on dynamic equilibrium of generation and recovery and (ii) the maximal rate of dislocation recovery pertains throughout the back flow period even though the driving force for recovery must decrease. In the literature there is very little direct information on the evolution of the density  $\rho$  of dislocations during dynamic recovery. The reasons are that dynamic recovery is generally accompanied by dislocation glide of type  $\dot{\epsilon}^+$  and that reliable observations can only be made if the dislocations can safely be pinned up to microscopic observation. A set of data was measured in [20] for the alloy Al-Zn where pinning is possible by precipitation of particles. The data were obtained in the qs state characterized by Eq. (1). It was found that the measured dislocations recovery rates  $\approx \dot{\rho}^-$  were in accord with Eq. (1) when the dislocation generation rate is expressed as

$$\dot{\rho}^- \approx \dot{\rho}^+ = \frac{M f_{\Lambda}}{b} \frac{\dot{\epsilon}^+}{\Lambda}. \quad (5)$$

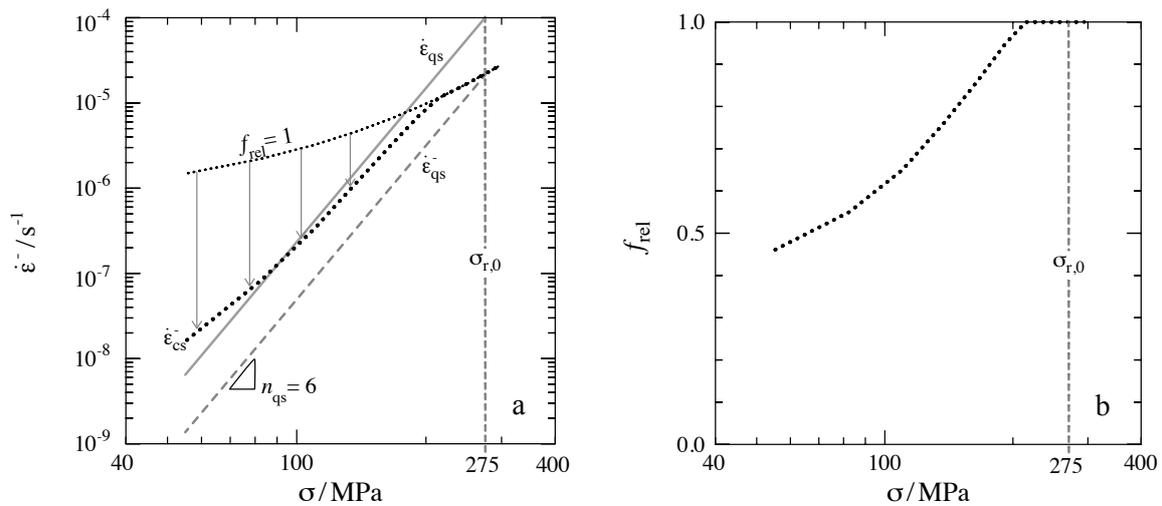
190 where  $\Lambda$  is proportional to the mean free path of dislocations and  $f_{\Lambda}$  is a numerical factor near 1.  
 191 For a rough estimate we set  $\Lambda = d_0$ ,  $\dot{\epsilon}_{r,0} = 10^{-4} \text{ s}^{-1}$ ,  $f_{\Lambda} = 1$ . This yields the rate  $\dot{\rho}_0^-$  of dynamic  
 192 dislocation recovery just before the  $R$ -reduction as  $1.99 \times 10^{-12} \text{ m}^2 \text{ s}^{-1}$ . The initial qs dislocation  
 193 spacing is estimated as  $\rho_{\text{qs}} = (b G / \sigma_{r,0})^2$  at  $\sigma_{r,0} = 275 \text{ MPa}$ . The solid line in Figure 4 shows the result  
 194 for  $t'_{\text{rec}}$ . The data symbols represent the experimental data for the time period  $t_{\text{back}}$  where anelastic  
 195 back flow occurs or cannot be excluded due to experimental inaccuracy. The result of this estimate is  
 196 that in a large  $R$ -range the time period  $t_{\text{back}}$  available for recovery during back flow is smaller than  
 197 the lower bound  $t'_{\text{rec}}$  of the time period  $t_{\text{rec}}$  of recovery needed to reach the new qs state of dislocation  
 198 density. This corresponds to the observation that recovery of  $X$ -line widths continues after the period  
 199 of back flow [22] and is another argument to assume that  $\dot{\epsilon}_{\text{cs}}^-$  in Fig. 6b represents the recovery-strain  
 200 rate and not the strain rate associated with generation and storage of defects.

