Reliability of Seismic Performance Assessments for Individual Buildings and Portfolios

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Abstract: Seismic performance and loss assessments can have widely varying degrees of uncertainty. An essential issue is whether a particular assessed seismic loss or performance result has sufficient reliability to serve as the basis for risk management decisions and actions, including whether or not a code prescribed performance level is met, or if an assessed loss level is acceptable. A method is developed measuring the reliability of performance and loss assessments for individual buildings and for portfolios. Consideration is given to how well the building investigation and corresponding evaluation process have been performed, the qualifications of the person(s) doing the assessment, the thoroughness of the evaluation, and the technical validity of the assessment procedure or model. The approach characterizes the uncertainty of each component of the assessment procedure for each building in qualitative terms. The resulting reliability measure is likely to be most useful for the cases where an entity is determining whether/or not a building has acceptable life safety performance, or if a portfolio has an acceptably low risk of seismic damage loss over a given period of time. In both cases, the reliability must either be sufficient to warrant action, or serve to indicate need for improved assessment.

Keywords: Reliability, Earthquake damageability, Structural evaluation, Safety, Financial risk, MC simulation

1 Reliability of building seismic performance evaluations

Many private owners and public institutions have taken steps to ensure that the seismic risks posed by their respective buildings are assessed and mitigated if necessary. Real estate investors and financiers often limit their investments to properties that have limited down-side risk, which may include insurance. Parts of these financial decision processes may depend on the assessed seismic risk posed by a building, and therefore the reliability of this assessment is of key concern. Often the questions at issue involve: whether a building meets the applicable Building Code or an owner/entities' requirements for stability/life safety performance; or, if the building's probable maximum loss (PML) is less than a given acceptable value. These questions are applicable to both individual buildings, and portfolios of multiple buildings that are locally or geographically dispersed.

There is inherent uncertainty in the reliability of the results of all professional evaluations, including seismic performance assessments. This general condition has been well-stated by Justice Roger J. Traynor in 1954:

Those who hire (professionals) are not justified in expecting infallibility, but only reasonable care and competence. They purchase the service, not insurance. (Traynor, 1954)

This is a recurrent theme in California Law applied to professionals performing work for a client, and of course it applies to those performing seismic performance evaluations. We are led to believe that this observation is universal. It is in the best interests of the client to determine how reliable a report will be or is, and the client should not rely on the professional's liability insurance to right the losses due to wrong decisions that may be

made upon the basis of the report if it were to be incomplete or wrong. Liability insurance is an unreliable method as a risk mitigation measure. This paper addresses exactly this problem: How can the reliability of a seismic performance assessment be evaluated? The recommended procedures address the following issues for both single and portfolios of buildings:

- Quality measured by the acceptable reliability or level of uncertainty of the reported seismic performance assessment.
- Confidence limits for reported assessed numerical loss value: where these limits
 are based on the assessor's statement of uncertainty together with the uncertainty
 in the analytic methods, available information, and the investigation procedures
 employed and data processing procedures used.

ASTM E2557 and E2026 provide standards for the assessment of seismic risk (PML) statistics for individual and locally compact groups of buildings, and a current ASTM Working Group is developing similar standards for portfolios of geographically distributed buildings located within defined seismic hazard zones. These standards are widely used, primarily by the financial industry, for the evaluation of the damageability risk of buildings being considered for real estate investments or securities evaluations. Accordingly, ASTM E2026 seismic risk assessments describe varying degrees of investigation of a building or group of buildings ranging from Level 0 (a screening or "desk top" investigation) to Level 3 (a highly detailed technical investigation and analytical evaluation). Having these descriptions, the user-client can prescribe the level(s) of investigation concerning building stability (BS), site stability (SS), building damageability (BD), contents damageability (C), and business interruption (B) according to the user-client's acceptable reliability or tolerance for uncertainty.

The ASTM standards state that the selection of the level of investigations performed should be guided by the acceptable level of uncertainty. The lower the tolerance for uncertainty, the higher the level of investigation should be. Also, the higher the seismic hazard of the region in which the building is located, the higher the level of investigation should be, all other things being equal. Of course, the cost and time of performing an investigation increases with the level and therefore the choice may be limited by the user's resources. For a given assessment based on a defined investigation level, this paper provides a method of determining a quantitative and qualitative measure of the related uncertainty and corresponding reliability, ranging from SUPERIOR to POOR. The method describes the means of expressing and combining both quantitative and qualitative information related to the components used in the assessment process. It is important to recognize that the ASTM standards do not provide an enforcement mechanism, therefore, there are essentially no controls or limitations on providers. The User hires a professional to perform a level of review as specified in the Standards, then relies on the same professional to indicate that they actually complied with the level, however there are NO consequences if the professional did something less. As a result, it is left up to the user/client to evaluate the reliability of the application of the methods and conclusions and to determine whether the provider has employed the necessary technical knowledge and care to perform the assessment. It is the responsibility of the user to apply and/or require quality assurance steps before using the results, or otherwise possibly suffer the consequences of making decisions based on non-reliable assessment results. The reliability is dependent on many factors, few of which may be mentioned or even considered within the evaluation report itself. This condition also applies to risk measures concerning portfolios of buildings. If the reliability is determined to be insufficient, then further investigation and analysis may be required before a responsible decision can be made based on reported findings.

FEMA P-154 and ASCE 41 are widely used tools for the evaluation of a building's expected seismic performance, and either/or both may be employed. Often the decisions for investment and use, as well as retrofit of buildings, are made that rely on the results of these tools. For both FEMA P-154 and ASCE 41, there is a need to be able to determine the reliability of the reported evaluations in order to ensure that risk management

decisions are made that are consistent with a knowledge of the degree of possible variability of the evaluation.

Performing an engineering study of an existing building can be an expensive and time-consuming process. FEMA P-154 and the ASCE 41 Tier 1 Check List Form evaluations have the advantage of being significantly less costly than a full engineering assessment of a building (such as FEMA P-58 or ASCE-41 Tier 3). A P-154 assessment is based on: the identification of certain building characteristics and risk issues, scoring these against a checklist, determining a cumulative score, and comparing this value to a prescribed acceptable score for life safety performance, such as 2.0 or more as a score. P-154 allows the assessor to rate the degree of each of the key damageability issues on the Level 1 Form, and permits the assessor to make some adjustments by means of a Level 2 Form. The adjustments are based on a more detailed description of the characteristics that affect the building's expected performance. This is most useful to justify that a building is acceptable even though its initial Level 1 tabulated score is less than 2.0 or other values depending on the level of seismic hazard of the site, with higher values for less risky sites. Alternatively, the Level 2 Form can serve to provide detailed information that can lower or raise the score from that of the Level 1 Form, providing some additional reliability of the result.

An ASCE 41 assessment can be performed at different Tiers ranging from Tier 1, which is a low-intensity evaluation using Checklists, to Tier 3, which requires significant engineering investigation and analysis. The results of the Tiers are evaluated based on three possible outcomes for a given performance issue: Compliant, Not Compliant, and Not Applicable. If any issue is found to be Not Compliant, then the Tier is considered to fail, that is, the building does not comply with the ASCE 41 requirements. Tier 1, the lowest assessment level, was designed to have a small probability that the result would call a BAD building GOOD (a Type I error consistent with common decision theory practice), and a higher probability that it would call a GOOD building BAD (Type II error). In effect, the ASCE 41 Tiers 1 though 3 provide a triage system, where if a building fails one Tier, then the next one can be performed, which is more intensive and may change the previous conclusion. The assessment tends to stop when the assessor is convinced that either no more information is likely to change the conclusion, or the resources for this purpose are exhausted. It is well established in the literature that the policy decision to minimize Type I errors, without considering the consequences of Type II errors is ill-advised. This is because the probability of a Type II error goes up as the probability of a Type I error goes down, (Benjamin and Cornell, 1970) – obviously the only effective way to avoid Type I errors is to do nothing. Therefore, we are led to the conclusion that when ASCE 41 Tier 1 assessments are to be used for making decisions regarding a building's acquisition, occupied use period, and/or a retrofit investment, it is necessary to determine the reliability of the ASCE 41 Tier 1 Performance Level assignment. If the reliability is too low (uncertainty too high) for the decision-making process, then it is necessary either to abandon the project, or to invest in a higher-level assessment. In recognition that acceptable reliability is key to the decision process, in this paper a method to regularize the evaluation of reliability is developed rather than just asking an expert or experts for their opinion. The method proposed provides documented support for conclusions concerning the assessment's reliability. For seismic safety purposes, it is obvious that calling a BAD building GOOD can have significant consequences. Whether a P-154 or an ASCE 41 evaluation has been or will be performed, there is the fundamental issue of what the reliability of the evaluation is and whether a responsible decision can be made based this evaluation. We will discuss the reliability process in terms of ASCE, FEMA and ASTM procedures. However, the issues involved in these evaluations are essentially the same, since these procedures result in a binary decision whether a building's seismic performance is either acceptable or not acceptable for the performance objective of life safety. In addition, the evaluation of the reliability of results from proprietary PML and Portfolio Risk (often called Catastrophe Models, or CAT, discussed in Section 3.1) procedures will be treated.

Before proceeding to the Assessment Reliability procedure, it is helpful to understand the current general process of solving Engineering and Economic problems. These problems, including those of reliability, risk, and decision making, without exception, are solved within the confines of a model universe. This universe contains the set of physical and probabilistic models (with assigned parameter values), which are employed as mathematical idealizations of reality to render a solution for the particular problem at hand. The selected model may contain inherently uncertain quantities or components, and furthermore, may be made up of sub-models that are invariably imperfect representations of reality, giving rise to additional uncertainties. Since the selection of a specific tractable model is necessary to solve the problem, an important part of formulating the complete model involves the representation of the related uncertainties such that some measure of the reliability of a predicted outcome is available. Any selected method of this representation of the nature and character of uncertainties should be stated within the confines of the selected model. While there can be many sources of uncertainty, in the context of modeling, it is convenient to categorize the character of uncertainties as either aleatory or epistemic. The word aleatory derives from the Latin word meaning the rolling of dice. Thus, an aleatoric uncertainty is one that is presumed to be the intrinsic randomness of a phenomenon. The word epistemic derives from the Greek meaning knowledge. Thus, an epistemic uncertainty is one that is presumed as being caused by lack of knowledge (concerning actual behavior or a lack of sufficient data for an adequate empirical representation). The reason that it is useful to have this distinction of the uncertainty sources within the context of an engineering analysis model is that the epistemic lack-of-knowledge-part of the uncertainty can be represented in the model by introducing auxiliary non-physical variables. These variables capture information obtained through the gathering of more data or use of more advanced scientific principles and/or more detailed analyses. An uttermost important point is that these auxiliary variables define statistical dependencies (correlations), between the components of the model, in a clear and transparent way, (Der Kiureghian, Ditlevsen, 2009). For example, if the random errors in prediction of a damage ratio were to be assumed (by the modeler) to have a Normal Probability Distribution (perhaps for tractability or ease of presentation) where the true error distribution is actually best represented by a Beta Distribution; this would be a source of epistemic error. When the corresponding mean and variance parameters of an assumed Probability Distribution function are evaluated by sample estimates that are based on a smaller sample of observations than the number required to obtain an acceptable range of confidence limits for the true parameter values, this would be classed as aleatory error. Whereas epistemic uncertainty can be reduced by acquiring knowledge and information on the system, and so can aleatoric uncertainty to a degree by use of more appropriate PDF and parameters, in practice, systems under analysis cannot be characterized exactly—the knowledge of the underlying phenomena is incomplete. This leads to uncertainty in both the values of the model parameters and on the hypothesis supporting the model structure. This defines the scope of the uncertainty analysis which we shall investigate herein.

The problem at hand is how to characterize the uncertainties caused by epistemic decisions (modeling assumptions and prediction equations) that formed the analytical basis of how the portfolio loss statistics. These assessed uncertainties will be evaluated by the Qualitative – Quantitative Matrix system that will be discussed in Section 2.2. We choose to call this the *epistemic* portion of the uncertainty or Reliability Level. It is assumed that the aleatoric (sample size) error in assigned parameter values and resulting portfolio loss statistics will be controlled by the corresponding sufficiently large number of Monte Carlo simulations employed in the CAT model as discussed in Section 4. It is important to mention that each building in the portfolio is to have quantitative representation of the uncertainty of its damageability characteristics. Further, as a derivative question, if the level of uncertainty of the assessed result is not acceptable, what steps can be taken to make the level acceptable (e.g., further investment in higher levels of investigation,

particularly for high value buildings)? The uncertainty contribution of each component can serve to guide this resource allocation decision.

The reliability of an assessment depends on the validity of the assumptions and idealizations of the components employed in the assessment. Specifically, the quality of information concerning the components of the assessment and the validity of assumptions used in the prediction model can significantly impact the performance conclusion; however, these impacts are not normally considered as part of the uncertainty assessment of the conclusion. These unconsidered or un-mentioned sources of uncertainty must be identified and included in the total representation of the reliability of the results. An example, using Qualitative Terminology concerns the level of information used to represent an individual building's damageability characteristics. This information can be obtained from: a building visit by an experienced evaluator (GOOD), a review of the construction documents by an experienced Structural Engineer (GOOD), or simply a Desktop assessment based in inferred characteristics of the building from photographs (POOR). In summary, there are alternatives (such as the ASTM E2026 levels of investigation) in the data collection, parameter specification, and damageability analysis methods that can have a significant effect on the assigned performance level or loss assessment. The purpose here is to provide a method by which a user can evaluate the reliability of the results by assigning and combining the uncertainties corresponding to the components or steps involved in a given assessment process.

The proposed method in this paper allows for representation of uncertainty for each of the individual issues or components in a loss assessment process, along with their combination for the total uncertainty of reported results of the process. The development the reliability of the damageability quality assessment process for one building or portfolios of buildings are discussed in the following sections:

- Section 2 addresses the quality of the individual building damageability
 assessment. The quality of the algorithm that determines the loss for the building
 or portfolio of buildings in a single assumed earthquake event is discussed. This
 will be required of a single building if that is all that is being assessed, or for each
 of the buildings in the all under consideration, or each of the buildings in a
 portfolio. It forms the basis on which all evaluations are completed.
- Section 3 discusses the concept of Portfolio Loss and its respective loss statistics,
 together with the practical need for Monte Carlo Simulation for the evaluation of
 the risk of aggregated loss due all possible Earthquake Events in the defined
 seismic region. The concept of "Bootstrap" sampling is introduced for the nonparametric statistical analysis of Monte Carlo simulations as a way to understand
 the uncertainty of a specific loss value.
- Section 4 addresses the uncertainty issues in determining the computed loss
 estimates for portfolios. These statistics are evaluated from the results of Monte
 Carlo simulations that aggregate the loss estimates of the portfolio for all possible
 earthquakes that can occur (the Event Set) and the representation of the statistical
 variability of how each of the individual buildings respond to these events.
- Section 5 addresses the evaluation of the uncertainty of reported portfolio loss assessment values to reflect both the *aleatoric* uncertainty of the computation process and the *epistemic* quality of the assessment process as a whole. Epistemic means in this context: Of or pertaining to knowledge or the conditions for acquiring it, (Halpern, 2017). Finding reliability for these possible individual issues allows characterization of the reliability of the total process. This will give not only the evaluation of the reliability of the findings, but also suggestions of ways that the quality of the results can be efficiently improved by altering some aspects of how the process is undertaken. Also, the descriptive identification of the issues and related sources of uncertainty can be employed before the assessment is performed in order to ensure that the assessment will provide results of sufficient reliability to make decisions.

