

1 Article

2 The effect of molybdenum on precipitation behaviour 3 in austenitic strip-cast steels containing niobium

4
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11 **Abstract:** Two low-C steels microalloyed with Nb were fabricated by simulated strip casting, one with
12 Mo and the other without Mo. Both alloys were coiled at 900 °C to investigate the effect of Mo on the
13 precipitation behaviour in austenite in low-C strip-cast Nb steels. The mechanical properties results
14 show that during the coiling at 900 °C the hardness of both alloys increases and reaches a peak after
15 3000 s and then decreased after 10,000 s. Additionally, the hardness of the Mo-containing alloy is higher
16 than that of the Mo-free alloy in all coiling conditions. Thermo-Calc predictions suggest that MC-type
17 carbides exist in equilibrium at 900 °C, which are confirmed by transmission electron microscopy (TEM).
18 TEM examination shows that precipitates are formed after 1000 s of coiling in both alloys and the size
19 of the particles is refined by the addition of Mo. Energy dispersive spectroscopy (EDS) and electron
20 energy loss spectroscopy (EELS) reveal that the carbides are enriched in Nb and N. The presence of Mo
21 is also observed in the particles in the Nb-Mo steel during coiling. The concentration of Mo in the
22 precipitates decreases with increasing particle size and coiling time. The precipitates in the Nb-Mo steel
23 provide significant strengthening increments of up to 140 MPa, much higher than that in the Nb steel,
24 ~ 96 MPa. A thermodynamic rationale is given, which explains that the enrichment of Mo in the
25 precipitates reduces the interfacial energy between precipitates and matrix. This is likely to lower the
26 energy barrier for their nucleation and also reduce the coarsening rate, thus leading to finer precipitates
27 during coiling at 900 °C.

28 **Keywords:** Molybdenum; Precipitation; Austenite; Niobium Steels; Strip Casting

29

30 1. Introduction

31 For the high-strength low-alloy (HSLA) steels containing niobium (Nb) produced by conventional
32 casting techniques, hot deformation in the austenite region usually induces the formation of Nb
33 carbonitrides precipitates [1, 2]. The Nb carbonitrides, formed in austenite, are able to provide
34 precipitation strengthening and refine the microstructure by delaying the recrystallization of austenite
35 at high temperatures, improving the strength as a result [2, 3]. However, these precipitates can be
36 eventually very coarse after a prolonged isothermal-holding in the austenite region, consequently
37 losing their advantage in the microstructure refinement and precipitation strengthening. In previous
38 literature, trace additions of molybdenum (Mo) were reported to enhance the precipitation
39 strengthening of steels microalloyed with Nb or/and Ti by suppressing the coarsening of Nb or Ti
40 carbides [4-10]. It was proposed that Mo changes the coarsening resistance of Nb-rich carbonitrides in
41 austenite by lowering interfacial energy [11], and thus refines the precipitates [11, 12]. However, despite
42 the extensive investigations on the effect of Mo on the formation of Nb-rich precipitates in austenite,
43 the mechanisms behind these observations are not well established.

44 Unlike conventional steel-making processes that usually undergo several controlled hot-rolling passes,
45 direct strip casting (DSC) combines casting and subsequent hot-rolling into a single and continuous

1 route with extremely rapid solidification and high cooling rates [1-3], which reduces cost and saves
 2 energy-consumption up to 90%. Dorin et al. [13] studied the formation of Nb(C, N) in strip-cast steels
 3 and found that chemically complex Nb-rich precipitates containing C, N, Si and S were formed in
 4 austenite during coiling at a high temperature (850 °C), which provides a significant strength increment
 5 of up to ~ 150 MPa. This early work also emphasized significant differences in the Nb(C, N) precipitates
 6 formed in strip-cast materials as compared to the ones formed in conventionally processed steel. One
 7 of the main differences is that strip casting produces as-cast samples where the Nb is supersaturated
 8 and the precipitates can then be formed during a controlled coiling treatment [14]. Consequently,
 9 precipitation occurs in non-deformed austenite. Thus, the mechanism behind the precipitation can be
 10 different to the strain-induced precipitation in previous literature. To the best of our knowledge, the
 11 effect of Mo on the precipitation of Nb(C, N) in the austenite phase field of strip-cast steels has rarely
 12 been studied.

13 In the present paper, two Nb-containing low-carbon steels were prepared via strip casting with and
 14 without Mo. The as-cast samples were then coiled at 900 °C for different durations and hardness testing
 15 was used to monitor the hardening response during coiling. Transmission electron microscopy (TEM)
 16 was performed to observe the precipitation for different coiling times. Finally, the thermodynamic
 17 effects of Mo on Nb-rich precipitates and corresponding precipitation strengthening are also presented.