201 The results of the present work do not allow us to deduce details about the mechanism of  
 202 recovery-strain. Cross slip [31] and climb [32] have been proposed as rate-controlling mechanisms  
 203 (compare [3]). Stress concentrations at boundaries by long-range internal stresses have been used  
 204 in descriptions of kinetics with the composite model [33]. Boundaries of low-angle type [11,21] in  
 205 coarse-grained materials and high-angle type in ultrafine-grained and nanocrystalline materials [34]  
 206 are being discussed as sinks of dislocations as well as boundaries themselves via recombination during  
 207 migration. In class II alloys with viscous dislocation glide and spatially homogeneous distribution  
 208 of recovery events long-range stresses seem to play little role [2,18,19,35]. The period of dominant  
 209 recovery-strain rate  $\dot{\epsilon}^-$  after load reductions seems suitable for dedicated tests of stress sensitivity and  
 210 microstructure evolution. Tests of this kind have been started on Al [36] and were recently continued  
 211 for nc Ni [22,23]. Better understanding of recovery-strain may be of profound value in technical  
 212 application of strong materials under conditions of varying stress  $\sigma$ , e.g. in stress relaxation and cyclic  
 213 deformation.

For a tentative and exemplary interpretation of the results we use the approach presented in [37]. It assumes that the volume density of recovery sites remains constant, also during anelastic back flow, and that the recovery-strain rate varies with a power  $q$  of the local stress  $\sigma_{\text{h}}$  acting at the recovery sites:

$$\dot{\epsilon}_{\text{cs}}^- = f_0^- \dot{\epsilon}_{r,0} \left( \frac{\sigma_{\text{h}}}{\sigma_{\text{h},0}} \right)^q \quad (6)$$

214 where  $\sigma_{\text{h}} = R \sigma_{r,0} + f_{\text{rel}} \sigma_{f,0}$  is the local stress at the recovery sites and  $\sigma_{\text{h},0} = k_{\text{h},0} \sigma_{r,0}$  is the qs value of  
 215  $\sigma_{\text{h}}$  at  $R = 1$  before the  $R$ -change. The numerical factor  $0 \leq f_{\text{rel}} \leq 1$  empirically simulates the relaxation  
 216 of the internal forward stress at the recovery sites during anelastic back flow. The exponent was chosen  
 217 as  $q = 7$ . Figure 7a shows the curve for the qs deformation rate with stress exponent  $n_{\text{qs}} = 6$  from



**Figure 7.** a) Recovery-strain rate  $\dot{\epsilon}_{cs}^-$  at constant structure after  $R$ -change from Fig. 6b (black dotted) compared to qs strain rate  $\dot{\epsilon}_{qs}$  (grey solid) and recovery-strain rate  $\dot{\epsilon}_{qs}^-$  in the qs state (grey dashed), b) anelastic relaxation factor  $f_{rel}$  as function of  $\sigma \approx R\sigma_{r,0}$  required to model  $\dot{\epsilon}_{cs}^-$  from (a) with Eq. (6).