2 Assessing an Individual Building

2.1 Key issues impacting reliability of an individual building assessment

The evaluation of the representation of uncertainty for a loss assessment for an individual building requires a careful identification and consideration of all of the issues and elements, herein termed as *components*, that can contribute to this uncertainty. For the evaluation of the uncertainty measure for each component in the assessment process, we are interested not only in the technical descriptive characteristics of the component but also the temporal currency and reliability of the observations as represented by the skill, expertise and experience of the person(s) involved in implementation and/or evaluation of the component. Both the technical characteristics and the quality of the assigned values impact the reliability of the results. It is proposed that the most efficient method of characterizing the reliability of the results of an assessment report is by the evaluation of the uncertainty of the individual components of the building assessment, and then combining these uncertainties to quantify the total uncertainty and corresponding reliability of the resulting assessment. The problem of combining qualitative terms that express degree of uncertainty will be addressed in Section 2.3. The following *Issues* are considered to be important for evaluation of individual building performance assessment:

- 1. **Seismic Exposure**: The characterization of the severity of the seismic hazards at the building site, including: intensity and related risk of damaging ground motions; surface faulting, liquefaction-induced settlement; and landsliding.
- Design Basis: What were the seismic design criteria under which the building was
 designed, and/or retrofitted or otherwise altered since construction? This includes the
 seismic requirements as well as the standard of practice used.
- 3. Quality of Evaluation Information and related Assessor: Were the design and/or modification retrofit documents available for review? Did the qualifications of the assessor meet ASTM 2026 guidelines for Senior Assessor? Was the building visited by the assessor?
- 4. *Configuration and Load Path*: What are the vertical and horizontal irregularities of the structure? Does the lateral load-resisting system accommodate any irregularities? Is there an effective load path? Does the detailing of the lateral load resisting system provide adequate ductility to accommodate expected demands? What is the potential collapse mechanism? Is this mechanism capable of sustaining the ASCE 7 Design Level Earthquake (2/3 MCE_R) or ASCE 41 BSE-2E displacements without collapse? (ASCE 7, ASCE 41)
- 5. Compatibility: Are the deformational characteristics of the building's structural and nonstructural elements compatible with the expected seismic drifts? Is there any unintended interference from other stiff elements that could cause failure of critical support elements?
- 6. *Condition:* Are the structural elements in good condition or deteriorated? Are any deteriorated elements important to the seismic resistance and stability? Is there any damage due to past earthquakes, accidents, or fires, and is this damage important to the seismic resistance?
- 7. Building Location: The specificity of how the location of the building is determined, such as by address, city, county or ZIP code, can greatly impact the reliability how the earthquake site and seismic ground motions are determined and whether these hazards are representative of the site. Having an accurate location for each building is critical not only to determine the individual building's locations with respect to the hazards that are posed, but also to assure that building is not systematically mislocated.
 If the assessment includes a loss estimate, such as damage ratio, or dollar loss, then also assess:
- 8. **Building Damage Determination:** How were the damageability values determined for given intensities of site ground motion? What model is used, and what is its basis? Does the model report a damageability probability distribution function for the results or a single value? If the results are expressed as a probable loss, is it specifically defined as an ASTM E2026 scenario loss (*SML*, *SEL*, *SUL*)¹ or a probable loss *PL*.

ASTM E2026 defined Scenario Loss as: Scenario Loss (SL) is the earthquake damage loss expectation to building systems and site improvements and where User-prescribed, building contents and/or related business interruption loss, associated with specified earthquake events on specific fault(s) affecting the building. SL values are expressed in terms of the damage ratio or damage cost/repair cost in present day dollars. The SL is generally limited to earthquake loss associated with the earthquake

9. Building Replacement Construction Cost: The replacement construction cost is the basis for almost all building damageability loss assessment procedures. The damageability loss is evaluated for a given event by multiplying the corresponding computed damage ratio times the building replacement construction cost. The Market value of a building is not a reliable indicator of building replacement construction cost. (Where other issues, such as contents damage, lost rents and revenues are considered, all contributions should be expressed in dollars.)

2.2 Evaluating reliability for individual building assessments

The Quality Rating System method proposed here is analogous to that used in FEMA P-695 (FEMA P-695, 2009, Section 3.4, also known as ATC-63). The individual component uncertainties are represented by their assigned Coefficients of Variation (β factors). For a building performance prediction Equation (such as for the P-695 collapse fragility, or for here, as the damage ratio) that can be represented as a product of multiple components, the uncertainty contribution due to an individual component can be represented by a random multiplier on the estimated system value. Therefore,

- The total uncertainty is the result of a chain of multiplication of the uncertainty of individual components that make up the decision process.
- Each uncertainty multiplier is assumed to have a lognormal distribution with mean one and standard deviation β_i . This is quite *convenient* in practice. For instance, β_i = 0.1 indicates a roughly ±10% change ($e^{0.1}$) of the estimated parameter, or β_i = 0.2 indicates roughly ±22%, etc. This provides an intuitive understanding why the total β for the process can be represented as the Root Mean Square (RMS) of component β_i values, see Section 2.3.

These component β_i factors can be estimated without the need of knowing the mean or median values of the respective underlying components. The final combined index must include uncertainty measures for all the components that impact the reliability of the assessment value or score. This value or score is used for the binary conclusions: *The building either meets the criteria of the specific requirements used procedure or does not,* or, the assessed loss value is too high to proceed with an action. The method of aggregation of the uncertainty indices for all of the components of the building assessment will be discussed in Section 5. The following are the seven individual components identified as having a significant impact on the overall reliability of a damage assessment. This assessment may in terms of: a PML value (defined and discussed below), an evaluation score from a P-154 assessment, an Earthquake Performance Level (I to VII) in terms level of compliance to CEBC requirements, or a deficiency list of demand/capacity ratios for individual elements of the structure from ASCE 41 Tier 3 analysis.

The reliability evaluation process used in this paper is an extension of a procedure used in FEMA P-695 to estimate the reliability of a *Structural Performance Behavior Evaluation Process*, (Deierlein, et al, 2008). Specifically, the problem involved the prediction of building collapse displacement or fragility due to earthquakes, using the results of nonlinear time history analyses of selected examples of proto-type building structural systems. The key questions addressed were; *How to assign quality measures of the factors, used in the calculation of collapse displacement,* and *How these quality of knowledge measures can be combined to relate to the certainty (reliability) of the results of the collapse displacement estimation process?* For a given factor (or component) used in the collapse estimation

ground-shaking hazard, but may include losses from other earthquake hazards, as prescribed by a User. Scenario Expected Loss (SEL) is the expected value of the scenario loss for the specified ground motion of the earthquake scenario selected. Scenario Upper Loss (SUL) is the scenario loss that has a 10% percent probability of exceedance due to the specified ground motion of the scenario considered. To these we add the Scenario Median Loss (SML) is the loss in the specified scenario earthquake that has a 50 percent probability of exceedance. ASTM defines *Probable Loss (PL)* as: earthquake loss to the building systems that has a specified probability of being exceeded in a given time period, or an earthquake loss that has a specified return period for exceedance. A PL value is meant to reflect, in a statistically consistent computational manner, all of the epistemic uncertainties that can impact damage estimates, including when and where earthquakes occur and with what magnitude, attenuations of ground motions at the site, local site effects and performance of the building systems in this ground motion. (ASTM E2026-16a)

Table 1. Assessment matrix for the implementation application of a quality measure for a considered issue or component. Each of the assignments of High, Medium and Low is described by text specific to the component under discussion. A value of 0.10 is taken as the very reliable, (little uncertainty), and 1 is not reliable (complete uncertainty). This Table is the same for all Quality Measures.

	Implementation		
Quality	Characteristics		
Measure	High	Medium	Low
Llich	SUPERIOR	GOOD	FAIR
High	β = 0.10	β = 0.20	β = 0.35
Medium	GOOD	FAIR	Poor
Medium	β = 0.20	β = 0.35	β = 0.50
Low	FAIR	Poor	Bad
LOW	β = 0.35	β = 0.50	β= 1.00

Table 2. Reliability qualitative terminology and their associated uncertainty quantitative values. When a β value has been determined quantitively, we propose to use the numeric bounds for assignment of a qualitative linguistic term for the value

Qualitative	Quantitative β value			
reliability	Assigned	Lower	Upper	
term	value	bound	bound	
Superior	0.10	0.000	0.150	
GOOD	0.20	0.150	0.275	
FAIR	0.35	0.275	0.425	
Poor	0.50	0.425	0.750	
Bad	1.00	0.750	1.000	

process, a measure of uncertainty (a β value: $0 < \beta < 1$) was assigned corresponding to three qualitative levels of Quality of Description of the factor (High, Medium and Low) and three levels of its assessed Quality of Implementation Characteristics (High, Medium and Low). FEMA P-695 Section 3.4 presents a simple matrix, shown in Table 1, that provides a single quantitative evaluation of β based on the paired qualitative assessments of: Quality of Implementation (High, Medium, Low) corresponding to a specific description Quality of Component *Description Measure* (High, Medium, Low). The lower the β value, the greater the certainty (reliability) of the result; conversely, the higher the β value, the lower the certainty (unreliability). The means of assigning the required quality measures shall become clear in Table 3 that presents matrices for how the pairs of quality for each of the nine components are assigned. An analytically determined numerical value of β can be expressed as a qualitative linguistic term by use of Table 2 following the numerical upper and lower bounds for each term in the assignment of the linguistic quantitative term. The β values of Table 1 are the same as used in P-695 with the exception that P-695 did not make an assignment of a (Low, Low) value, which we call BAD and assign a β =1.0.

A most important advantage of being able to assign a quantitative uncertainty factor β_i for each component i used in an evaluation process (analogous to the FEMA collapse displacement as described above), or for our objective of building loss assessment, is that these quantitative β_i values ($0 \le \beta_i \le 1$) can be combined in a statistically valid procedure to provide the total uncertainty of the result of the evaluation. This was done as discussed above by assuming that the uncertainties are multiplicative in their impacts, and lognormally distributed with mean one. The multiplicative process of lognormal standard deviations of the individual components to be combined as the standard deviations as the Square Root of the Squares; and it does not need knowledge of the mean. It is essential to note that the combinatory process would be quite subjective if the levels of uncertainties were to be left in Qualitative terms.

For the proposed method of evaluating the uncertainty of an assessed damageability or a related Performance Level, the approach described above for the assignment of qualitative uncertainty expressions by the matrices of Table 3 here and similar tables elsewhere, and the corresponding quantitative βi factors by Tables 1 and 2 is necessary because building damageability assessments are based on varying degrees of professional knowledge and related judgements. The expression of the likelihood for building response and the corresponding degree of uncertainty is based, primarily, on the experience and qualifications of the assessor and on access to information available concerning the specific characteristics of the building and related seismic risks. For a particular building, detailed engineering analyses and on-site materials testing and investigation (such as ASTM E2026 Level 3 investigations) are usually not feasible. Also, actual seismic performance data for current building types is not sufficient to provide accurate empirical prediction. As a consequence, it is necessary to utilize expert judgmental qualitative values as a major basis for loss assessments. At best, these judgmental values are based on experience and information obtained from building construction documents and/or a building visit when possible. Table 2 gives a simple qualitative ranking based on qualitative terms SUPERIOR, GOOD, FAIR, POOR, and BAD and their corresponding (judgmentally assigned) qualitative uncertainty measures (β values). The number (five) of the qualitative terms of Table 2 has the benefit of being odd such that there is a subjective middle or neutral representation for judgement heuristics. Table 1 gives how the β values can be assigned where two descriptors Quality Measure and

Implementation Characteristics, refer to the matrices of Table 3, rather than one judgmental choice made concerning a particular issue, component, or step involved in the assessment process where Table 2 applies.

For a particular building assessment, the β values of the Table 1 should be considered as starting values that may be modestly adjusted if the resulting uncertainty evaluation is clearly between the matrix values for a specific use. For example, the assignment of an interim value of 0.275 if the judgement is that an assessment is better than FAIR and less than GOOD, or 0.25 if it is closer to GOOD than to FAIR. Also note that when a particular evaluation from Table 2 is not sufficiently reliable for the user/client's purpose, additional analyses and/or investigation expenditures can serve to reduce the initially high β value such that an acceptable total reliability can be achieved. In many cases it may not be clear that definitive choices can be made in the Table 1 assignments. If we designate the probability of the Quality Measure as P_j for the three Measures j = H, M and L, and as probability Q_k for the Implementation Characteristics, and β_{jk} be the corresponding β value in Table 1 for row j and column k, then the appropriate combined β_i value is determined as:

$$\beta_i = \sqrt{\sum_{j=1}^3 \sum_{k=1}^3 P_j Q_k \beta_{jk}}$$
 (1)

This simple average approach is used to determine the assigned value since we are in essence interpolating between the β values of the component matrix. For example, if the *Quality Measure* was assigned as *MEDIUM* with probability 100% and the *Implementation Characteristic* High with probability 75%, and to *MEDIUM* with probability 25%, then the β value would be 0.237; if the same probabilities were assigned to both, then the β value would be 0.153. We recommend that when there is complete uncertainty in the characteristics of a Measure or its Implementation, that *Poor* or *Bad* is assigned depending on whether there is insufficient or no information on which to evaluate the characteristics.

It is also important to recognize that Table 1 essentially provides a quantitative way to define the qualitative terms of performance: SUPERIOR, GOOD, FAIR, POOR and BAD. For many cases decision makers may prefer to express their judgements to their peers in qualitative terms. Similarly, users, particularly for non-technical audiences, may feel more comfortable or effective in using these qualitative terms for the justification of an economic decision rather than quantitative values, which would require more explanation and possibly confusion. Our goal is to use these same terms to describe the reliability/uncertainty of the assessment results. Tables 2 provides guidance on how to assign quantitative β values according to the pairs of qualitative expressions for component Quality Measure and Implementation Characteristics as obtained from the Table 3 component matrix evaluations. The β values, since they are measures of uncertainty, serve to indicate that the higher their value—the lower the reliability. For the specific objective of evaluating the reliability of a building assessment, the following procedure, as developed in the next Sections, will be used:

- For each component i (i=1 to 9), under assessment, Table 3 provides descriptive matrices for corresponding qualitative terms either as a pair of component *Quality Measure* and *Implementation Characteristics* description, or a single descriptor used for of the component evaluation, β by direct application of the Table 1 values to the individual matrix locations.
- In some cases, there is the quality measure that combines the quality of implementation within its description, then the assignment is direct and the quality assignment is directly given, then use Table 2 to directly assign the β .
- The resulting N =9 quantitative β_i values are combined by the RMS Equation 2 discussed in Section 2.3 to give β as the quantitative measure of this aspect of the assessment.
- Entering this β value into Table 2. provides the corresponding qualitative description.