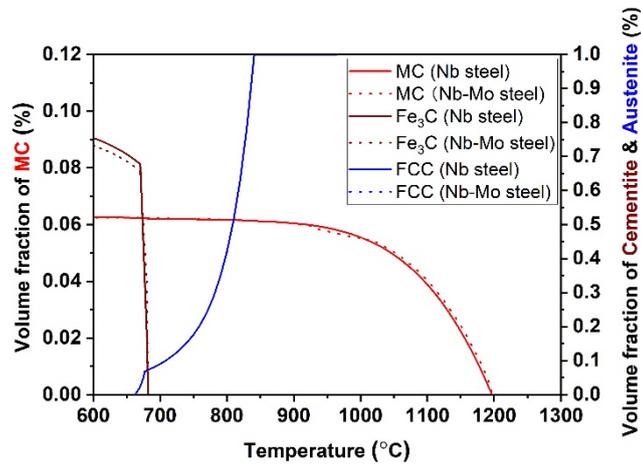
18 2. Materials and Methods

19 The compositions of the alloys studied in this work are listed in Table 1. The steels were cast using a
 20 lab-scale strip casting simulator, known as a dip tester [15]. The steels were melted in a 75 kW induction
 21 furnace using high purity starting elements. The details of the casting process can be found in [16, 17].
 22 After casting, the samples were immediately transferred into a preheated muffle furnace within 2 s,
 23 and within this time the samples did not cool below the coiling temperature of 900 °C. The detailed
 24 thermal profile and schedule diagram of coiling treatment can be found in [16]. Coiling times varied
 25 from 100 to 10,000 s, and all samples were air-cooled to room temperature at the end of the coiling
 26 treatment.

27 **Table 1.** Compositions of the studied alloys, wt.%.

	C	Mn	Si	Al	Nb	Mo	S	N	Fe
Nb steel	0.05	1.45	0.21	0.003	0.05	-	<0.0005	0.01	bal.
Nb-Mo steel	0.05	1.50	0.23	0.004	0.05	0.33	<0.0005	0.01	bal.

28
 29 Thermo-Calc software with TCFE 9: Steels/Fe Alloys v9.0 database was used to check to the equilibrium
 30 phases at 900 °C for the two steels, as displayed in Fig. 1. It can be seen that at 900 °C MC-type carbides
 31 can be formed in the austenite region and the theoretical volume fraction of these carbides in
 32 equilibrium is ~ 0.0605%.



1

2 **Figure 1** Volume fractions of MC, austenite and cementite in equilibrium, as predicted by Thermo-Calc software
 3 with TCFE 9: Steels/Fe Alloys v9.0 database.

4

5 Hardness tests were carried out at room temperature to monitor the hardness evolution of both steels
 6 coiled at 900 °C for various times. Average values were generated from at least 7 measurements for
 7 each condition.

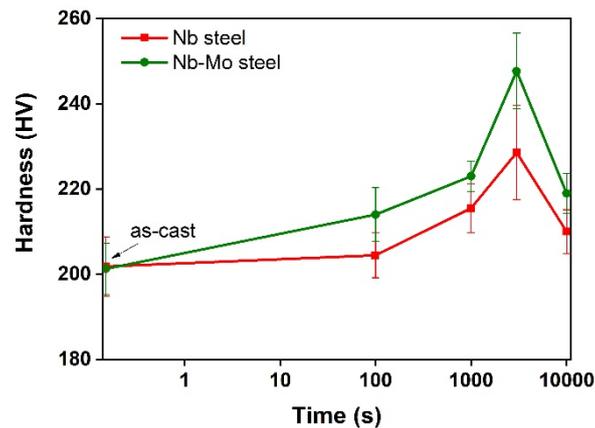
8 Samples examined by optical microscopy were prepared by sectioning parallel to the casting direction.
 9 The specimens were ground using increasingly finer grades of silicon carbide paper, followed by
 10 polishing using diamond particles solutions. Polished samples were etched in 4% nital solution for 10
 11 s. Optical micrographs were taken using Olympus HR DP70 microscope.

12 TEM foils were electropolished in a solution of 5% perchloric acid in methanol using a twin-jet Tenupol
 13 unit, running at 30 V and ~ -35 °C. Carbon layers for TEM carbon replica samples were prepared using
 14 a JEOL JEE-420 Vacuum Evaporator and supported by 300 square mesh copper grids. TEM observation
 15 was performed on Philips CM20 instrument with a LaB₆ filament operating at 200 kV. Composition
 16 analysis of precipitate particles was carried out using JEOL FEG 2100F TEM with JED-2300T energy
 17 dispersive spectroscopy (EDS) detector, operating at 200 kV. Gatan GIF Quantum 965 post column
 18 electron energy loss spectroscopy (EELS) analysis was carried out for fine composition examination
 19 using an energy range of 0 to 1000 eV.