218 [28], the qs recovery-strain rate  $\dot{\epsilon}_{qs}^-$  under the condition that  $\dot{\epsilon}_{qs}^-/\dot{\epsilon}_{qs} = 0.22$  independent of stress, and  
 219 the recovery-strain rates  $\dot{\epsilon}_{cs}^-$  from Eq. (6) for the cases  $f_{rel} = 1$ , *i.e.* no relaxation of internal forward  
 220 stress during anelastic back flow, and decrease of  $f_{rel}$  with decreasing  $\sigma = R\sigma_{r,0}$  as shown in Fig. 7b,  
 221 leading to perfect fit of the measured  $\dot{\epsilon}_{cs}^-$ -curve (dotted black line) in Fig. 6b. Even though the fit of  
 222 the measured  $\dot{\epsilon}_{cs}^-$ -curve was possible with relaxation of the internal stress  $\sigma_{f,0}$ , it seems probable that  
 223 some exhaustion of recovery sites during back flow will contribute to the reduction of  $\dot{\epsilon}_{cs}^-$  indicated  
 224 by the downward arrows in Fig. 7a as well. This exercise shows that a quantitative description of  
 225 the recovery-strain rate using simple phenomenological laws for dynamic recovery is possible and  
 226 indicates that dedicated tests in the period of recovery-strain dominance, like the ones performed in  
 227 [22,23,36], seem promising to determine the kinetics of dynamic recovery.

#### 228 4.3. Comparison of stress dependences of $\dot{\epsilon}^+$ and $\dot{\epsilon}^-$ at constant structure

229 One problem with measuring the recovery-strain rate  $\dot{\epsilon}^-$  is that its separation from  $\dot{\epsilon}^+$  in  
 230 load/stress change tests is not trivial and sometimes impossible. The separation is easy and accurate  
 231 if the inflection point in the semilogarithmic  $\dot{\epsilon}_{r,2}$ -curve (Fig. 6b) is well pronounced. This depends  
 232 strongly on the slope of this curve at  $R = 1$ . This slope is mostly given by the stress exponent  $n_{cs}^+$  of  $\dot{\epsilon}^+$ ,  
 233 Eq. (A15) which should be distinctly larger than the slope of the  $\dot{\epsilon}^-$ -curve. According to the estimate  
 234 of Eq. (A14)  $n_{cs}^+$  decreases inversely proportional to the temperature  $T$ . Therefore the separation of  $\dot{\epsilon}^-$   
 235 becomes increasingly difficult when  $T$  increases. Solid solution strengthening leads to further reduction  
 236 of  $n_{cs}^+$ . Then the inflection point in the semilogarithmic  $\dot{\epsilon}_{r,2}$ -curve (Fig. 6b) disappears completely (*e.g.*  
 237 in Al-5Mg [14,19] and Fe-Si [15]). This probably indicates that the kinetics of  $\dot{\epsilon}^+$  (with storage of crystal  
 238 defects) and  $\dot{\epsilon}^-$  (with recovery of crystal defects) become indistinguishable in the  $\dot{\epsilon}_{r,2}(R)$  plot and can  
 239 no longer be used for separation.

## 240 5. Summary

- 241 • In ufg Cu-Zr at  $0.5T_m$  recovery-strain  $\epsilon^-$  connected with dynamic recovery of strain-induced
- 242 crystal defects was found in tests with perturbation of the qs state by load reductions.  $\epsilon^-$  adds to
- 243 the strain  $\epsilon^+$  connected with dislocation generation and storage.
- 244 • The stress dependence of  $\dot{\epsilon}^+$  yields an activation volume consistent with the classical theory of
- 245 thermally activated glide.
- 246 • The recovery-strain rate  $\dot{\epsilon}^-$  contributes 10% to 30% to the quasi-stationary strain rate  $\dot{\epsilon}_{qs}$ .

- 247 • The stress dependence of  $\dot{\epsilon}_{cs}^-$  at constant structure is consistent with that of the recovery-controlled  
248 qs strain rate  $\dot{\epsilon}_{qs}$ .

249 **Author Contributions:** conceptualization, W.B. and P.K.; methodology, V.S., J.D., P.K. and P.E.; software, W.B. and  
250 P.E.; validation, P.K., J.D.; formal analysis, W.B.; investigation, V.S., J.D., P.K.; resources, J.D.; data curation, J.D., P.K.  
251 and W.B.; writing—original draft preparation, W.B.; writing—review and editing, W.B., P.K. and P.E.; visualization,  
252 W.B.; J.D., P.K., W.B. and P.E.; supervision, W.B. and V.S.; project administration, V.S.; funding acquisition, V.S.