An important advantage of the quantitative β values for each component is that the total uncertainty β of the assessed damageability and related Performance Level

assignment may be evaluated in a mathematically consistent procedure (RMS), as discussed in Section 2.3. Rationally, it would not be possible express the *Total Uncertainty* as a combined effect of a set of different qualitative terms, except by assigning the most prevalent value which is not very compelling.

In a single-property loss assessment, an ASTM Level 1 or higher investigation is deemed an *engineered* study, while Level 0 is considered a *desktop* study and has no required technical professional input. In practice, it is common that the Portfolio study reports are vague in stating how the individual building's seismic characteristics were determined, and what the qualifications of the qualifications of the assessor were. The miss-characterization or miss-representation of primary characteristics such as construction type, year built, lateral load resisting system, condition, occupancy, etc., can result in substantial biases in estimated seismic risks. In practice, it is becoming more common that stakeholders engage seismically experienced professionals for the review of these critical inputs before the actual analyses are implemented by the damageability models. The related investigative tasks for specified properties may include:

- Review/verify that the construction type assigned to the building is appropriate:
- Review/verify that the occupancy type assigned to the building is appropriate.
- Review/verify that the year built, and year upgraded (if any) assigned is appropriate and the extent of any modification(s) or upgrades is properly considered.
- Review/verify that secondary modifiers that are building specific are provided by suitably qualified and experienced engineers and properly represented in the CAT model.
- Review/verify that the site seismic hazards have been properly considered, that is confirm that the building is not at a site that is subject to site failure (faulting, liquefaction, or landsliding) within the supporting portion of the site.

It is assumed that these technical assessments are completed by an individual(s) that have seismic civil and structural engineer knowledge but are not qualified at the level required by ASTM E2026 to do such studies at Level 1 or higher. The bulleted items level of effort does not qualify as an ASTM Level 1 of Investigation as defined in the ASTM Standards, which typically requires site visits and design drawing reviews as well as the assessor be qualified to ASTM E2026 specified experience and capabilities. To accommodate this important and growing practice in portfolio risk studies, we consider an intermediate Level of Investigation between ASTM Level 0 and Level 1, which can distinguish with more fine detail than the ASTM levels at the low end, by assessing a quality level for the assessment results to help users distinguish the results that can be relied upon from those that cannot. For this purpose, the authors add an ASTM Level 0.5 of Investigation with a corresponding definition that the bulleted items above are followed. This allows some flexibility in the limited ASTM definitions, and the capabilities of the persons assigning the seismic characteristics are given. (Lee, 2021). We propose the definition of this be referred to this level of investigation as a Simi-Engineered Assessment in which the property damageabilities are characterized based on general, not specific, information about the building types, characteristics and site conditions. The purpose of this new defined Level is to reduce the uncertainty in damageability of individual assets by limiting the potential for basic errors in essential inputs, such as misinformation on building year-built, number of stories, occupancy, existing damage to the structural system and its condition, lateral force resistance system type and quality, modifications to the structural system, or mischaracterization of construction types. Under the present requirements of ASTM Level 0, the potential for errors and mischaracterizations may be so large that its use may result in unacceptable levels of uncertainty in seismic performance characteristics. Alternatively, the cost of implementation of a Level 1 examination of the plans for the building and observation of its construction characteristics may not be feasible. The proposed Level 0.5 provides a compromise that makes serious errors much less likely.

Table 3 presents a set of proposed evaluation criteria in the form of descriptive matrices for assignment of each of the nine components impacting the assessment of the reliability of the building's damageability evaluation and/or the resulting assigned Performance Level. These matrices provide qualitative descriptions to characterize the conditions of how the component issue is described and its evaluation is implemented, and allow the corresponding quantitative β_i uncertainty value to be found from Table 1 and the corresponding Qualitative expression from Table 2. It is emphasized that these descriptions are intended to guide the assignment of the β values and that there may be additional characteristics of the process that are important in a particular application. Therefore, it is advised that the value assigned be adjusted, either by revising the Table entries or by adjusting the resulting values by the method of Equation 1, to reflect the value that best describes the professional opinion and experience of the assessor for the circumstance and conditions. As an example, for a FEMA P-154 assessment, if initially a Level 1 assessment for a particular building was used and the outcome was determined to be inadequate, then the performance of a Level 2 investigation can either change or confirm its acceptability rating. The increased Quality due to the use of Level 2 can be used to justify subsequent decisions concerning the building.

Table 3. Each of the nine components listed in this Section require assessment using Table 1 for the assessed quality of the component βi, where i is the component issue under discussion. The following matrices describe the conditions that result in the assigned Quality Measure text and Implementation Characteristic text for the components used for determining the reliability index. It is recommended that the assessor use either their own specific characterization of the seismic loading conditions important to the user, or use the seismic performance requirements of the applicable code or current edition of ASCE 41. These considerations are intended to assess both the principal and secondary influences that impact the resulting damageability and stability of the building. It is prudent to check the resulting determination as discussed in Section 4 and possibly reconsider the assignments for individual items based on these observations. References are made to ASCE 41 ground motions BSE-1E and BSE-2E, which are respectively the probabilistic ground motions with 20% and 5% probability of exceedance in 50 years. See Tables 1 and 2 for the assignment of the βi value.

 Seismic Exposure: Refers to the reliability of the characterization of the various seismic hazards affecting the building site.

Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	Probabilistic ground motion hazard distribution is determined for the building site either by a site-specific study or by use of the USGS web site for specific Latitude and Longitude coordinates of the building site and for a reliably determined site soil type from a site soil report.	High	There are no site faulting, earthquake-induced liquefaction, or landslide issues for the site. These may be determined from a soils report for the site, or as indicated for the locations of the site on governmental seismic hazard susceptibility maps.
Medium	Same as High Quality described above, except that the soil type is determine by large-scale surface geology maps or other web-based tools that are not well substantiated.	Medium	The quantification of the site failure on susceptibility maps for the site are evaluated as having low likelihood (25% or lower) of impacting the building stability if they occur, because of the building structural characteristics and condition.
Low	Ground motions characterized by Modified Mercalli Intensity (MMI) or Building Code maps of ground motion regulatory maps assigning zone ground motion values or similar quantitative characterizations.	Low	All others.

^{2.} Design Basis: Refers to the level of concern for seismic performance issues contained in the Code and Standards used for design of the building or structure.

Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	Original design regulations applicable are 1997 UBC or CBC building code or later, or the design or full seismic retrofit were completed after the ASCE 41 threshold dates for the building type for acceptability.	High	The assessed design is evaluated as showing a high concern for seismic performance issues, especially in the load path and detailing. Practices may significantly exceed the minimal requirements of the enforced code under which it was designed. This is a professional judgment by the assessors based upon their knowledge of current and historic practices.
Medium	Original design regulations applicable was regulated by 1976-97 UBC or equivalent building seismic design code, and the design was completed before the ASCE 41 threshold date.	Medium	Design meets minimum applicable building code requirements with no concern shown for non-current prescribed special detailing. This is assessed as having a low to moderate margin of over-strength of critical seismic elements necessary for assuring stability.
Low	Otherwise	Low	All others

3. Basis of evaluation: Refers to the variety and quality of the sources of building information used in the evaluation. If an evaluated building is to be modified, then the basis for the modifications needs to be specified, and also how the modifications made since construction may changes the seismic performance of the building.

Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	Building design documents were available and reviewed by the assessor; if the building is constructed, the building was visited by the assessor(s).	High	Review completed by an ASTM E2026 qualified Senior Assessor for Level 1 or higher assessments, see Section 6.2.3, who has a working knowledge of ASCE 41 and ASCE 7. Alternatively, independently peer reviewed by a knowledgeable person(s) who is qualified as a Senior Assessor, who supports the conclusions.
Medium	Either the structural design drawings were assessed or the assessor visited the building to determine the mode of construction and its lateral-load resisting system. The plans assessed must be at least 95% construction drawings or better for buildings yet to be constructed.	Medium	Review completed by an ASTM E2026 qualified Assessor or higher for ASTM Level 1 or higher assessments, see Section 6.2.3. Alternatively, if the report has been completed, and the FEMA P154 score is less than 2.0, or ASCE 41 assessment is Level 2 or higher.
Low	Otherwise	Low	All others

4. Configuration and Load Path: Refers to irregularities in the configuration and/or discontinuities in the load path of the lateral load-resisting system and how well/or not the design addresses these irregularities in order to provide acceptable seismic behavior, e.g., maintenance of structure strength and stability at maximum seismic displacement under earthquake loads specified by the client, see the suggestion in Table 3 caption.

Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	There are no ASCE 7	High	As-built drawings reviewed, and/ or structure
	irregularities in the lateral load-		visited for as-built and/or modified configuration.
	resisting system, or these are		The design meets the specified load, resistance, drift,
	specifically addressed in the		and detailing requirements described in ASCE 41 for
	building design and analysis so		damage control (BSE-2E in ASCE 41).
	as to comply with ASCE 7		
	requirements,		
Medium	There are none of the following	Medium	The design meets the specified load, resistance, drift,
	ASCE 7 irregularities: Horizontal		and detailing requirements described in ASCE 41 for
			collapse prevention (BSE-1E in ASCE 41).

	Types 1b and 4 or Vertical Types 1, 4, and 5.		
Low	Otherwise	Low	The building investigation did not consider concentrations of inelastic deformations capable of causing global or partial collapse due to damage control ground motion (BSE-1E in ASCE 41).

5. Compatibility of deformation characteristics: Refers to the stiffness compatibility among all structural elements' earthquake loads. It is intended that both the ASCE 41 S5 in BSE-2E and S-3 in BSE-1E performance be assessed, with

the most restrictive result applying	g.
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Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	The stiffness and deformational characteristics of all elements of the lateral load-resisting system are compatible in all directions, and were considered and documented in the assessment.	High	The structural design is evaluated for consistency in accommodating expected seismic drifts at collapse prevention levels of site ground motions. The evaluation may be that these were considered to be present or absent. Review completed by an ASTM E2026 qualified Senior Assessor for Level 1 or higher assessments, see Section 6.2.3, who has a working knowledge of ASCE 41 and ASCE 7. Alternatively, independently peer reviewed by a knowledgeable person(s) who is qualified as a ASTM E2026 Senior Assessor, who supports the conclusions.
Medium	The assessment considered and documented structural elements that may pose a stiffness incompatibility with the orthogonal lateral load-resisting system. These included elements posing stiffness incompatibilities occur in both horizontal directions.	Medium	The structural design is evaluated for detailing of any stiffness incompatible elements follow acceptable procedure so that their behavior does not adversely impact the expected seismic performance of the building at damage limitation levels of site ground motions. The evaluation may be that these were considered to be present or absent. The assessment was prepared by a licensed engineer, and were stamped.
Low	The assessment did not consider and document whether any structural elements with or without stiffness incompatibilities occur in both horizontal directions.	Low	All others

6. Condition: Refers to the physical condition of the building, particularly the structural elements of the vertical and horizontal elements of lateral force resisting systems, and how the observed condition may affect the expected seismic performance of the building. Refer to Table 2 for direct assignment of β. If the building has yet to be constructed, this assessment is considered not applicable.

Assignment	Quality Measure and Implementation Characteristics
Superior	The building's non-structural (e.g., cladding) and structural elements were observed and reported to be either be in acceptable condition or to have no visually observed deterioration. Inspection performed by a currently licensed engineer having confirmed seismic performance knowledge and experience and principal responsibility for the technical evaluation consistent with ASTM E2026 requirements.
Good	Some structural elements of the vertical and/or lateral force resisting systems were observed and reported to have suffered some localized deterioration or damage that may have diminished the capacity of a few elements, but does not generally impair the reliability of the seismic resistance system.

Poor	The building materials are observed and reported to be degraded or damaged at locations impacting
	the seismic resistance of the building, and/or appears to have been modified in ways that have not
	been permitted and that could impair the reliability of the lateral load-resistance system.

7. Location determination: Refers to the procedure to locate the building's site relative to precisely located seismic ground motions events that may occur, whether the site is within regions subject to liquefaction, landslide or tsunami inundations, and thereby have a basis for reliable assignment of hazard conditions. Refer to Table 2 for direct assignment of β.

Assignment	Quality Measure and Implementation Characteristics
Superior	The building's site is located by address and/or specific latitude and longitude.
Good	Not used.
Fair	The building's site is located by the town or city where it is located so that the building can be located
	within a few miles of its true location. This application does not apply to large urban area, but can
	apply if a location is indicated in a well specified and identifiable area.
Poor	Not used
Bad	Where Superior or Fair do not apply.

8. Building Damage Calculation: Refers to the technical manner in which the damage estimate was developed and evaluated in terms of the relevant building characteristics and conditions, along with the qualifications of the personnel taking technical responsibility for the seismic evaluation. Implementation requires that all information from the Matrices 1 through 6 is incorporated in the representation of seismic loading and in the building damageability characterization. The method of this incorporation shall be stated in the report to apply. If the building has yet to be constructed, this assessment should state the assumptions for construction monitor of the structural design team.

design team.			
Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	The damage probability distribution function and related parameters are characterized as a function of a site response value (say PGA or Spectral Ordinate), is developed based upon peerreviewed, published damage-prediction models that are corroborated by actual damage observed to buildings in past earthquakes. The predicted damageability measure shall be defined (e.g., mean or median) along with estimated measure of prediction error. Effects of any existing site hazards (e.g., liquefaction) have been evaluated and included in the damage assessment.	High	The report complies with the requirements of ASTM E2026 requirements for a Level 1 or higher. The report is prepared by a currently licensed engineer, having confirmed knowledge and experience in seismic performance who has the principal responsibility for the technical evaluation.
Medium	The damage values are obtained by use of an analytic engineering analysis of the building response with stated methods used for matching the engineering performance values (e.g., D/C ratios, deflections, element rotations) with a measure of corresponding damage. The model used is described sufficiently to evaluate it applicability and reliability.	Medium	The report complies with the requirements of ASTM E2026 and/or E2557 requirements for proposed Level 0.5. The report is stamped by a licensed engineer, having confirmed knowledge and experience in seismic performance who has the principal responsibility for the technical evaluation.
Low	The damage prediction model is unsubstantiated in its basis.	Low	The report does not comply with ASTM E2026 proposed Level 0.5 or higher.

^{9.} Building Replacement Construction Cost: Refers to the replacement construction cost used to determine the dollar loss. The damageability loss is evaluated for a given event by multiplying the corresponding computed damage ratio times the building replacement construction cost. Where other issues, such as contents damage, lost rents and revenues are considered, all contributions should be expressed in dollars or as a percentage of replacement cost.

Assignment	Quality Measure and Implementation Characteristics						
Superior	Replacement cost of the individual building determined by appraiser; if done historically, adjusted						
	by an appropriate construction cost escalator for the building type.						
Good	Replacement market value determined by appraiser in the past 5 years and adjusted by realty						
	inflation index to make current. If the building has yet to be constructed, this is considered to be the						
	estimated construction cost contract value.						
Fair	Square footage times a regional realty construction cost factor that reflects current cost of						
	replacement for the building use type and construction type.						
Poor	The value is determined as the market price, or other indicators.						
Bad	Not used.						