20 3. Results

21 3.1 Hardness

22 Hardness measurements were conducted on the two steels for different durations of coiling at 900 °C,
 23 as shown in Figure 2. The as-cast hardness of both the Nb and Nb-Mo steels was ~ 201 HV indicating
 24 the minor effect of 0.33 wt.% Mo to the Nb steels in the as-cast condition. This has been explained by
 25 the very small solid solution strengthening from the addition of Mo in solid solution when the as-cast
 26 microstructure of both alloys is very similar [18]. As coiling treatment progresses, the hardness of both
 27 alloys evolves in a similar manner. In the early stage (before 100 s), the hardness slowly increases.
 28 Afterwards, a more rapid hardening occurs in both alloys by reaching the peak hardness after 3000 s at
 29 900 °C. The Nb-steel and Nb-Mo-steel reached peak hardness values of 225 and 245 HV, respectively.
 30 However, after 10,000 s coiling the hardness of both steels drops. Generally, the hardness of the Nb-Mo
 31 steel is higher than that of the Nb steel.

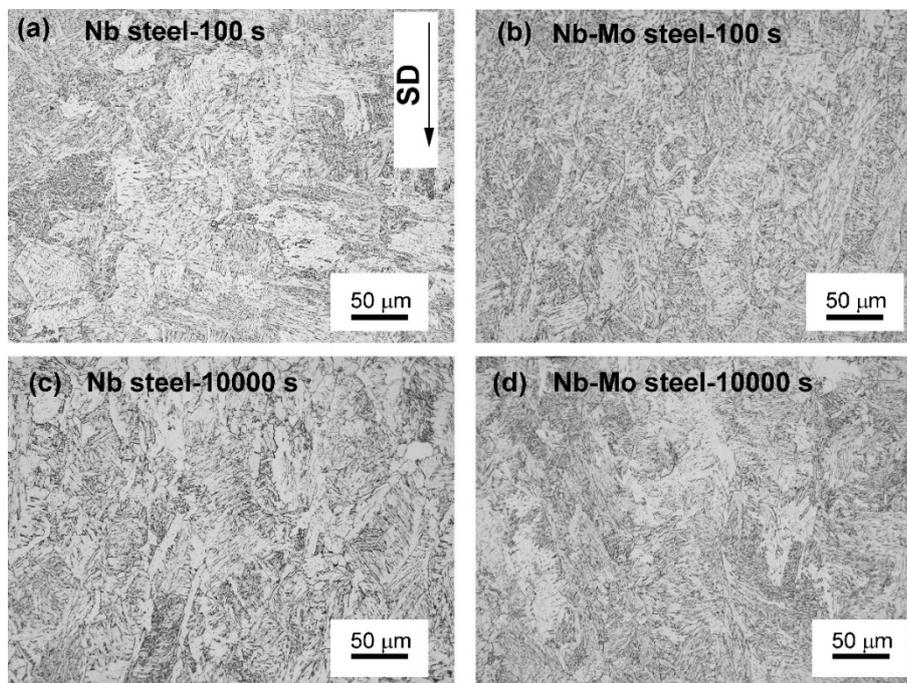


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2 **Figure 2** Hardness evolution of the Nb and Nb-Mo steels during coiling at 900 °C.3

3.2 Microstructure

4 The microstructure of the two steels coiled at 900 °C for 100 and 10,000 s were examined and shown in
 5 Fig. 3. Both microstructures are mainly bainitic, similar to the as-cast microstructure [16], however some
 6 grain boundary allotriomorphic ferrite formed in the Nb steel after 10,000 s coiling at 900 °C, but not in
 7 the Nb-Mo steel. The formation of allotriomorphic ferrite in strip-cast Nb-steel was already reported in
 8 an earlier study [13]. The allotriomorphic ferrite forms during the isothermal treatment at 900 °C, the
 9 bainite then forms upon cooling from the coiling temperature. For the case of the Nb-Mo steel, the
 10 suppression of the ferrite formation during coiling is due to the solute drag by Mo, which has been
 11 discussed in [16].



12

13 **Figure 3** Optical images of the microstructure of the Nb (a & c) and Nb-Mo (b & d) steels coiled for 100 and 10,000
 14 s at 900 °C. (Solidification direction (SD) is shown by the arrow.)