## 253 Appendix A. Determination of inelastic strain

The load  $F$  corresponding to an engineering stress

$$\sigma_{eng} = F/S_0 \quad (A1)$$

was varied in steps. Fig. A1a shows an example. Assuming volume constancy, the cross section varies with the gauge length

$$l = l_0 - \Delta l, \quad (A2)$$

where  $\Delta l$  is the measured length change, as

$$S = S_0 l_0/l = S_0 \exp(\epsilon_{tot}), \quad \epsilon_{tot} = \ln(l/l_0) \quad (A3)$$

where  $\epsilon_{tot}$  is the total “true” strain. Fig. A1b shows the variation of  $\epsilon_{tot}$  with time  $t$  corresponding to Fig. A1a. The  $\epsilon_{tot}$ -steps in Fig. A1b result from the changes of the elastic strain related with the changes of  $F$ . To eliminate these steps the elastic strain must be estimated. This was done in the following straightforward manner. The elastic strain is composed from two components:

$$\epsilon_{el} = \epsilon_{el,Cu} + \epsilon_{mach}. \quad (A4)$$

$\epsilon_{el,Cu}$  is the elastic strain of the gauge length  $l$  of the specimen described by:

$$\epsilon_{el,Cu} = \sigma/E \quad (A5)$$

with

$$\sigma = F_c/S \approx \sigma_{eng} \exp(\epsilon_{tot}) \quad (A6)$$

as “true” stress acting in the gauge length and  $E \approx 9 \times 10^4$  MPa as elastic tensile modulus (Young’s modulus) of Cu.  $\epsilon_{mach}$  is the elastic strain

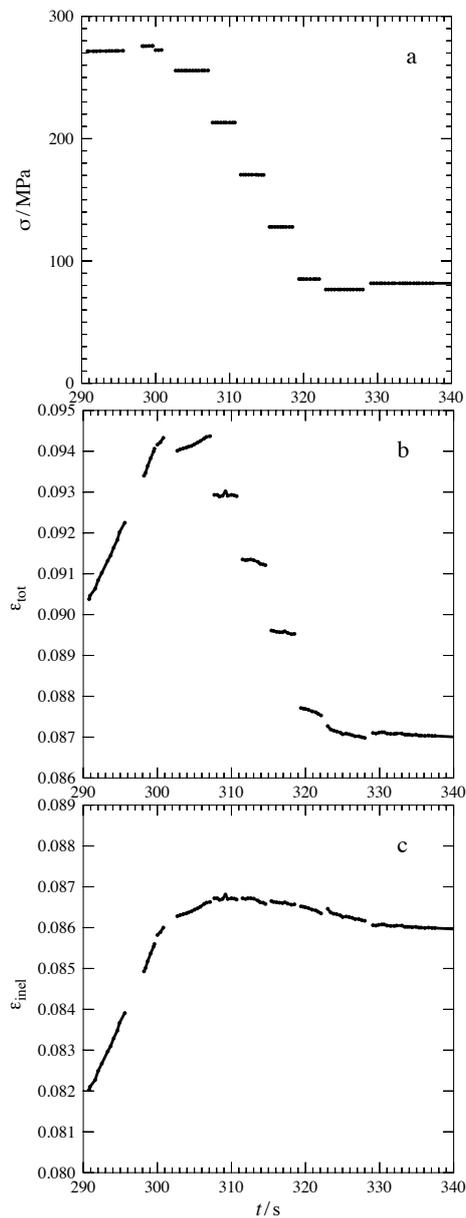
$$\epsilon_{mach} = \Delta l_{mach}/l \quad (A7)$$

resulting from all parts of specimen and machine entering the measured length change outside the gauge length  $l$ . The unknown elastic machine length change was determined in an iterative manner so that the elastic steps in the  $\epsilon_{tot}$ - $t$  plots like Fig. A1b were optimally suppressed. An analytical formulation with a power law:

$$\Delta l_{mach}/\text{mm} \approx c_1 (F_c/\text{N})^{c_2} - c_3. \quad 0.001 < c_3 < 0.006 \quad (A8)$$

with  $c_1 = 2.23 \times 10^{-4}$ ,  $c_2 = 0.74$  and a constant  $c_3$  turned out to be comfortable and sufficiently exact. The approximate inelastic strain then follows as:

$$\epsilon_{inel} = \epsilon_{tot} - \epsilon_{el}. \quad (A9)$$



**Figure A1.** a) Stress  $\sigma$ , b) total strain  $\epsilon_{\text{tot}}$  with elastic strains from machine and specimen, c) inelastic strain  $\epsilon_{\text{inel}}$  versus time  $t$  in load change test on 8Cu-Zr at 673 K.