2.3 Determination of reliability/uncertainty values for individual building assessments

The determination of the reliability for a specific building's quality evaluation requires a mathematically defensible (statistically valid) method of combining the individual component uncertainties are combined to reach an aggregated value, or measure of uncertainty, for the specific assessment process. As discussed in the beginning of Section 2.2 with the use of the model format of FEMA P695, it is assumed the damage assessment process can be represented as a multiplicative function of the assigned component values [e.g. (ground motion intensity) times (building damageability characteristics) times ...] such that the logarithm of the assessed value is in the form of a sum of the logarithms of the components. For the purpose of mathematical tractability and consistent with the level of accuracy in the Qualitative-Quantitative relations in Tables 1 and 2, it will be assumed that the Probability Distribution of the random error in the assigned value for each measure is Log-Normal with a unit mean value and that the assigned β_i is the standard deviation as discussed above, as well as the coefficient of variation since the mean is one. These assumptions allow the determination of the combined uncertainty as a square root of the mean sum of the squares. While we have proposed nine critical components that affect the reliability of an ASCE 41, P-154, ASTM PML evaluation, or other applications may consider more or fewer issues. Therefore, we will consider M issues in the assessment calculations to make the method appropriate for general application.

The evaluation of the combined uncertainty in an assessed value is based the Probability Rule for the Variance of a Sum of independent random variables being equal to the sum of the individual variances (β_j^2). Given the M values of β_j for the each of the independent j^{th} issues, and using the assumption that the β_j is the standard deviation of the random error in the value of issue j element, the combined uncertainty β is the root mean sum of the squares (RMS) of the β_j values as:

RMS:
$$\beta = \sqrt{\frac{\sum_{j=1}^{M} (\beta_j)^2}{M}}$$
 or WA: $\beta = \sqrt{\frac{\sum_{j=1}^{M} v_j \beta_j^2}{\sum_{j=1}^{M} v_j}}$ (2)

In the left expression it is assumed that all of the uncertainty components have equal importance. The expression on the right assumes that the individual issues have differing weights of importance, with v_j being the assumed weighting factor for the j^{th} uncertainty source. For the particular objective of this uncertainty procedure that relates qualitative and quantitative descriptions, the division by M in the left- and right-radical is to ensure that the β value remains between 0 and 1 such that Table 2 can be used for the qualitative description of this mathematical (quantitative) result. This also achieves the desired result that if all of the β_j values are the same that the assigned β is the same as the individual value. The left-side relationship of Equation 2, called RMS here, is interpreted as introducing no bias into the computation since all components are treated equally, and the right-side, called Weighted Average (WA), as introducing a weighting corresponding to the subjective belief in the component's relative importance to the reliability of the result. Each weighting is an assumption; it is suggested that the right-side Equation be used only if there is a significant difference in the assessed importance of some elements

compared to others. This may occur where some of the damageability or loss contributions are less important when compared to others for a particular building.

Equation 2 is the primary mathematical tool used to aggregate uncertainty values (β_j or similar items) used throughout this paper, although Equation 3 as given below provides a simpler alternative, but not as well based on statistical methods. It is important to note for some evaluations that not all of the components will be important, and those deemed unimportant may be excluded from the computation. Therefore, not all assessments will have nine components of interest. It may also be true that there are other elements that bear on the reliability of the assessment that must be added. We advise that the basis for such additions and/or subtractions be documented in the report.

The purpose of this proposed *reliability of assessment* method is to provide the user with a *qualitative* description of the reliability of a given result: specifically, a quantitative β value is evaluated and then entered into Table 2 to provide the equivalent qualitative term describing the assessment. In this way we do not have to consider the nuance of meaning of a change, such as 0.01, in the β value, but instead use a qualitative term to represent the reliability. The basic presumption is that the user of an assessed value is better justified (and more comfortable) to make decisions if GOOD or SUPERIOR apply, and reject decision making if the reliability is POOR or BAD. The method also serves to identify the specific components and implementations where investment in more information may improve the rating.

Alternative Mean β : It could be argued that use of the average (rather than the RMS) of the contributors to be an appropriate way to assess the net reliability of the resulting evaluation, since it does not require assuming that the β values are surrogates for the standard deviation of the logarithms of the individual component in the analysis, and the aggregation approach does not require independence of the component assigned values. The justification would be that this form represents the average or expected error.

$$SA: \beta = \frac{\sum_{j=1}^{M} \beta_j}{M} \quad \text{or} \quad \beta = \frac{\sum_{j=1}^{M} v_j \beta_j}{\sum_{j=1}^{M} v_j}$$
 (3)

This will be called the *Simple Average* (SA) combination approach, either by a simple average of equally weighted values (left), or weighted values (right). Equation 3 is the primary alternative means to aggregate β_j used throughout this paper, but is generally not preferred to Equation 2.

Table 4 provides the β values for the RMS and the Simple Average alternatives for different assumptions of the β values. The Table shows the impact of completing a portion of the issues with a common β value by a better or poorer assessment procedure than the balance, where the β values are a given level for all but one or two values which are different, termed 1x and 2x in the Table. While the resulting values are comparable for some combinations, the Simple Average yields systematically higher reliability factors (that is lower β) for all 1x and 2x values. The range of the ratio of the RMS β values to their simple average range from 1.000 to 1.673 for the 1x comparisons, with the 2x values being in a tighter range of 1.000 to 1.458. We find the RMS approach is consistently the most conservative, and can be better justified on a mathematically basis, if the multiplicative model of components is accepted. The RMS aggregation procedure will be used for the further developments dealing with single building and portfolio assessments.

As seen in Table 4, changes in having either one or two higher or lower than the principal β values can alter the model's reliability index significantly. The clear implication of this table is that accepting less than FAIR component reliability as the basis for the component assessment, makes it very unlikely that the assessment will get a FAIR rating or better. In contrast, when SUPERIOR or GOOD is the base assessment, one can allow one or two components at a lesser rating and still get a GOOD or FAIR rating. This behavior may be considered in the formulation of a strategy when it is intended to increase the building assessment's reliability with the most efficient use of available resources. In addition, the behavior exhibited in the Table provides a direct way to see what would be needed to improve the reliability of the assessment conclusion where there is a concern that the reliability is too low upon which to base a decision. Often the most important link in the assessment procedure concerns whether or not the assessor has access to the

Table 4: Impact on the Building β of having all but indicated β values fixed at the same value, with one (1x) or two (2x) β values set at the variable β value. Two aggregation approaches are used: RMS of the β Equation 2, and simple average. Green highlighting indicates that the β qualified for a SUPERIOR ratings per Table 2, blue indicates GOOD, uncolored indicates FAIR, and orange indicates POOR or BAD. Only base values of FAIR or better are given; others can be easily calculated

und change i	variable β									
Fixed β	1x0.1	1x0.2	1x0.35	1x0.5	1x1.0	2x0.1	2x0.2	2x0.35	2x0.5	2x1.0
RMS: 5 issues										
0.10	0.100	0.126	0.180	0.241	0.456	0.100	0.148	0.235	0.326	0.637
0.20	0.184	0.200	0.238	0.286	0.482	0.167	0.200	0.270	0.352	0.651
0.35	0.316	0.326	0.350	0.385	0.546	0.278	0.299	0.350	0.417	0.688
RMS 6 isst	RMS 6 issues									
0.10	0.100	0.122	0.170	0.224	0.418	0.100	0.141	0.218	0.300	0.583
0.20	0.187	0.200	0.232	0.274	0.447	0.173	0.200	0.260	0.332	0.600
0.35	0.322	0.330	0.350	0.379	0.518	0.292	0.308	0.350	0.406	0.644
RMS 7 isst										
0.10	0.100	0.120	0.161	0.210	0.389	0.100	0.136	0.205	0.280	0.541
0.20	0.189	0.200	0.228	0.265	0.421	0.177	0.200	0.252	0.316	0.561
0.35	0.326	0.333	0.350	0.375	0.498	0.301	0.315	0.350	0.399	0.611
RMS 8 issi										
0.10	0.100	0.117	0.155	0.200	0.366	0.100	0.132	0.195	0.265	0.507
0.20	0.190	0.200	0.224	0.257	0.400	0.180	0.200	0.246	0.304	0.529
0.35	0.329	0.335	0.350	0.372	0.482	0.307	0.319	0.350	0.393	0.585
RMS 9 isst	ues									
0.10	0.100	0.115	0.150	0.191	0.346	0.100	0.129	0.187	0.252	0.480
0.20	0.191	0.200	0.222	0.252	0.383	0.183	0.200	0.242	0.294	0.503
0.35	0.332	0.337	0.350	0.370	0.469	0.312	0.323	0.350	0.388	0.563
Simple Av	erage: 5 is									
0.10	0.100	0.120	0.150	0.180	0.280	0.100	0.140	0.200	0.260	0.460
0.20	0.180	0.200	0.230	0.260	0.360	0.160	0.200	0.260	0.320	0.520
0.35	0.300	0.320	0.350	0.380	0.480	0.250	0.290	0.350	0.410	0.610
Simple Av		ssues								
0.10	0.100	0.117	0.142	0.167	0.250	0.100	0.133	0.183	0.233	0.400
0.20	0.183	0.200	0.225	0.250	0.333	0.167	0.200	0.250	0.300	0.467
0.35	0.308	0.325	0.350	0.375	0.458	0.267	0.300	0.350	0.400	0.567
Simple Av										
0.10	0.100	0.114	0.136	0.157	0.229	0.100	0.129	0.171	0.214	0.357
0.20	0.186	0.200	0.221	0.243	0.314	0.171	0.200	0.243	0.286	0.429
0.35	0.314	0.329	0.350	0.371	0.443	0.279	0.307	0.350	0.393	0.536
Simple Av										
0.10	0.100	0.113	0.131	0.150	0.213	0.100	0.125	0.163	0.200	0.325
0.20	0.188	0.200	0.219	0.238	0.300	0.175	0.200	0.238	0.275	0.400
0.35	0.319	0.331	0.350	0.369	0.431	0.288	0.313	0.350	0.388	0.513

structural design drawings, has visited the building to examine its condition, and/or has the qualifications to do the assessment. For example, if the assessment does not have any of these afore mentioned attributes, then the rating of Component 3, *Basis for Evaluation* is likely to be *POOR* or *BAD*. The raising the Component 3's rating can dramatically change the β value from 0.5 or lower to 0.2 or lower. If the base value of assessment is *GOOD*, then the reliability could go from *FAIR* to *GOOD* or better by this single action. If, in addition, a second attribute is improved, then Table 4 makes it clear that the impact can be significant. It is important to note that if there is concern about reliability of the assessment and the results will be an essential factor in making fiduciary decisions, it is appropriate to set the criteria for the performer/provider of the assessment to meet the client's goals before the assessment is commissioned. The purpose is to minimize the possibility of results that *are not sufficiently reliable to use for related decision purposes.*

2.4 Aggregation of Building Damageability Uncertainties for a Portfolio

In the evaluation of Portfolio uncertainties in Section 5, it is necessary that a representation be determined for the overall damageability uncertainty for the group of buildings considered. This is represented by a weighted aggregation of the uncertainty values for each of the individual buildings as determined from Section 2.3. Since it is most common that portfolios consist of buildings having different levels of investigation, it is important that the corresponding β differences be reflected in the reliability estimate for the portfolio loss assessment. We will use the building replacement value to provide the weighting for each building. This aggregate for the building evaluation for the portfolio is similar to the weighted version of Equate 1:

$$A = \sqrt{\frac{\sum_{i=1}^{N} c_i \beta_i^2}{\sum_{i=1}^{N} c_i}} \tag{4}$$

Where A is the aggregated damageability uncertainty for the Portfolio, β_i is the damageability uncertainty for the i^{th} building in the portfolio of N buildings, and c_i is the replacement cost of the building. The same caution applies to these equations as was discussed in Section 2.3. The same caution applies to use of these equations as was discussed in Section 2.3. There is no reason to suppose that a simple average be used here because the value of the β_i is easily defended since these are independent structures and thereby the β_i are independent.

Not surprisingly, when all of the buildings have the same implemented damageability assessment procedure, that is, the A value for the group is identical to the common β value for each. For an existing portfolio analysis, the β_i values are fixed, and the uncertainty index A is fixed. However, for a portfolio that has yet to be assessed, or for one that is in part to be reassessed, there is an opportunity to make choices that specify the level of investigation for those individual buildings that can significantly impact the A value. This pre-assessment specification applies as well to the indexes B and C to be developed respectively, in Sections 3 and 4. It should be noted that the Proposed Investigation Level 0.5, as discussed in Section 2.2, may be particularly useful for those specific buildings that pose a significant element of the loss risk and when a Level 1 assessment is not feasible because of time limits or lack of resources.

2.5 Example application for decisions concerning a single building's acceptability

A pivotal issue in real estate management of a building may be whether a seismic assessment's findings are of adequate quality to make a decision of the future use, modification, or purchase of the building. We presume that an evaluation prepared has determined whether or not the building is acceptable is based on the client's purpose for having the assessment completed. Here, the focus is on the quality of the building evaluation and the issue is to decide whether the building is acceptable for occupancy or not based on its seismic evaluation and conformance to an established standard. In the State of California, the usual measure of the assessed seismic performance for a building, new or existing, is the degree to which the building meets the seismic performance requirements of the California Building Code. In California the standard for a state-owned building, including the University of California and California State University Systems, is the degree to which the building meets the seismic performance requirements of the California Existing Building Code. For new buildings this code requirement is an adaptation of ASCE 7, and for existing buildings it is Section 317 and the following Sections of the 2019 Edition of the California Existing Building Code (CEBC). The issue for decision making is that conformance with Building Code objectives is a binary process: the building either meets or does not meet the criteria. A satisfactory way to express the seriousness of a particular level of non-code acceptability decision is to use a rating scale to express the degree of risk. A satisfactory way of describing the seriousness of a particular assigned level of non-code acceptability is to use a rating scale to express the degree of risk. For this purpose, the California State University System, and the University of California have assigned a category method for Earthquake Performance Rating Levels based on CEBC evaluations, see Table 5.

Table 65R (1804) Rating soft Extibhquake. Parfor thorn 2019 CEBJO: Existing Buildings from the current edition of the CSU Seismic selficing those double on the CBC. (CSU Seismic Policy, March, 2020). The University reoft will form in buildings these definitions, as do most California State Agencies. For levels III through V, the assessing engineer 31718 in Exast in glotton at the illustrig supported by the independent peer reviewer. These follow the requirements of the CEBC, or where the case in the last of Culifornia State Agencies in ASCE 41 by not allowing the capping of values Unitersity of Culifornia did not the EEC University,

appearing of Europe han and the Europe and Europe and Europe					
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fixed the section of the CBC requirements of the CBC requirements	1				
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Applainting of the arciding or exceeding the requirements of CEBC for Risk Category IV					
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thilding that you curred after adoption of the 1995					
Adiparting vilating teacher and either the current of CEBC for Risk Category I-III					
periofitmance criteria with BSE-1 and BSE-2 hazard levels without MCER capping replacing BSE-R	III				
2. That BSE divespectively also given in CSBC. Alternatively, a building meeting the CBC requirements	111				
3. The undividuating he structural components increases the					
A SUNG for gevir a threating were seeming the requirements of CEBC for Risk Category I-III	IV				
structural companies of the existing structure by more	l V				
And in the requirements of CEBC for Risk Category I-III					
performation when the control of the specified for the	V				
states the increased forces determined in accordance with					
A building elitheacting the fill of the control of	VI				
has been increased sincethe original construction, the	VI				
Recuil of highest all hated she positive and lighthest differ sheety hazard to its occupants under gravity					
the difference building should be evacuated and posted as dangerous until remedial actions are taken	VII				
4. Strusture the Butterned can strubber the depress fibed dead and live loads.					

reduced the lateral-load-resisting capacity of the structural system by more than 10 percent.