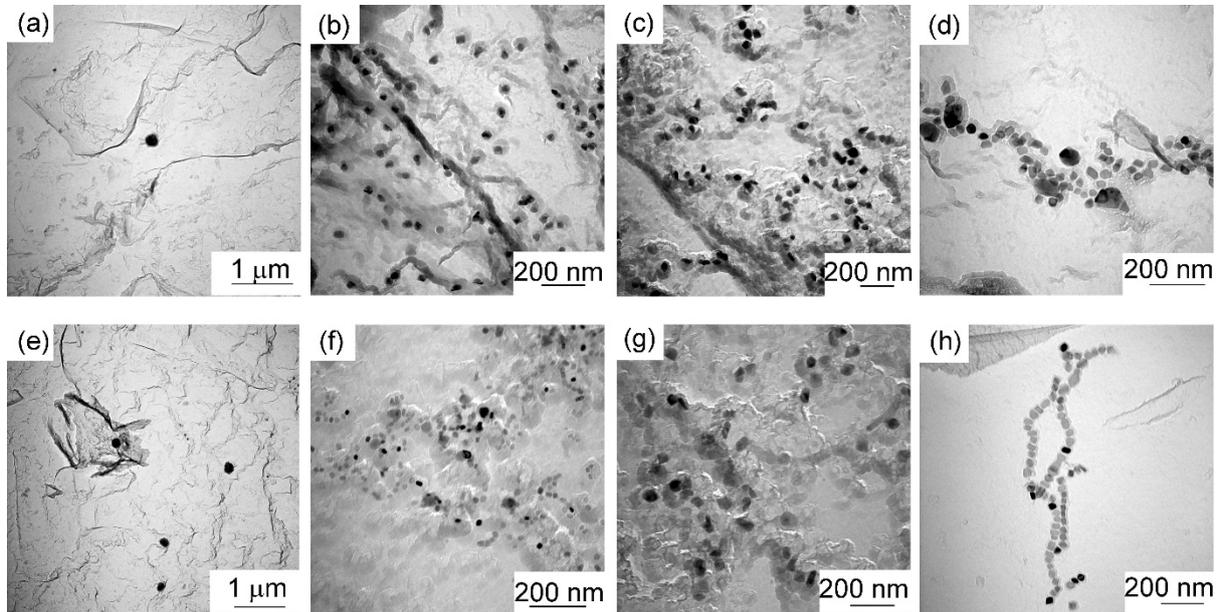
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3.3 TEM

16 Bright-field (BF) TEM images of carbon replicas produced from the Nb and Nb-Mo steels coiled at
 17 900 °C for various times are shown in Fig. 4. Precipitation does not occur after coiling for 100 s and only

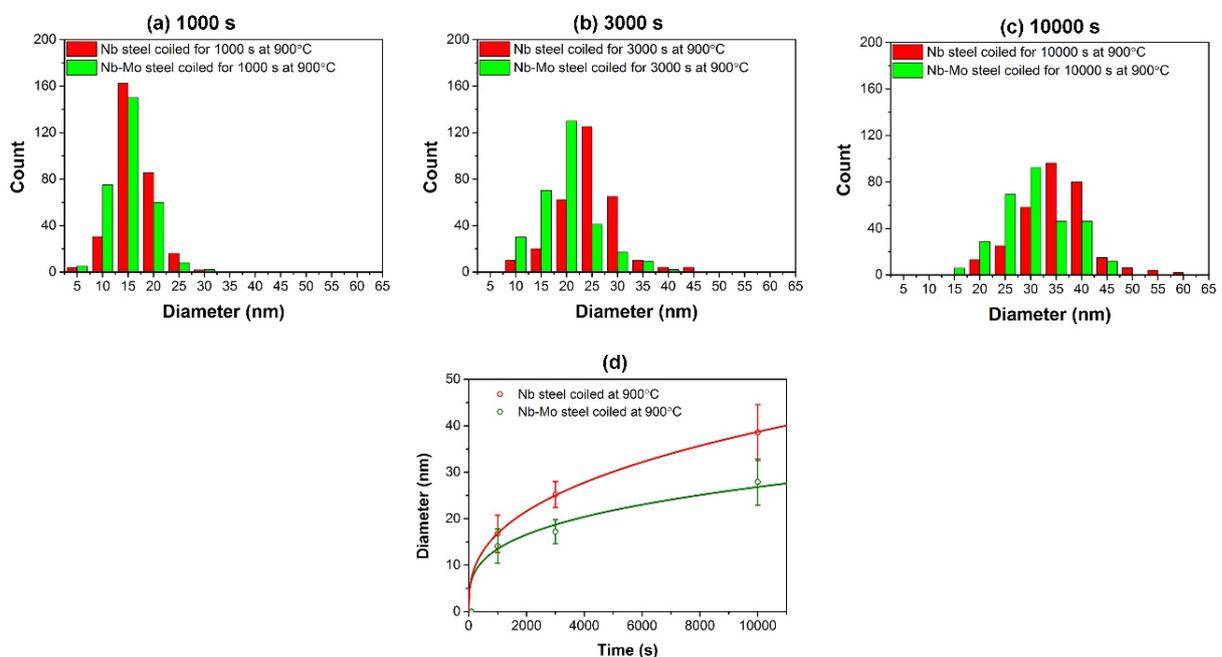
1 some coarse spherical particles around 250 nm in diameter are observed in both steels (Fig. 4 a & e).
 2 After 1000 s of coiling at 900 °C, precipitates are formed on grain boundaries and dislocations. From
 3 the Thermo-Calc calculation in Fig. 1, these precipitates are MC-type carbides. The size of the carbides
 4 in both steels increases as a function of coiling time, Fig. 5. Generally, the particle size in the steel
 5 containing Mo is smaller than that in the Mo-free steel.