Individual choice of  $c_3$  for each test proved reasonable to compensate systematic errors of the  $\Delta l$ -signal near  $F = 0$  before the motions of specimen and strain gages become uniaxial. In a final step the stress was corrected by changing Eq. (A6) to

$$\sigma \approx F_c/S = \sigma_{\text{eng}} \exp(\epsilon_{\text{inel}}). \quad (\text{A10})$$

254 This has only marginal influence on the results. Fig. A1c shows that the elastic steps from Fig. A1b  
 255 have virtually disappeared. Some gaps in the curves are caused by data acquisition problems. The test  
 256 includes a small stress increase at  $t \approx 300$  s followed by stepwise unloading within less than 30 s. It  
 257 is seen how the (inelastic) strain  $\epsilon_{\text{inel}}$  continues to increase till 307 s and then starts to decrease. This  
 258 decrease is called anelastic, because it is reversible on a macroscopic level. The elimination of the  
 259 elastic strain helps to visualize the anelastic response that is less pronounced than the elastic one (also  
 260 in comparison to the elastic response of the specimen). Eq. (A7) may cause an elastic overcorrection  
 261 at stresses below 100 MPa. However, this is irrelevant for the inelastic strain rates in the periods  
 262 of relatively constant load, where the major elastic strain component resulting from  $\Delta l_{\text{mach}}$  remains  
 263 constant.

## 264 Appendix B. Activation volume of dislocation glide

Glide in the course of expansion of dislocation loops bounding the slipped areas causes an inelastic strain rate  $\dot{\epsilon}^+$ . It is driven by the resolved shear stress  $\sigma/M$ , where  $M$  is the geometrical factor of conversion from normal to shear stress and strain (for untextured face-centered polycrystals: Taylor factor = 3.06),  $k_B$  is the Boltzmann constant, and is supported by thermally activated overcoming of thermal obstacles. The operational activation volume is defined by

$$V_{\text{op}}^+ = k_B T \frac{d \ln \dot{\epsilon}^+}{d \sigma / M} \quad (\text{A11})$$

To get a rough estimate of  $V_{\text{gl}}^{\text{op}}$  we tentatively use the classical model of thermally activated glide through a field of point-like repulsive obstacles. According to this model the activation volume is

$$V^+ = b \lambda_{\text{gl}} \Delta x_{\text{gl}}. \quad (\text{A12})$$

265 where  $\lambda_{\text{gl}}$  and  $\Delta x_{\text{gl}}$  are obstacle spacing and width, respectively. Eq. (A12) holds under the condition  
 266 that the microstructure including the internal stresses remains constant in the change test. If

- 267 •  $\lambda_{\text{gl}}$  is set equal to the expected spacing of free dislocations,  $bG/\sigma$ , and
- 268 •  $\Delta x_{\text{gl}}$  is approximated by  $b$ ,

$V^+$  becomes a simple function of stress:

$$V^+ \approx b^3 G/\sigma. \quad (\text{A13})$$

By approximating  $V_{\text{op}}^+$  in Eq. (A11) by  $V^+$  from Eq. (A13) and using the mathematical identity  $d\sigma = \sigma d \ln \sigma$  one arrives at a simple estimate

$$n_{\text{cs,est}}^+ \equiv \frac{b^3 G}{M k_B T}. \quad (\text{A14})$$

of the stress exponent of  $\dot{\epsilon}^+$  at constant structure<sup>1</sup>:

$$n_{cs}^+ = \frac{\partial \ln \dot{\epsilon}^+}{\partial \ln \sigma}. \quad (\text{A15})$$

269 The  $n_{cs}^+$ -estimate is independent of  $\sigma$  and inversely proportional to temperature  $T$  for a given material.

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<sup>1</sup> Meanwhile it has become customary to neglect the condition of constant structure; this leads to a mix-up with the qs rate sensitivity [16,38].

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