5. Changes in live or dead load increase story shear by more than 10 percent.

Generally, a Level IV rated building can be used without limitations, and a newly leased or purchased building must meet the same requirement, (CSU, 2020). In the long term, the CSU and UC policies are to have all of

their buildings meet or exceed this Level of seismic performance requirements. However, the objective of achieving a Level IV rating for deficient buildings can be very demanding. In order to provide incentives, the CSU has chosen to accelerate the seismic retrofit work by enforcing the following CEBC requirements:

For existing buildings, any time that a building has proposed work requiring a
building permit under the CEBC, that if the work is of the type and/or extent that
exceeds stated triggers that require a seismic evaluation, see Table 6, then the
building must be seismically evaluated and if indicated, actions must be taken,
within the proposed work, to make the building consistent with CEBC
requirements.

It should be noted that the stated triggers for a required CEBC assessment do not necessarily require assessment whenever a modification of the building is proposed that requires a permit. The work must be in excess of the stated trigger limits. In addition, since 1992, in order to achieve *due diligence* for the life safety performance of all of its facilities, the CSU has performed regular assessments, at all campuses, to determine those buildings in its inventory which pose a significant seismic risk. When such an assessment determines that the vulnerability is too high to accept, then CSU decides on whether the building warrants retrofit as soon as resources become available (listed as Priority I), or be retrofitted whenever any permitted work (no trigger limits) is proposed (listed as Priority 2). These decisions depend on the Ratings of seismic performance indicated in Table 5. In addition, the CSU has determined that a building identified as posing an

unacceptably high life safety risk will either require administrative action to seismically retrofit the building in a short-specified term, or cease use of the building.

The above description of the CSU Performance Requirements in terms of

Requirements in terms of Rating values, provides an example of where the proposed Uncertainty and Quality evaluation methodology can be applied. The resulting uncertainty evaluations can be used as guides for risk management decisions governing retrofit existing of buildings, along with the decisions concerning lease or purchase of additional buildings. When a building has been assessed to determine its seismic performance by use of FEMA P-154 or

Table 7. Proposed decision matrix for how to act upon the assessed confidence in the reliability of assigned seismic performance level of the building. These requirements are for the CBC occupancy Seismic Category I, II and III. See text for the descriptions of the Lists. The option always exists to delay determination of how to proceed by commissioning a more complete seismic assessment.

Seismic	Actions for implementation based			
assessment	upon the reliability Quality of			
reliability	performance estimate (Acceptable or			
Quality	Not-Acceptable).			
SUPERIOR	Very High reliability: no action if			
JUPERIOR	Acceptable.			
Good	High reliability: no action if Acceptable			
	If rated as Acceptable, no action			
	required. If rated as Not Acceptable			
	and owned, then plan for seismic			
	retrofit when other improvements, or			
FAIR	remodeling are proposed. If for			
FAIK	purchase plan to retrofit immediately.			
	(Equivalent to assigning building to			
	List 2 as discussed.) If for financing,			
	then carefully assessed to assure the			
	return is commensurate with the risk.			
	Regardless of assessment, either do not			
Doop/PAD	proceed, or complete a higher level of			
Poor/Bad	evaluation. (Equivalent to assigning			
	building to Priority 1 as discussed.)			
•	<u> </u>			

ASCE 41, or other means, an assessment of the uncertainty *A* corresponding Quality of the conclusions of should be made by the proposed method. Table 7 provides an example of how these uncertainty measures could be used to guide decisions. For the case of a *POOR* or *BAD* Quality evaluation, it is recommended that **no** decision be made based upon the evaluation, unless the risk is managed by requiring earthquake insurance, with an appropriate deductible. With the prevalent insurance rates, it may be more cost-effective to refuse the investment opportunity rather than incur the cost of a more reliable damageability assessment.

3 Uncertainty for Portfolio Assessment Procedures

3.1 How do the problems of assessing portfolios of buildings differ from a single building?

Most portfolio seismic analyses focus on the determination of dollar loss, or in some cases the ratio of loss to replacement cost, caused by earthquake occurrences to a portfolio of buildings located at sites that are not subject to the same degree of seismic hazard from any one of the earthquakes that could impact some of the portfolio's members. This loss and its probability of being exceeded play an important role in many financial decisions. For a Portfolio Loss assessment due to the risk of all possible damaging events in the hazard zone, the evaluation of the loss for each of the individual buildings is essential; however, these are not sufficient since for the aggregation of the loss there are other factors that impact the reliability of the estimate. These include: correlation of damage for a given event, consideration of all of the multiple possible seismic events and the statistical response of each building to these events, and the dispersion of building damageabilities and values. Of these factors, only the loss reliability value for the individual buildings was included in the Section 2 issues. Also, concerning representation of individual building

uncertainties, it is usual that the resources and effort available per building is considerably less than those for a single property assessment, except perhaps for a few very high value properties at a high seismic-risk location. Also, it is important to recognize that the ASTM E2557 procedures used for the Scenario Loss Assessments (SEL, SUL) for single buildings or multiple buildings at a single site cannot be aggregated for an equivalent Portfolio Loss at multiple sites because of the different earthquake ground motion at the sites due to the same earthquake event, and there are multiple possible events for the seismic zone. The scenario measures SEL and SUL for a Portfolio due to a specified event can be misleading (unless possibly for the special case where the high value properties are concentrated near to the source of the selected scenario event) because of the multiple sources and dispersed locations of high value properties.

Typically, Portfolio Loss Assessment reports will indicate the aggregated losses likely to buildings where the individual losses include repair cost and possibly building contents loss and lost rents and revenues. Reported loss assessment values are usually given with the probability of losses being exceeded over a specified time period, commonly one year. Probable Loss (PL) is defined by ASTM E2026-16a as:

Probable Loss (PL): earthquake loss to the building systems that has a specified probability of being exceeded in a given time period, or an earthquake loss that has a specified return period for exceedance.

A *PL* value is meant to reflect, in a statistically consistent manner, all of the uncertainties that can impact damage estimates, including when and where earthquakes occur and with what magnitude, attenuations of ground motions at the site, local site effects and performance of the building systems in this ground motion. The PL values are expressed in terms of the damage ratio, and are generally limited to earthquake loss associated with the earthquake ground-shaking hazard, but may include losses from other earthquake hazards as prescribed by a User. *PL* values are given either as a value with specified return periods, or as values that have specified probabilities of exceedance in a given time period. This definition serves the same purpose for geographically distributed portfolios.

For the case where the Portfolio building sites are geographically distributed, any given event can cause intensities of ground motion and corresponding levels of damage that are different for each building site. The Portfolio Probable Loss must consider the effects of all possible damaging events in the hazard region together with the likelihood of the event occurring. The event representation problem typically is addressed by the formation of *Event Sets* that represent all of the possible earthquakes that can impact one or more of the buildings in the portfolio. The *Event Set* includes all damaging magnitudes, location on features (seismic source: faults, areas), and corresponding recurrence rates for each of the features in the seismic zone.

The general concept of ASTM's Probable Loss (PL) as adapted and applied to portfolios offers the only means of expressing total risk to a portfolio due to all possible damaging events from all seismic sources that can impact any one of the portfolio buildings. Additionally, the PL process provides for the representation of the uncertainty of each building's damageability response to the site ground motions.

A major difference between portfolio versus single building assessment is that the portfolio structures are distributed over large areas, possibly national in scope, and it is not possible to characterize the same ground motion for all building sites. This problem is addressed in portfolio analysis by selecting *Event Sets* that represent all of the possible earthquakes in aggregate that can impact one or more of the buildings in the portfolio. The Portfolio Probable Loss statistics are derived for all possible statistics of the building losses in each of the event set earthquake ground motions, and reflect the weighted probability of the event, the site ground motion in this event, and the statistics of the loss due to this ground motion to the building, aggregated over all members of the event set. A purely analytical derivation is not practical because of the complexity of the integrals of loss functions in each event times probability density functions for all buildings and locations, sometime thousands. Also complicating this analysis is that the site ground

motions due to each event are often complicated probabilistic computations with many trees of conditional random variable distribution functions. The formal mathematics can be described, but their complexity does not allow closed form solutions.

As a result, Monte Carlo simulations are usually the only practical computational approach to the determination of the probability distribution of Portfolio Loss for a one-year time period. These simulations are performed within what is termed as the Catastrophe (CAT) Model. A very large sample size of simulations is made to provide sufficient precision (by the Law of Large Numbers) for determination of the Probability Distribution Function and corresponding Loss Statistics. Following are necessary components and procedures for a valid CAT Model used for Portfolio Risk Assessment.

CAT modeling is the term used for a computer-based analysis procedure to determine the financial threat of a group of properties (the portfolio) due to all of the seismic events that can occur during a stated time period and impact on one or more of the properties. The determination of the loss values for the portfolio involves both types of uncertainties (epistemic and aleatory). In the modeling process, it is difficult to determine whether a particular uncertainty should be put in the aleatory or the epistemic category. It is up to the model's builder to make this distinction. The choice depends in part on scientific knowledge, but much more so, on the practical need for limiting the sophistication of the model in order to make the model feasible for use. In most cases, the calculations in these models are performed by the Monte Carlo method that may require millions of simulations to achieve numerically stability of the results; as a consequence, economy of computation is imperative, (Zio, 2013). The parameters that are included in a particular CAT model can be characterized as aleatory because they are treated as random variables based on a limited amount of data and/or expert judgement. The computational results can characterize those uncertainties included in the simulations (sample estimation error) for the given model, but these do not address the epistemic uncertainties introduced by the assumed probability distribution types and related parameters and methods as employed in the model. Therefore, the simulation results cannot fully reflect the epistemic uncertainty of the result. This is because, ordinarily, the providers do not address the basis on which the analytic portions of the model were selected and the degree of accuracy (and possible bias) introduced in the results. As an example, when a specific event ground motion intensity is to be evaluated at a building site, what "source to site" attenuation model is used to determine the numerical value of this site intensity? There is often more than one acceptable model that can each produce different results for the same assumptions of the event. It could be argued that the use of a fault tree (with weighted likelihood for say three models) resolves this "single choice" difficulty; however, in fact, the use of multiple weighted ground motion model (attenuation relationship) results does not fully resolve the uncertainty problem because the weights (measures of credibility) for each branch need to be judgmentally assumed. Further, the representation of these weights as random variables with probability distributions does not provide resolution, since it is necessary to choose a representative distribution function. Further, the choice of the attenuation model does not address the issue of the assigned attenuation distance from the event source to the site, which itself is subject to high aleatory uncertainty in the available historical event data sets used to determine the attenuation model. In addition, there is a lack of more fundamental (epistemic) knowledge such as the compressive and shear strength of the rock rupturing, location and size of rupture, the direction and speed of the induced rupture, the geology of the travel path, etc. Nonetheless, the distinction of the two types of uncertainty is useful in establishing an analytical framework that treats the complex uncertainty in CAT modeling process in a formal and systemic manner, and also important for model builders and decision makers to test and understand the sensitivity of CAT modeling outcomes to various model choices and modeling assumptions (Lee 2021., 2018; Lee, 2018).

It is helpful to mention here that a typical Portfolio Loss Assessment process (CAT) involves a very large sample set of the simulated Portfolio Loss Values. The mathematical justification for the use of this data set to infer probability statements concerning Portfolio

Loss is provided by the notion of the *Indifference Principal*, in which each calculated outcome can be considered to be equally likely to occur, (Halpern, 2017). The principal of indifference is that all elementary outcomes of the simulations are equally likely, the core assumption that underlays probability theory. Thereby, the probability distribution for the loss in designated period can be directly determined by order statistics evaluation of the simulations. No *a priori* probability distribution function needs to be assumed, but the empirical distribution function from the simulations serves this purpose.

The process of Portfolio Loss Assessment proceeds as follows: given the structural description, replacement cost, and site location of the buildings within the defined seismic hazard zone having location and activity description of the seismic sources, determine and evaluate the following components or steps.

- Ground shaking source including segments activated, magnitudes, event-to-site
 distances to each building in the portfolio (termed the Event Set). Attenuation
 relations to each building site, site soil types and surface intensity effects. Each
 element of the Event Set requires a temporal evaluation of its likelihood of
 occurrence.
- Site-specific hazards (e.g., liquefaction, landslides, fault rupture).
- Structural damage prediction relation (usually in terms of damage ratio) in terms
 of site ground motion intensity and building damageability characteristics.
 Include damage due to any site-specific hazards.
- Losses (building repair and restoration, contents, business interruption, demand surge, i.e., increase of costs immediately after the event when demand for services and materials exceed supply). Loss is a function of damage ratio, plus any additions due to site-specific hazards. Cost of building replacement should be based current construction cost estimate.
- Aggregation of individual property losses and probabilities into portfolio probable loss statistics, accounting for uncertainty in individual building losses, aggregation of uncertainties for portfolio loss.
- Estimates for Portfolio Loss statistics.

At its core, the problem of determining portfolio loss assessment reliability involves: the representation of the reliability in hazard assessment (source seismicity, site ground motion and other hazards), the representation of the reliability of the damageability characteristics of each building in the portfolio, including the consequences of any existing site hazards (liquefaction-, landsliding-, or settlement-induced), and other secondary consequences (fire, or demand surge losses). For the reliability/uncertainty related to the damageability characteristics of EACH individual building, the approach will be as developed in Section 2 for each building, and then these uncertainties will be aggregated (weighted by respective replacement values, see Equation 6) for the uncertainty of portfolio damageability. The results will be included as a part of the complete portfolio uncertainty and corresponding qualitative reliability of Section 4.