6



7

8 **Figure 4** Bright-field (BF) TEM images of the carbon replicas of the Nb (a – d) and Nb-Mo (e – f) steels coiled at
 9 900 °C for 100 s, 1000 s, 3000 s and 10,000 s, from left to right. Note scale bar changes.

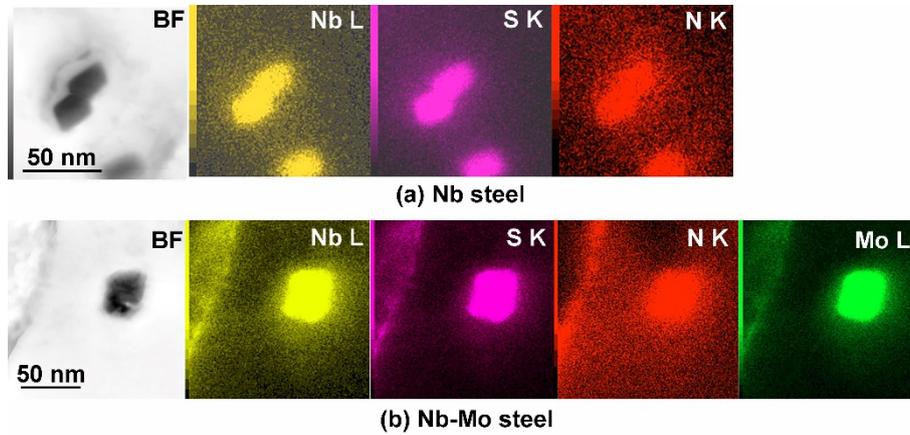


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11 **Figure 5** Size distributions (a – c) of the carbides in the Nb and Nb-Mo steels coiled at 900 °C for 1000 s, 3000 s and
 12 10,000 s, respectively. (d) is the average particle size evolution of the two steels during coiling at 900 °C.

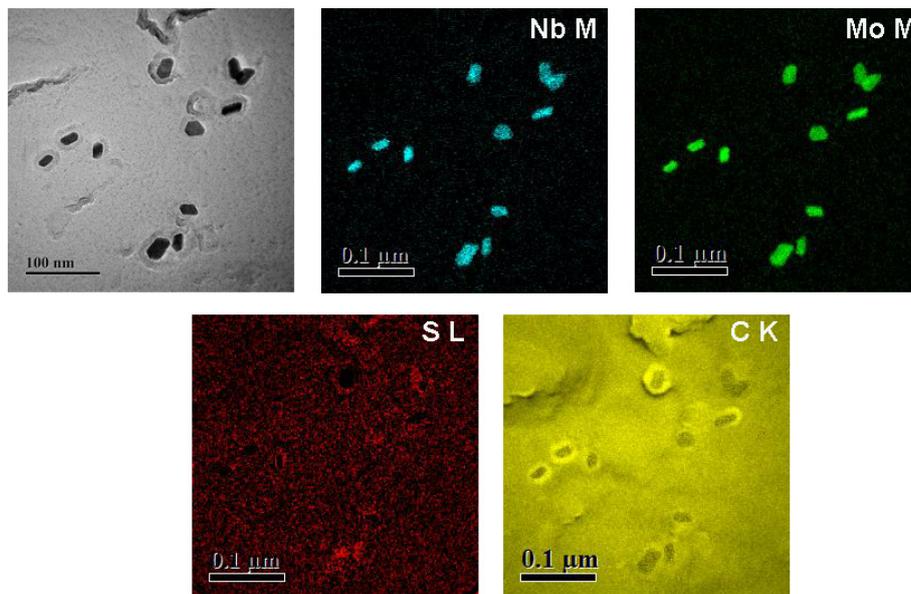
13 The compositions of carbides formed in both alloys coiled at 900 °C for 10,000 s were analysed by TEM-
 14 EDX, as shown in Fig. 6. The carbides in both steels are enriched in Nb, S and N. In the Nb-Mo steel,

1 the carbides also contain Mo. However, Nb (L), Mo (L) and S (K) peaks overlap in EDX spectrum, which
 2 presents difficulty for accurate compositional analysis of the carbides. Therefore, EELS was utilised to
 3 confirm the presence of Nb, Mo and S in the carbides, as shown in Fig. 7. The carbides in the Nb-Mo
 4 steel coiled at 900 °C are clearly enriched in Nb and Mo. However, whilst S is not identified to be present
 5 in all the precipitates, minor S segregation was observed at some precipitates. This result agrees with
 6 earlier reports of the presence of S in the Nb-carbonitrides formed in austenite [13].



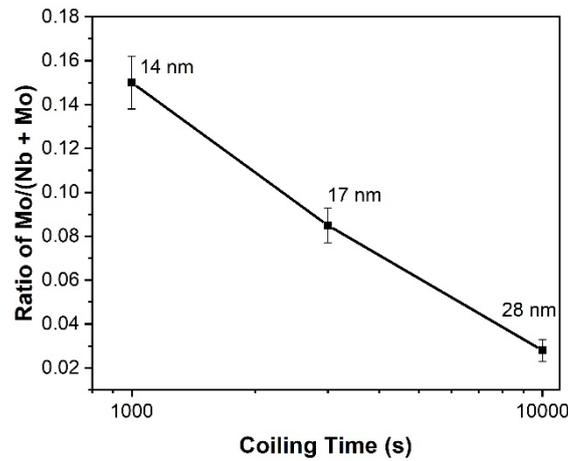
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 8 **Figure 6** Bright-field (BF) TEM image and corresponding EDX chemical maps for the carbon replicas of precipitates
 9 in the (a) Nb and (b) Nb-Mo steels coiled at 900 °C for 10,000 s.

10



11
 12 **Figure 7** EELS examination for the chemistry of the precipitates in the Nb-Mo steel coiled at 900 °C for 3000 s.

13 Based on TEM-EDX analysis, the Mo/(Nb + Mo) composition ratio of the carbides in the Nb-Mo steel
 14 coiled at 900 °C are presented in Fig. 8. It can be seen that the ratio significantly decreases with
 15 increasing coiling time and particle size. This suggests that Mo atoms play an important role during
 16 the nucleation at the early stages of the precipitation kinetics at 900 °C. As the precipitates coarsen,
 17 however, they are mainly enriched in Nb given the decrease in the Mo/(Nb + Mo) ratio as a function
 18 of coiling time. This growth mechanism can be rationalized by the difference in diffusivities between
 19 Nb and Mo [19-21].



1

2 **Figure 8** Mo/(Nb + Mo) ratio of carbides formed in the Nb-Mo steel coiled at 900 °C for various times.

3

4 **4. Discussion**5 *4.1 The effect of Mo on the thermodynamics of precipitation*

6 In the austenite region, the solid solubility products of NbC, NbN and MoC are obtained from [12, 22]:

7
$$\log[\text{Nb}] \cdot [\text{C}] = 5.43 - 10960/T \quad (1)$$

8
$$\log[\text{Nb}] \cdot [\text{N}] = 6.163 - 7583/T \quad (2)$$

9
$$\log[\text{Mo}] \cdot [\text{C}] = 4.96 - 12230/T \quad (3)$$

10 where, $[M]$ is the weight percentage of element M in solid solution. As (Nb, Mo) (C, N) carbonitride can
 11 be treated as a solution that is composed of NbC, NbN and MoC and having NaCl-type structure, the
 12 $(\text{Nb}_{k_1+m_1}, \text{Mo}_{k_2})(\text{C}_{k_1+k_2}, \text{N}_{m_1})$ formula was used in the present work for the thermodynamic and kinetic
 13 discussion. Here, k_1, k_2 and m_1 are the mole fractions for NbC, MoC and NbN and $k_1 + k_2 + m_1 = 1$.
 14 Through calculation, the equilibrium ratio of Mo/(Nb+Mo) at 900 °C is 0.00177, which indicates that the
 15 precipitates observed in this work were thermodynamically unstable and did not have an equilibrium
 16 composition, as shown in Fig. 8.

17 It is well-known that microalloyed carbonitrides formed in the austenite matrix typically keep a cube-
 18 on-cube orientation relationship with the matrix [22]. Therefore, the lattice misfit can be calculated as:

19
$$\delta = \left| \frac{a_{M(C,N)} - a_\gamma}{a_{M(C,N)}} \right| \quad (4)$$

20 where, $a_{M(C,N)}$ and a_γ are the lattice parameters for carbonitrides $M(C, N)$ and austenite, respectively.
 21 From the literature [22, 23], the austenite lattice parameter is taken here to be 0.36615 nm, and the lattice
 22 parameter for $(\text{Nb}_{k_1+m_1}\text{Mo}_{k_2})(\text{C}_{k_1+k_2}, \text{N}_{m_1})$ can be obtained by using the linear interpolation method
 23 [12]. The interfacial energy can be calculated as:

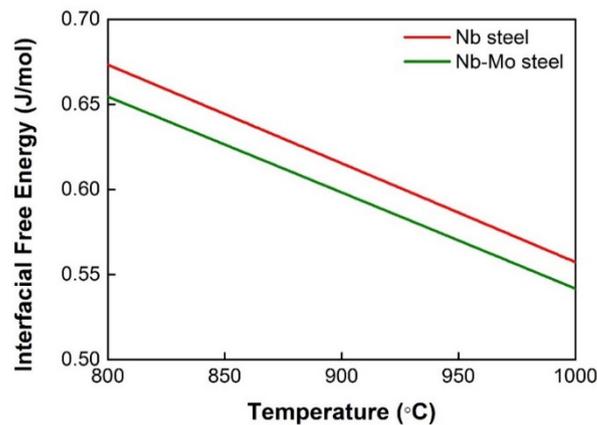
24
$$\alpha = \frac{Ea\alpha}{4\pi(1-\nu^2)} f(\delta) \quad (5)$$

25 where E is the elastic modulus (208.2 GPa [23]), ν is the Poisson's ratio (0.32 [24]) and

26
$$f(\delta) = \delta \left[\frac{2}{1+\frac{1}{4\delta^2}} - \ln(2\delta) \right] \quad (6)$$

27 Figure 9 shows the interfacial energy between the precipitates and the austenite matrix as a function of
 28 temperature. It can be seen that the precipitates in the Nb-Mo steel have a lower interfacial energy than

1 in the Nb steel when coiled at 900 °C. This is contrary to previous work that reported an increase in
 2 Gibbs free energy when adding Mo to MC precipitates [7, 25]. According to the classic theory of
 3 nucleation [22, 23, 26], the increase of Gibbs free energy (absolute value) reduces the driving force for
 4 precipitation, while the decrease of interfacial energy is beneficial for precipitation. Thus, there is a
 5 competition between the effect that Mo has on the Gibbs free energy and on the interfacial energy.
 6 The decrease in interfacial energy from Mo is responsible for the enhanced nucleation of the
 7 carbonitrides. This explains the high concentration of Mo in the precipitates at the early stages of
 8 precipitation and also the smaller size of the precipitates in the Mo-containing steel.



9

10 **Figure 9** Interfacial free energy of the precipitates formed in austenite for the two steels.

11 4.2 The effect of Mo on the coarsening kinetics of precipitation

12 The influence of Mo in the Ostwald ripening stage of precipitation was quantified using LSW theory
 13 [27, 28], which predicts the average size of particles when the volume fraction of precipitation is small:

$$14 \quad \bar{r}_t = \bar{r}_0(1 + k\sigma Dc_0t)^{1/3} \quad (6)$$

15 where \bar{r}_t and \bar{r}_0 are the average particle radius and nucleus radius, respectively. D and c_0 are the
 16 diffusivity and mole concentration of the controlling element respectively, t is the coiling time, and k is
 17 a constant parameter. The controlling element can be determined by the value of the product $D \cdot c_0$. At
 18 900 °C, $D \cdot c_{0-Nb}$ ($= 9.9 \times 10^{-17}$) is smaller than $D \cdot c_{0-Mo}$ ($= 4.3 \times 10^{-16}$) [21]. Thus, Nb is the rate-limiting element
 19 in both steels. Therefore, the coarsening of the precipitates in both alloys when coiling at 900 °C is
 20 dependent on the interfacial energy σ , which was lower in the Nb-Mo steel than in the Nb steel.
 21 Consequently, the coarsening rate of precipitates in the Nb-Mo steel coiled at 900 °C is smaller than
 22 that in the Nb steel, leading to a smaller particle size (Fig. 5). Additionally, as mentioned above, the
 23 diffusion of Mo between precipitates and matrix also slows the growth and coarsening of particles.

24 4.3 Precipitation hardening

25 A simple yield strength model was used to better understand the strengthening contribution from the
 26 precipitates. As shown in Figure 3, the bulk microstructure of both steels is very similar and mainly
 27 consists of bainite. For simplicity, we consider that the strength increment observed during coiling
 28 comes mainly from the precipitates. The equivalent yield strength is obtained by converting the
 29 hardness values as per the equation ($\sigma_y = 3.06H_v$) in [29]. After coiling for 100 s at 900 °C, the strength
 30 of the Nb-Mo steel increases by ~ 25 MPa, but no obvious change in the strength of the Nb steel occurs,
 31 which suggests that a small amount of very fine precipitates is formed, likely due to the lower interfacial
 32 energy from Mo (Fig. 9) that reduces the energy barrier to nucleation. However, no Nb-rich
 33 carbonitrides are seen in the Nb-Mo steel coiled at 900 °C for 100 s using the carbon replica
 34 preparation method (Fig. 4). This is probably due to the low extraction capability of carbon replica for
 35 the particles with diameters < 10 nm.