3.2 Assessing uncertainty/reliability for portfolio loss assessments

This section addresses how to determine the reliability of a portfolio assessment. Herein, for clarity we use γ in place of β to represent the uncertainty parameter for the components and results of the Portfolio Loss Assessment. We assume that the CAT model provider will report the statistical characteristics of the assessment approach such that these can be verified to be valid within the laws of probability and statistics. Typically, a computation of portfolio probable loss statistics (such as loss value having a given probability of exceedance in a given time period) is performed using sequential Monte Carlo simulations of: event seismicity, site ground motion intensity, building damageability, associated building costs and losses, and aggregated portfolio losses. Each of these steps require an assignment of a probability density function and related parameters from which the Monte Carlo simulations are selected. The simulated aggregate loss results provide a large size sample that allows the determination of the empirical probability density function of the annual portfolio loss. The entire procedure is termed as the CAT Model. The number of assigned parameters is usually kept to a

minimum so that the computations are achievable. As a consequence, there are many assumptions and parameter value assignments in the simulation process whose uncertainties are not considered (therefore not reported) as part of the uncertainty of the final calculated loss statistics. These unconsidered or unmentioned (epistemic) sources of uncertainty in the CAT Model must be identified and included in the total measure of the uncertainty of the results. For example, the complex Earth's crustal deformation models, seismicity models, earthquake rupture models, and ground motion prediction models may be greatly simplified by a CAT Model developer for the purpose of practical implementation. The building site ground motion intensity measure due to a given event could be represented as Peak Ground Acceleration, or better as Response Spectrum Values (GOOD), or worse, such as the Modified Mercalli Intensity ratings for the region of the site (POOR). Similarly, the effects of the site soil column characteristics on the surface ground motion intensity may be derived from a site-specific soil assessment (GOOD) or from large scale geologic hazard maps (POOR). Another example concerns the level of information used to represent the individual building's damageability parameters. This information can be from: a building visit by an experienced evaluator (GOOD), the assessment of the construction drawings by an experienced Engineer (GOOD), or simply a review of Desktop photos and real estate documents (POOR). Also have the observed building deficiencies (including primary and secondary influences) been entered into the CAT Model: (GOOD) if entered, or (POOR) if not entered. The building damageability parameter evaluations for a given building within the portfolio can be performed at any level of reliability as discussed above. These levels may vary for different buildings within the portfolio and the corresponding individual uncertainties must be included in the aggregated uncertainty weighted by the building replacement value of the portfolio loss statistics. In summary, there are various alternatives in the data collection, parameter specification, data input, and analysis methods used in a given CAT Model: the specific choices of these alternatives and representation of their related quality, method of implementation, and measure of uncertainty can have a significant effect on the reliability of the corresponding CAT loss statistics. The purpose here is to provide a method by which a user can evaluate the reliability of the CAT results by assigning and combining the uncertainties corresponding to the options and alternatives used in a given CAT Model.

3.3 Evaluation of characteristics and components in portfolio loss assessment

There are three principal sources of uncertainty for portfolio loss assessments: first, the way in which the damageability of the individual buildings making up the portfolio is determined (uncertainty of damage assessed in Section 2); second, how the CAT model determines the loss for the individual buildings and then aggregates this loss for total portfolio loss; and third, what the combinatory statistics of the simulations process is numerically. The computational statistics of the damageability analysis will be addressed in Section 4. In this section, we address the uncertainty of loss aggregation in Portfolio Loss Assessment process. For most portfolios, the site seismic hazard along with the individual building damageability characteristics and related reliability level of knowledge are different for each property in each possible damaging event. Computationally, Portfolio Assessment uses the concept of *Event Sets* to characterize the overall seismic hazard (see Section 3.1). Also, building damage values due to a given Event are correlated, and this must be recognized in the summation or aggregation of building losses due to all possible events. Therefore, the representation of the Event Set is a key element in any portfolio assessment to ensure that the aggregated damage loss for the set of buildings is properly determined. The key components and sources of uncertainty in the evaluation of portfolio damage loss statistics that are related to the determination of loss of individual buildings and portfolio loss aggregation are:

1. EVENT SET (ES)—Event Sets represent the earthquake events by location, magnitude range, recurrence rates and other characteristic of the event such as nucleation, rupture initiation, that are used to characterize the events included in the related event intensity computations along with their site attenuation distances. Concerning magnitude range, generally, a magnitude 5.0 earthquake

is capable of damaging an existing Unreinforced Masonry Bearing Wall building in the near field, and a magnitude 5.75 is capable, in the near field, of damaging a newly constructed building designed to current building standards. It is often useful (for computational efficiency) to characterize the seismic hazard by identifying those particular sets of events that cannot impact portions of the portfolios, and thereby allow the uncoupling of the risks for these different areas. This uncoupling of certain portions influences how the CAT model is developed and has implications for computational efficiency of the CAT model, but does not have any significant effect on the reliability of the loss results. It is also essential that recurrence rate information is available for each seismic source. Where a main fault can produce events on different segments or combinations of these segments, each with magnitude range and rates of occurrence, then the resulting events and corresponding return period shall be included in the event set. The reoccurrence rate for each event in the event set is necessary, such that each simulated event losses and resulted aggregated portfolio loss can be associated with this reoccurrence rate. From each source, there must be a sufficiently large number of simulated events that the sample magnitude-frequency distribution (MFD) Empirical Distribution Function that can yield useful loss return periods over a wide range of values, allowing determination of the loss estimate associated with the longest mean return period of interest (practically represented by Order Statistics of the simulated values tail). This is termed the Empirical MFD rather than the implied definitive MFD because it is based on a finite number of simulations and may not adequately represent the true MFD.

- 2. Loss Aggregation (LA)—Description of how the loss Probability Distribution Function (PDF) or the Cumulative Probability Distribution Function (CPDF) reported is determined for the portfolio. This is the process by which each individual building loss due to a given event is aggregated for the whole portfolio of buildings, and the result is then aggregated for all events in the event set. This needs to be performed in a statistically valid manner to provide the Portfolio Loss Statistics having a given return period. While there is the option of assuming the CPDF (such as Log-Normal or Beta distribution) and evaluating the related parameters in terms of the sample estimates based on the simulated loss data, this mathematical representation is subject to epistemic error. For the case where Monte Carlo Simulation can produce the required very large sample size, it is preferable to use the non-parametric ranked order statistics as described above. A typical process for the successive simulation is as follows:
 - A) From the *Event Set* randomly select an Event with known characteristics and determine (by selected ground motion models site soil effects) the PDF of ground motion intensity at each impacted building site in the portfolio to this event.
 - B) For each building, determine the Damage Ratio PDF (refer to *Matrix 7 in Table 3*) due to the item A ground motion randomly selected Item A.
 - C) For each building, determine loss PDF of simulated damage ratio for the site for each portfolio building.
 - D) Aggregate all building losses for portfolio loss due to selected event from the PDF for the event (Item A), PDF of the site response (Item B), and loss PDF (Item C). This yields one simulation loss for the Portfolio in the event assessed. This loss will have a Return Period associated with the selected Event.
 - E) Repeat the above sequence with a sufficiently large number of simulations necessary to define (with acceptable sampling error) the PDF of the random Portfolio Loss due to all possible independent events and corresponding independent responses buildings. For a given return period the Portfolio Loss Statistics are determined from this PDF.

3. DEMAND SURGE CONSIDERATION (DS)—Repair costs are based on the building replacement cost times predicted damage ratio. The reliability of the replacement cost is addressed for each building in Item 8 of Table 3 for individual buildings. Demand Surge reflects the influence of repair cost inflation due to post-earthquake demand for construction materials and labor costs of repair while the market is distorted. There is a surge in pricing for building services and materials as demand for limited supply is significantly increased in the post-event emergency period. See Olsen and Porter, (2011), for a recent review of how demand surge is estimated. When cost escalation is not important, then issue 3 can be ignored.

Discussion: Demand surge is an issue for individuals and institutions that sustain losses in large-scale natural disasters, particularly for property insurers and governments that finance reconstruction. Estimates of demand surge following large-scale natural disasters have quantified a general increase of costs ranging from 10 to 40% following Hurricane Katrina to 50% after Cyclone Larry. For specific materials and labor items, news reports have documented price increases of 30% for oriented strand board following Hurricane Katrina to a 2,000% increase for securing a tarpaulin to a damaged roof after the 1999 Sydney hailstorm. The higher repair costs at each property result in a greater loss for an insurer that indemnifies many properties in an affected area. For a single insurer, this additional loss caused by demand surge may mean the difference between survival and ruin. For example, 20th Century Insurance, based in the Los Angeles area, was nearly bankrupted by claims following the 1994 Northridge Earthquake, a disaster that produced a reported 20% demand surge. (Olsen and Porter, 2011). Often this item is estimated by multiplying the calculated cost by a factor representing the expected increase of costs where demand far exceeds the supply of both skilled manpower and materials.

For the above components, the corresponding uncertainty measures γ_j are to be determined similarly to the procedure for single building procedure by the descriptive quality Matrices in Table 8 and the use of Table 1 or Table 2 for the quantitative and qualitative expressions. All of these uncertainties in portfolio loss evaluation steps as well as the related uncertainties in the individual building loss estimates for the building damageability evaluations are ones that need the attention of the user to make sure that the reliability of the CAT Model Portfolio Loss Statistics is consistent with the requirements for the user's decision-making process. At a minimum, Items 1 and 2 should be considered.

Table 8 gives matrices for assignment of the qualities of Assessment and Implementation of each of the three components impacting the uncertainty and corresponding qualitative reliability of the Portfolio CAT Model loss statistics. This *matrix* procedure follows the approach used for individual building uncertainty evaluations of Section 2.3. These matrices are intended to provide qualitative representations of how the element issue was addressed to yield the corresponding quantitative uncertainty r_i . The manner of combining these r_i values for the total Portfolio Uncertainty and Quality will be discussed in the next sub-sections where the resulting p_i values will be combined (RMS) to represent the total measure of uncertainty r_i of the resulting CAT Model loss statistics.

Table 8. Definitions of Quality Measure and Implementation characteristics for the components of the portfolio evaluation. For purposes of clarity, we characterize the portfolio component uncertainty by γ rather than the β used for single building assessments.

1. Event Set: Definitions of quality measure and implementation characteristics for Event Sets within a Risk Zone.

Assignment	Quality Measure Characteristics	Assignment	Implementation Characteristics
High	The seismic hazard base that is	High	All earthquakes with magnitude greater than or
	relevant to the portfolio		equal to 5.5 in moderate-to-high seismicity
	comprehensively considers		regions or 5.0 in low seismicity regions are
	alternative scientifically credible		included if they pose a significant damage threat
	sub-models in representing the		to at least one building in the portfolio. Events
	regional seismicity and ground		extensively represent the randomness of future
	motions. Maximum magnitudes		earthquakes in occurrence, magnitude, rupture

	are established by geological or other scientific methods. Both known faults and unknown sources (background seismicity) are considered. Rates of earthquakes with magnitude 5.0 or greater conform to regional magnitude-frequency relationship. All models/sub-models have been peer-reviewed.		location, and rupture length. Ground motion intensity consider both record-to-record variability and spatial correlation. Multiple vibration response periods are represented. Probabilistic ground motion hazards computed from the event set at the portfolio sites are demonstrated to conform to the base hazard model, with difference that is generally less than 15% for the level of ground motion that is deemed to pose a significant damage threat to portfolio buildings (e.g., at 475-year return period).
Medium	The seismic hazard base that is relevant to the portfolio considers all earthquake sources recognized as significant with sufficient justifications.	Medium	Same as above but the probabilistic ground motion hazards computed from the event set at the portfolio sites are demonstrated to conform to the base hazard model, with difference that is generally less than 27.5% for the level of ground motion that is deemed to pose a significant damage threat to portfolio buildings. Or single magnitudes are assigned to earthquake sources with magnitude 5.75 or greater in moderate-to-high seismicity regions or 5.5 or greater in low seismicity regions that can impact at least one portfolio building. Events comprehensively represent the randomness of future earthquakes in occurrence, magnitude, rupture location, and rupture length. Ground motion intensity considers attenuation variability.
Low	All others	Low	All others.

2. Loss Aggregation: Aggregation is a description of how the total loss values from the considered sources (e.g., building damage, contents damage, lost rents and revenues, ...) are determined from the individual building's loss response to ground motions for an event set. It is important for the user to understand how the estimates of damage and other losses are determined, and whether these are on models that are backed by sound reasoning and available performance data. Refer to Discussion of this Item 4. for sequence of evaluation.

-	ita. Refer to Discussion of this ftern 4. for sequence of evaluation.							
Assignme	Quality Measure	Assignmen	Implementation Characteristics					
nt	Characteristics	t						
High	Use statistically valid methods, including Monte Carlo Simulation to determine probability loss distributions required for evaluation of the portfolio loss statistics determination.	High	The loss for each individual building has been specified by a probability distribution function, and the aggregated loss for the portfolio is expressed as a probability distribution function. Otherwise, Monte Carlo Simulation is employed according to requirements of Section 4).					
Medium	Use assumption of portfolio loss distribution computed for each event in the event set; or use assumption of specific probability distribution for Probable Loss. Statically valid methods are used aggregate loss estimates to the portfolio.	Medium	The loss for each individual building has been specified by a probability distribution function. Assumptions are made for event-loss distribution as a specific probability distribution (such as Log-Normal, Beta distribution) with justification. Alternatively, for only selected buildings that comprise at least 50% of the replacement value of the portfolio. assumptions are made for Probable Loss distribution with closed-form statistical distributions with justification.					

Low	Where the methods used are	Low	Insufficient implementation description. Is presented to
	not specified and/or not		complete an assessment of its characteristics
	described in sufficient detail for		
	a specialist (peer reviewer) to		
	understand the basis of how the		
	computations were done.		

3. **Demand Surge:** The influence of repair cost inflation due to post-earthquake demand for construction materials and labor costs of repair while the market is distorted. This surge in pricing for building services and materials as demand for limited supply can significantly increase in the post-event emergency period. This element should only be considered if demand serge is important in the financial payments for repair are time critical; if not, do not consider this element this element. For events that cause small damage in an area, the assessment of demand surge should be SUPERIOR. If not important to the client, then this element should not be included in the portfolio rating R.

Assignment	Quality Measure and Implementation Characteristics						
Superior	Not used, because experience is limited and no generally supportable approach is in the literature						
	that assures it can be anticipated outside the influence of other uncertain market conditions.						
Good	How the demand surge issue is treated in the damageability analysis and its basis is supported by						
	technical descriptions and indications of the empirical evidence of experience in earthquake and						
	related natural hazard occurrences.						
Fair	Sufficient description and justification of the methodology and model calibration (if historical data						
	available).						
Poor	Important, but not modeled and without justification.						
Bad	Not used.						

3.4 Determination of reliability of assessments procedures for a portfolio of buildings

Having the qualitative measures for Quality Description and Implementation for each component, the corresponding uncertainty values γ_i , for i = 1 to 3 components can be determined from Table 1, where r is the Tabulated β from Table 1. We now have a basis for evaluation of the uncertainty factor for the loss aggregation in Portfolio Loss Assessment process By use of procedures similar to those employed for individual buildings, the uncertainty of the portfolio is taken as the RMS of the uncertainties of the three components using Equations 1 or 2. The value resulting B is the uncertainty contribution of the Portfolio Model evaluation. Since there is only one portfolio model, there are not separate values determined for each building. The contributions of the individual building's assessment reliability will be discussed in Section 5. The division is to ensure that B remains between zero and one. In order to define the Quality of the Portfolio Assessment, the quantitative value γ_i can be transformed to its equivalent qualitative term by the use of Table 2. For statistical reasons the RMS evaluation is preferred over the Simple Average, since its basis is comparable to evaluation used in an RMS process, not just an assumption of equal contribution by addition. B is determined as:

RMS: B=
$$\sqrt{\frac{\sum_{j=1}^{M} r_i^2}{M}}$$
 or WA: $B = \sqrt{\frac{\sum_{j=1}^{M} v_j r_j^2}{\sum_{j=1}^{M} v_j}}$ (5)

At this point, we have achieved the basic objective of describing the *Quality* of the building assessment results either as a numerical *B* or as qualitative descriptor ranging from *SUPERIOR* to *BAD*. The user now has this qualitive basis for the justification of decisions. Also, if reliability needs improvement, the uncertainty contribution of each component is identified, and resources can be allocated to improve related information or adjustments in any particular component.

4 Uncertainty of sample estimates from Loss Simulations

4.1 Considerations of the uncertainty issues of Portfolio Loss Statistics

The determination and form of the assumed probability functions and related operations required for the analytic evaluation of portfolio loss statistics have such mathematical complexity that a closed form mathematical expression is virtually impossible to determine for any measure. In addition, it is difficult and, in cases not possible, to evaluate confidence limits for the results – other than by judgmentally assigned *epistemic* uncertainty values. The epistemic issues have been discussed in Section 3. However, these computational results are subject to sampling (*aleatory*) error. This section addresses this last major source of uncertainty that can affect the quality of the Portfolio Loss Statistics. It is well established that the number of simulations in a Monte Carlo process has a large influence on the reliability of the estimated statistics—where this reliability is represented by the degree to which the sample estimates are representative of the *true* values being evaluated by the process.

The Monte Carlo simulation process provides a large sample size data set of N portfolio loss values which when ranked from largest-to-smallest, including all zero values, is sufficient to determine the non-parametric Complementary Cumulative Probability Distribution Function (CCPDF) for the portfolio loss. The CCPDF allows direct determination of the likelihood of any portfolio loss value being exceeded in a year, PL, as well as in a specified time period of T years for any loss being exceeded or being in any defined loss range. This process provides probability values from 0 to 1.0 with high PRECISION, but not necessarily ACCURACY. The reliability analysis of this paper is intended to determine the degree of reliability of the estimate, that is, its accuracy or measure of uncertainty. The number of simulations must be sufficient to converge to the true value within specified limits of accuracy, however, even then, the uncertainty bounds for losses will not be reduced to zero. The client/user must be provided with a sufficient representation of this uncertainty in order to make responsible decisions.

It is usual practice that each simulated value L is the Portfolio Loss that can occur during a one-year period of exposure to all possible earthquakes that can occur. The ranked (largest to smallest) order statistics of the simulated values provides a sample representation of the CCPDF. This provides an estimate of the probability of exceedance for any specific simulated value. However, while we can clearly state a numerically precise value for this estimate, we need to pay attention to the following advice of Wasserman and many other authors related to such estimates:

The main point to keep in mind is that an estimate of f_n without some sense of the confidence set is usually not useful. (Wasserman, 2006, page 57) (N.B., f_n is the probability density function estimate for loss.)

While the reliability/uncertainty of the sample estimate of a probability of exceedance or any other portfolio loss statistics can be improved by increased number of simulations, the accuracy is also dependent on the method of drawing samples from the simulated data set; this *sampling procedure* will be addressed in the next Section. Typically, the number of simulations, *N*, depending on the characteristics of the portfolio, is very large. The following section addresses the issue of expressing the uncertainty of the loss statistics that are estimated from the simulated data (e.g., Coefficient of Variation, CV). It is important to recognize that it is common that financial decisions are based on the high, but rare reported PL value (such as for 500-year return period), and therefore it is most important to be able to assess the reliability of estimates of these *upper tail* portions of the loss. Special attention is needed because fewer simulated values occur in the *upper tails* (since there is a lower probability of being selected in the simulation process).

We discuss two issues on this subject to characterize the uncertainty of the CAT computational results as presented in a Portfolio PML report:

- The quality of the definition of the calculated loss parameters from the CAT model;
- How the uncertainty in the Portfolio loss distribution function has been represented, such as, is a confidence value given for the reliability of the specific

loss results, including CV, and probability of exceedance and any other numerical statistic of the process.

These issues are addressed in the next sections.

4.2 A reliability computational approach using *Bootstrap* sampling

With the advent of fast, high capacity, computational systems, new techniques of data sampling are now feasible. Wasserman reports on the extensive statistical literature concerning how to interpret Monte Carlo simulations and extract reliable information from them, (Wasserman, 2006). Obviously, the number of simulations has a great impact on the reported loss statistics. The basic issue when making a financial or policy decision based on a loss estimate is to have a measure of the reliability of the reported loss value for a specified likelihood of being exceeded (e.g., 50th and 90th Percentiles, or 225- and 500year return period). In classic Parametric Statistics the width of Confidence Bands for an estimated parameter is, essentially, inversely proportional to the square root of sample size N. However, for the Non-Parametric Statistics (e.g., order statistics) of simulated data, the confidence bands vary with the number of data values greater than the *Statistic* that is being estimated. It is observed that the accuracy of the CCPDF for seismic loss estimates decreases with increasing loss values. Thiel and Zsutty show this is the case for 17 sites in California, Nevada, Oregon, Utah, Washington, and Guam for the same marginal seismic performing building types, (Thiel, Zsutty, 2018), and for individual buildings having a wide range of damageabilities, from very low to very high, at 14 US sites, including Alaska, (Thiel, 2001). The model portfolio, as assessed in Section 4.3, exhibits this behavior in its Figure 2. For the user/client, in practice, it is common that the financial decisions based on portfolio loss assessment are usually focused on the PL tail risk, for example, a 250- or 500-year return period for exceedance, equivalent to a respective annual probability of exceedance of 0.4% or 0.2%. These low probability, high damage loss levels, are characterized as the tail risk portion of the loss curve and also may be characterized in practice as the *right tail risk*. It is reasonable for the uncertainty of the evaluations of these very low probability of exceedance loss values to have higher uncertainties because, in their high value range, there are radically fewer simulation results than for the values nearer to the central losses. Therefore, we assert that to use a full range of complementary cumulative probability distribution function uncertainty values to represent the uncertainty of all loss values would be misleading. The following discussion proposes an approach to how the uncertainty for a given loss value can be determined based on how Monte Carlo damage assessment results are statistically examined by sampling procedures.

Given that we have the results of a Monte Carlo simulation of N loss values from the assessment of the earthquake loss of a given portfolio, we propose a rather direct way to determine the reliability statistics of the loss values of interest. The simulation results are given as a group of losses {Li, i=1, N} that could occur in a one-year exposure due to the hazard of the Event Set. This group must include all the simulations that resulted in zero values. The group represents all the realizations of the probabilistic process of assessing the aggregated loss value for the portfolio. By the process of ordering the values of Li, from largest to smallest, we can directly estimate the probability that any selected value L_i will be equaled or exceeded by determining the ratio of the ranked sequence number N_i of the element L_i to the number N of total simulations (this is called an *Order Statistics* method of determining an empirical CCPDF. In terms of Non-Parametric Statistics, the Probability of $(L \ge L_j)$ is estimated by the ratio N_j/N . From the full set of N loss values, we could also determine: the estimate of the Portfolio Expected Loss as the sample expected value, the median loss, along with the loss variance. Further, with the CCPDF we can estimate the likelihood of exceeding any loss level. However, the basic problem is that we need confidence intervals for these and other specified loss statistics based on sample estimate values. In order to fulfill this requirement, we will employ what is termed in statistics a *Bootstrap* resampling procedure to develop the confidence intervals for loss values of interest from the Monte Carlo array of Portfolio Loss simulations.

Classical Parametric Statistical Methods assume that sample data are drawn from a known Probability Distribution Function, and use the full sample of size N to estimate the parameter values of the assumed Probability Distribution. Applicable parametric tests are then employed to compare the sample estimates to the true parameter values. For example, for an assumed Normal Distribution, the confidence limits of the true mean value involve use of the Students t-distribution (with N-1 degrees-of- freedom) about the sample average value. However, for the case of Portfolio Loss we have no a priori notion of what the true Probability Distribution function is for this loss, and as a consequence we have chosen to use non-parametric statistical methods. Non-parametric statistical uncertainty assessment depends on the observation that the sample set of values represents all of the reliable information available, and there is no need to assume a parametric probability distribution function for the data. This observation is particularly applicable for the case of Monte Carlo simulations where the sample size can be of the order of 10^4 or more. Specifically, we will use *Bootstrapping*: a method that uses M resamples with replacement of each individual randomly selected data value, from the original data in order to form M sets of independent possible occurrences based on the same data. Bootstrapping can be used to assign measures of accuracy (mean, variance, confidence intervals, prediction error, or any other statistic) to sample estimates from the M resampled sets, (Efron and Tibshirani, 1993, Wasserman, 2006, Davidson, Hinkley, 2009, Halpern, 2017). The resulting set of M sample estimates can be assumed to be from an independent and identically distributed population of N simulated data values. The basic steps of the Bootstrap procedure are as follows:

- 1. Construct an empirical probability distribution function, $\hat{F}(x)$, from the sample placing a probability of 1/n at each point $x_1, x_2, ... x_N$. When this is ordered from smallest to largest, it is the empirical distribution function (EDF) of x, which is the nonparametric maximum likelihood estimate (MLE) of the population distribution function F(x).
- 2. Determine the k loss values for which probability confidence limits are desired, θ^k , and determine what number of resamples, M, should be completed.
- 3. Select a random sample of size N equal to the number of simulations with replacement from the original set of values. This is the *resample* set x_1^* .
- 4. Calculate the statistics for each θ^k from this resample, yielding $\hat{\theta}_i^k$, where *i* is the sequence number of the k^{th} resample.
- 5. Repeat Steps 2 and 3 M times. The confidence values for each loss of interest is represented by the set $\hat{\theta}_i^k$.
- 6. Construct a probability distribution for from the $M \, \hat{\theta}_m^*$'s by placing a probability of I/M at each point, $\hat{\theta}_1^*$, $\hat{\theta}_2^*$, ... $\hat{\theta}_M^*$. This distribution is the Bootstrap estimate of the sampling distribution of $\hat{\theta}$, $\hat{F}^*(\hat{\theta}^*)$. From this the standard deviation and the mean determined the CV can be calculated, as can any percentile statistic of the process. The implementation of this step is discussed below. [adapted from Mooney, Duval, 1993)

Note that even though each resample has size N equal to that of the complete data set, the randomized selection of each value, with replacement, results in a different set of the N values in probability. It is possible that some initial values will have multiple realizations in a resample and some values will not appear at all. Because it is unusual that in Portfolio loss analysis many simulations, often a 100,000 simulations made of the order of 100 or fewer resample may be sufficient. If for one or more of the loss values of interest, the number selected is not sufficient to get an acceptable confidence limit, then additional resamples can be implemented with limited effort. As will be seen in Table 12, the coefficient of variation (CV) converges quicky with 30 resamples for the 500K Model Portfolio simulations. As Efron and Tibshirani state: Bootstrapping is used not to learn about general properties of statistical procedure, as in most statistical procedures, but rather to assess the properties for the data at hand. Nonparametric bootstrap inferences are asymptotically efficient. That is, for large samples they give accurate answers no matter what the population, (1994). These results are technically considered to be more accurate aggregate statistics of the simulated process than the raw set of original values would provide by the original simulations, (Davidson, Hinkley, 2009).

A simple and reliable way to make this conversion to continuous values is to use the Microsoft Excel functions PERCENTILE.INC(array, k) or PERCENTILE.INC(array, k) to

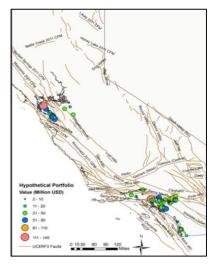
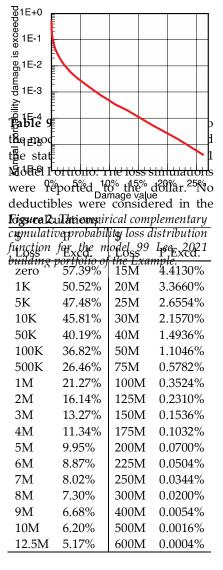


Figure 1. Reproduction of the model 99 building portfolio assess by Lee indicating the location and value of the buildings by the color and size of the filled circle. (Lee, 2020A).



determine the array value at a specified percentile of interest (*k*). This is an implementation of the Percentile methods discussed by Davidson and Hinkley, (1999). These functions use interpolation methods to obtain values not limited to the specific values for each element in the sorted array. We expect this method to work well for the Bootstrap samples for Portfolio Loss because the functional form of the empirical distribution functions is quite regular, approximating an exponential decay function. One can use the PERCENTILE.EXC function to determine the percentile exclusive of the first and last values in the array, or use the PERCENTILE.INC function to determine the percentile inclusive of the first and last values in the array. We prefer the INC version, although they tend to yield the same results for 10 or more sets, but they do not for a smaller number of values.

4.3 Example results for a model portfolio of buildings

We analyze an example of assessed loss results for a model portfolio that was the subject of a recent paper by Lee, (2021). The portfolio is composed of 99 buildings in two regions within California as shown by the map of their locations along with their relative values, see Figure 1. The total replacement value of the portfolio is about \$2.3 billion, with about \$1.7 billion in Southern California and \$0.6 billion in Northern California. Among the 100 buildings, 77 are low-rises (1-3 stories), 17 are mid-rises (4-7 stories) and 5 are high-rises (8 stories and above). The portfolio was modeled using HAZUS damage method

(HAZUS, 2013). All low- and mid-rises are modeled as Concrete Shear Walls (HAZUS Model Building Type: C2L and C2M, respectively) and all highrises are modeled as Steel Moment Frame (HAZUS MBT: S1H). The seismic Design Code used varies according to the age of a building, with pre-1975 modeled as Moderate Code (MC) and post-1975 modeled as High Code (HC). Occupancy Type is uniformly COM4 - Professional/Technical Services (Office). For damage uncertainty, a random ASTM 2024-16a Level of Investigation 0, 1, and 2 is assigned for each building. Lee, (2021) performed a Monte Carlo simulation of 500,000 losses for a one-year period of exposure to the related events sets. These simulated annual losses include the possibility of several earthquakes occurring within the same year time window, and also include zero values when no damaging events occur. Figure 2 gives a graphic indication of the loss values in a year and the probabilities of their exceedance. Note the large number of zero loss simulations, as expected. It is often useful to plot the complementary cumulative distribution function to verify that it is regular. The model portfolio data of Table 9 are plotted in Figure 2, which indicates that the base data are regular in that they are monotonically decreasing in a smooth, uninterrupted manner. Portfolio loss curves are typically of this shape.

From the table of 500K

(Lee, 2021) simulations, we formed M=30 Bootstrap random selections of N=500K simulations, each individual value selection with replacement, that is, each entry was determined as a random selection from the original simulated loss table. Thus, the 30 sets constitute a selection of 15M samples from the original 500K loss simulations. The Bootstrap sampling method is used to examine the reliability of the mean, standard deviation and other statistics (such as high tail values) of a random set of resampled simulations; here the procedure is to refine their values by computing the specified statistics for each of the 30 independent resamples and comparing them,

(DiCiccio, Efron, 1996, Davison, Hinkley, 2009, Wasserman, 2006). The probability values were determined using the Excel Percentile.inc function for the resample results as discussed above.

Table 10 assesses the differences from the median of the upper and lower bounds and other statistics of the Bootstrap results for the N=500K total

simulations. The Lee and Bootstrap values are close for the averages. Note that the values for the average match well those of the original data set from

(Lee, 2021), as expected for such a large sample. However, the variability increases drastically as the damage values increase. It is clear that the estimation process using 30 500K resamples worked quite well. Lest this be viewed as a major task, the run time on an IMAC Excel spreadsheet was less than 10 minutes to produce these results. Using the values of Table 10 we can determine a lower and upper bound 80% confidence limits for the annual risk of a \$100M loss as (0.343%, 0.362%). For comparison we have calculated the corresponding 90% confidence limits as [0.305%, 0.421%]. We shall call these the confidence limit (CL) bounds for a specified probability of exceedance limits. The upper limit represents the highest risk, and is thereby more likely to be weighted in financial risk management decisions. However .it is prudent to consider the whole range to remain objective.