1 In recent work by Dorin et al. [13], the shearing to by-passing of the Nb-carbonitrides formed in the
 2 austenite was found to occur for a radius of ~ 6 nm. In the present work, the precipitates formed at
 3 900 °C are always larger and we hence assume that they will be by-passed by moving dislocations. As
 4 a result, the Friedel's statistical model for Orowan looping [30] can be used to estimate the strength
 5 increment from the precipitates:

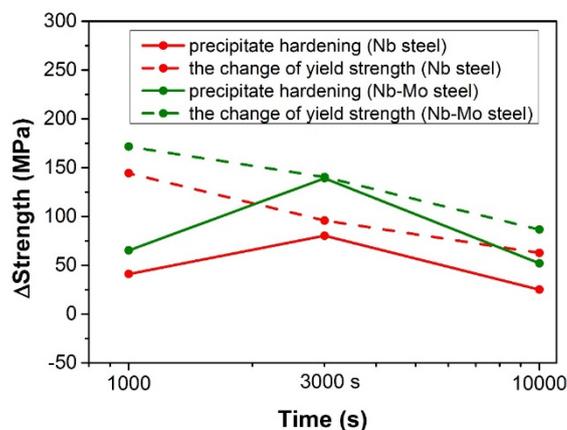
$$6 \quad \sigma_p = 0.7MGb \frac{\sqrt{f}}{R} \quad (7)$$

7 where M is the Taylor factor (~ 3), G is the shear modulus of ferritic matrix (~ 80 GPa [23]), b is the
 8 Burgers vector (~ 0.25 nm [23]), f and R are the volume fraction and the radius of precipitates. In this
 9 work, the maximum precipitation hardening at each coiling time at 900 °C was calculated using the
 10 theoretical volume fraction of Nb carbonitrides under equilibrium calculated by Thermo-Calc software
 11 with TCFE 9: Steels/Fe Alloys v9.0 database, 0.0605%, as shown in Table 2.

12 **Table 2.** Calculated precipitation hardening (MPa) by Orowan mechanism for the Nb and Nb-Mo steels coiled at
 13 900 °C.

Ageing time	Nb steel	Nb-Mo steel
1000 s	144	171
3000 s	96	140
10,000 s	63	87

14 The change in yield strength between the as-cast and coiled samples provides a direct measurement of
 15 the precipitate hardening for each sample. Figure 10 compares the measured precipitation hardening
 16 with the calculated precipitation hardening shown in Table 2. It can be seen that for both alloys the
 17 calculated and measured precipitation hardening at 3000 s are very close. For coiling times less than
 18 3000 s the measured strength is lower than the calculated strength, and this is probably because the
 19 volume fraction is lower than the maximum. This means that there is still solute available after 1000 s
 20 of coiling at 900 °C. After 3000s, the LSW prediction agrees reasonably well with the experimental
 21 strength determined from the hardness measurements. For the longest coiling time, the precipitation
 22 hardening reduced, which was due to the growth and coarsening of precipitates. Additionally, at 10,000
 23 s, the measured yield strength is slightly lower than the calculated strength, which probably because
 24 after a long time coiling the concentration of carbon in solid solution decreases due to precipitation,
 25 resulting in lower solid solution strengthening. Furthermore, the coarsening of austenite grains and the
 26 formation of allotriomorph ferrite (Figure 2) after a long time coiling may also contribute to the drop in
 27 the measured strength.
 28



29 **Figure 10** Comparison of the precipitation hardening using the maximum theoretical volume fraction and the
 30 change of yield strength for both steels coiled at 900 °C.
 31

1 5. Conclusions

2 In the present study, the effect of Mo on the precipitation behaviour in austenite in low-carbon strip-
3 cast steels containing Nb has been investigated. The key conclusions are as follows:

- 4 (1) The hardness values of both as-cast steels were similar. During coiling at 900 °C, the hardness
5 of the two steels increased and reached the peak at 3000 s, then decreased after 10000 s coiling.
6 Generally, the Nb-Mo steel had higher hardness than the Nb steel at all coiling times.
- 7 (2) The microstructures of both steels coiled at 900 °C were bainite, only some grain boundary
8 allotriomorph (GBA) were formed in the Nb steels coiled for 10,000 s at 900 °C.
- 9 (3) Nb-carbonitrides precipitated in both steels after coiling for 1000 s at 900 °C, and the size of the
10 particles in the Nb-Mo steel was finer than that in the Nb steel. In the Mo-containing steel, Mo
11 also participated in the precipitation, and the concentration of Mo in Nb-rich carbonitrides
12 decreased with increasing particle size and coiling time.
- 13 (4) The enrichment of Mo in the Nb-rich carbonitrides reduces the interfacial energy between
14 precipitates and the matrix, which lowers the nucleation energy barrier and the coarsening rate
15 of precipitates.
- 16 (5) Strength modelling suggests that precipitation reached maximum volume fraction (0.0605%)
17 after coiling at 900 °C for 3000 s. The precipitates in the Nb-Mo steel imparted an increase in
18 strength up to ~140 MPa, which was much higher than that in the Nb steel, ~96 MPa. Further
19 strengthening contributions of the precipitates in both steels decreased after 10,000 s coiling at
20 900 °C due to the coarsening of the particles.

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