As will be seen in Section 5.2, the coefficient of variation (CV) plays an important role in the description of the degree of reliability of the portfolio estimates of loss statistics. We will consider two approaches to presenting the loss and the probability of the loss being exceeded; one focusing on the dollar amount, and the other on the probability that the loss is exceeded. In practice it is common that portfolio loss reports focus on the probability that a given dollar loss is exceeded, or on the loss for a given probability of exceedance. Many insurers are interested in the likelihood of losses exceeding a fixed dollar value. Table 11 reviews the calculated coefficients of variation (CV) for different dollar losses to the Model Portfolio. These values clearly indicate that if large loss values are of interest, then the number of simulations *M* in the bootstrap sample has a significant influence on the uncertainty of the results. It may be convenient to specific the criteria for acceptability uncertainty are set in terms of the probability that critical loss values of interest. Table 12 shows first the damage values expressed as PL for the 500K30 analysis, and the CV results for the four simulation strategies of Table 11 over a wider range of probability values. As a caution, strictly speaking the very high CV values can be lowered by performing more bootstrap resamples. However, a high number of resamples will not change the probability loss value above 10% by much, and the basic degree of uncertainty as obtained from Table 2 will still be qualitatively evaluated as GOOD or better, (see bias estimation for Monte Carlo simulation in Davison, Hinkley, 2009). It is notable that the CV values are similar over the full range of lower loss percentages for the different simulation numbers, but their CV values become significantly larger as the loss value

Table 10. Bootstrap for 500K30 simulation of the Model Portfolio loss values to determine the probability ranges for individual loss values. The 10% and 90% headers indicate the probability of the damage exceeding raw loss value. CV is the coefficient of variation (Standard Deviation/Average). The [Lee, 2021) values are the probabilities associated with the original simulation data set. The remaining values were determined from the statistics of the resampled sets using the PERCENTILE.INC. function.

Loss	Min	10%	Average	Median	Lee, 2021	90%	Max	CV
\$10M	6.115%	6.160%	6.192%	6.196%	6.200%	6.226%	6.236%	0.5%
\$25M	2.618%	2.628%	2.653%	2.656%	2.655%	2.675%	2.700%	0.8%
\$50M	1.074%	1.081%	1.101%	1.102%	1.105%	1.120%	1.131%	1.3%
\$75M	0.564%	0.565%	0.577%	0.578%	0.578%	0.587%	0.602%	1.7%
\$100M	0.343%	0.343%	0.351%	0.349%	0.352%	0.362%	0.371%	2.4%
\$150M	0.141%	0.143%	0.152%	0.152%	0.231%	0.160%	0.165%	4.0%
\$250M	0.031%	0.032%	0.034%	0.034%	0.034%	0.036%	0.045%	7.9%

Table 12. Comparisons of the loss values with the CV for the percentage loss for exceeding the loss value for the Model Portfolio for different Bootstrap approaches depending on the original loss Monte Carlo simulation total. 500K30 means 500K. The portfolio value is \$2.3 Billion. The column Occurrence indicates the probability of the loss value is exceeded as determined from the 500K30 simulations results. The annual expected loss, AEL, of the 500K30 simulations is 0.122% and the CV of this loss for the different simulation numbers are as indicated; The CV are so low because there are so many loss simulations below this loss value.

simulations below this loss value.								
	CV							
Occur-	20K3	100K3	200K3	500K30				
rence	0	0	0					
57.4%	0.27%	0.27%	0.16%	0.10%				
43.3%	0.27%	0.27%	0.25%	0.15%				
31.9%	0.33%	0.33%	0.34%	0.19%				
15.2%	0.67%	0.67%	0.56%	0.29%				
9.16%	0.93%	0.91%	0.66%	0.39%				
5.57%	1.1%	1.2%	0.9%	0.5%				
2.94%	1.8%	1.7%	1.4%	0.7%				
1.26%	2.5%	2.5%	2.0%	1.3%				
0.680%	3.6%	3.6%	2.0%	1.7%				
0.420%	4.8%	4.5%	2.8%	2.1%				
0.276%	6.0%	5.8%	3.9%	2.7%				
0.113%	10.6%	10.6%	7.6%	4.3%				
0.0490%	13.1%	13.1%	10.0%	6.3%				
0.0250%	15.9%	15.7%	12.3%	6.8%				
0.0140%	33.6%	30.1%	23.5%	12.3%				
0.0030%	66.6%	61.5%	42.6%	24.4%				
AEL	3.90%	1.39%	0.95%	0.66%				
	Occurrence 57.4% 43.3% 31.9% 15.2% 9.16% 5.57% 2.94% 1.26% 0.420% 0.276% 0.113% 0.0490% 0.0250% 0.0140% 0.0030%	Occurrence 0 57.4% 0.27% 43.3% 0.27% 31.9% 0.33% 15.2% 0.67% 9.16% 0.93% 5.57% 1.1% 2.94% 1.8% 1.26% 2.5% 0.680% 3.6% 0.420% 4.8% 0.276% 6.0% 0.113% 10.6% 0.0490% 13.1% 0.0250% 15.9% 0.0140% 33.6% 0.0140% 33.6% 0.0030% 66.6%	Occur- 20K3 100K3 rence 0 0 57.4% 0.27% 0.27% 43.3% 0.27% 0.27% 31.9% 0.33% 0.33% 15.2% 0.67% 0.67% 9.16% 0.93% 0.91% 5.57% 1.1% 1.2% 2.94% 1.8% 1.7% 1.26% 2.5% 2.5% 0.680% 3.6% 3.6% 0.420% 4.8% 4.5% 0.276% 6.0% 5.8% 0.113% 10.6% 10.6% 0.0490% 13.1% 13.1% 0.0140% 33.6% 30.1% 0.0030% 66.6% 61.5%	Occurrence 20K3 100K3 200K3 rence 0 0 0 57.4% 0.27% 0.27% 0.16% 43.3% 0.27% 0.27% 0.25% 31.9% 0.33% 0.33% 0.34% 15.2% 0.67% 0.67% 0.56% 9.16% 0.93% 0.91% 0.66% 5.57% 1.1% 1.2% 0.9% 2.94% 1.8% 1.7% 1.4% 1.26% 2.5% 2.5% 2.0% 0.680% 3.6% 3.6% 2.0% 0.420% 4.8% 4.5% 2.8% 0.276% 6.0% 5.8% 3.9% 0.113% 10.6% 10.6% 7.6% 0.0490% 13.1% 13.1% 10.0% 0.0250% 15.9% 15.7% 12.3% 0.0140% 33.6% 30.1% 23.5% 0.0030% 66.6% 61.5% 42.6%				

Table 11. Comparisons of the CV of the dollar losses for the Model Portfolio for different Bootstrap approaches depending on the original loss Monte Carlo simulation sizes of N = 20K, 100K, 200K, and 500K. 500K30 means 30 resamples of 500K each.

-	CV					
Loss	20K30	100K30	200K30	500K30		
\$10M	2.6%	1.1%	0.8%	0.5%		
\$25M	4.9%	1.8%	1.4%	0.8%		
\$50M	9.3%	2.9%	2.1%	1.3%		
\$75M	11.3%	4.0%	2.3%	1.7%		
\$100M	12.5%	5.3%	3.0%	2.4%		
\$150M	19.0%	7.9%	6.0%	4.0%		
\$250M	35.1%	17.0%	11.9%	7.9%		

increases. This makes sense if you note that the number of non-zero expected number of occurrences for 5% exceedance probability is 25,000 for the 500K30 case, of which 43% are zero, or about 14,250 losses greater than zero, while for 0.0056% exceedance probability the number is 28 non-zero values, on which the CV for the loss value depends. Clearly, the confidence in drawing firm conclusions is significantly different for these two values as seen in the comparative CV values. The annual expected loss to the portfolio (AEL), shown at the bottom of Figure 12, is the calculated value of a "lower bound fair value" for the insurance cost. In many cases the loss will be determined using a deductible, in which case the loss would be lower but the analysis will be similar.

4.4 Assigning an uncertainty parameter for computation of statistics from simulated data

There are two primary issues that have been discussed above that can affect the Quality and related uncertainty of reported Portfolio Loss Statistics:

- First, whether or not the CAT Model loss assessment procedure has been described sufficiently in order to verify that the methods are valid and the input is representative of the portfolio and location. Were the reported results described in an appropriate statistical terminology related to loss and risk occurrence? In order to detect possible sources of uncertainty, there should be a reasonably descriptive presentation of the CAT Model procedures by the performer so as to allow the user/client to assess the validity of the essential steps of the model and their implementation.
- Second, whether or not the computational uncertainties in the reported results are presented, and, if so, how were these uncertainties determined, and does the procedure have statistical validity? If the provider gives confidence bands it is assumed that they will provide at a minimum, loss value confidence estimates for specified loss statistics specified by the client, or confidence bands for all the loss values reported. Few CAT models are known to report confidence ranges or even provide qualitative discussions of confidence for loss values. In the opinion of the authors this is an important addition to the reporting of loss values in Portfolio studies and will serve to provide a considerable enhancement of knowledge to the users/client for purposes of decision making. See Section 4.4.

Table 13. Definitions of Measure Characteristics and Implementation Characteristics for the components of the Loss Simulations evaluation. These are assumed to be given as a probability of the damage level confidence bound for median probability for a given dollar loss. Not all loss values will have the same confidence span. The resulting uncertainty values determined from Table 1 will be labeled C. Note that the actual computed CV is not considered in this evaluation, it is considered in Section 4

Assignment	Measure Characteristics	Assignment	Implementation Characteristics
High	ligh Medium requirements plus reports full		Coefficients of variation (CV), and/or
J	annual damage PDF of portfolio loss		Confidence Limits (CL) are provided for the
	values.		principal reported damage loss value(s).
			Discussion provided indicating how these
			CV and/or CL were determined.
Medium	Medium Low requirements plus specify how the		Qualitative discussion is provided
	portfolio loss levels were determined,		concerning the possible ranges of variability
	including the number of simulations used		of the principal reported damage loss
	and how they were processed.		values.
Low	Report includes portfolio annual loss	Low	No confidence levels or discussion of
	probability of exceedance values levels for		uncertainty is provided for reported
	selected damage levels with minimal		damage loss values
	technical support for the methods		
	employed and their technical basis.		

Table 13. presents the matrix process proposed to be used to determine the uncertainty factor for these two issues. From each matrix, the resulting pair of Quality assignments (for Description and Implementation) are to be used in Tables 1 and 2 to evaluate the Portfolio Computations uncertainty value C. The resulting quantitative value can be expressed as a qualitative term from Table 2.

We have considered the problem of how to assign a qualitative reliability term for a particular loss value that has a CV value of 0.50. The authors would characterize this value for a loss as *BAD*. Using this assignment as the basis for measurement, we can express the qualitative uncertainty of a given CV(L) value by using one half of the limits the Table 2 entries as appropriate interpretations of CV reliability terms assignments. Table 14, is used to characterize these as uncertainty, *S*. Using these definitions, only 1 of the 500K30 loss values (20%) in Table 12 would qualify as rated *BAD*, and all the loss values below12.5% for the 20K30 to 500K30 bootstraps would qualify as *FAIR* or better; all of the AELs rate *Superior*. Because these uncertainties are variable based on the loss value under consideration, we have not included them in the quality assessment considered in this Section, but will use it in Section 5.2 for rating a numerical loss reliability.

5 Portfolio Reliability Evaluation

5.1 Statement of the uncertainty issues considered

This section addresses the combination of the uncertainties involved the results of Portfolio Loss Assessment. The prior Sections 2, 3 and 4 have addressed the assignment of the uncertainties in terms as quantitative measures of the reliability or quality of each of the essential phases of a portfolio loss evaluations. These measures are:

A.The combined uncertainty of the individual building damageability assessments *A* as determined in Section 2.4.

B. The uncertainty of the algorithm (CAT Model) that determines the aggregated loss for the portfolio of buildings in earthquake events, as represented by *B* in Section 3.4.

C. The uncertainty of the Monte Carlo computational process employed to simulate the aggregated portfolio loss (here, in terms of loss due to a one-year period of exposure to the event set hazard), and how the statistical sampling uncertainties of the reported loss results, as represented by *C* in Section 4.4.

Table 14. Assignment matrix for the uncertainty assessment of a specific CV value, termed S. These assignments will be used in Section 5.2. These were determined as one-half the Table 2 limit values for the qualitative level.

	1	
S Assignment		CV value
Superior		CV≤0.075
	GOOD	(0.075 <cv≤0.1375< td=""></cv≤0.1375<>
FAIR		0.1375 <cv≤0.2125< td=""></cv≤0.2125<>
	Poor	0.2125 <cv≤0.375< td=""></cv≤0.375<>
	Bad	CV>0.375

We note that *A* and *B* have to do with the theoretical (epistemic and aleatory) uncertainties introduced by the method of analysis, and *C* relates to the (aleatory) uncertainties of evaluating the specific reported results from the simulated data set. In this Section we combine these measures into a value that applies to the results of the Portfolio Loss assessment. We designate the quantitative uncertainty of the Portfolio by the symbol *R*. As before, the quantitative values of uncertainty are used in order to provide a logical method of combination by the use of the RMS method employed in Equation 2:

RMS:
$$R = \sqrt{\frac{A^2 + B^2 + C^2}{3}}$$
 or WA: $R = \sqrt{\frac{v_A A^2 + v_B B^2 + v_C C^2}{v_A + v_B + v_C}}$ (6)

In the left Equation it is assumed that all of the uncertainty measures have equal importance. The Equation on the right allows the assignment of differing weights of importance, v_j for the j^{th} uncertainty measure. The authors prefer the RMS option because in our opinion the three contributors to the uncertainty of the portfolio are of equal importance. However, there may situations, perhaps depending on the special characteristics of the portfolio, or the particular situation of the user-client, where the WA option might be useful. It is important to note that when only one buildings is being assessed, that the B is not applicable and the Equation 6 is reduced to only including A and C, and reduction of the divisor to 2. If the analysis has only one site, but possible several buildings, then R depends on only A, and R=A.

R represents the uncertainty/reliability of the assessment and includes the representation of the epistemic error in the CAT Model and associated simulation process, and the aleatory error in the sample estimates of the portfolio loss statistics. The quantitative value of *R* can be expressed as an equivalent qualitative term by use of Table 2—if desired for effective communication.

It is interesting to evaluate the impact of different levels of quality for the three measures (A, B, and C) on the overall reliability of the portfolio using the RMS procedure. The results can useful for indicating where more information is required to achieve an acceptable reliability or for setting requirements for a proposed assessment. The RMS rating for one SUPERIOR, one GOOD and one FAIR is 0.24, which falls in the range given in Table 2 for GOOD. Table 15 allows the evaluation of many of the possible options assuming that the values of the elements are consistent with Table 2 central values. It is clear that the likelihood of getting an acceptable rating (FAIR) is not possible if one of the valuations is BAD. However, as long as none of the ratings are below FAIR, it is still possibly to get a FAIR rating. If the client is careful in the setting of the criteria for the completion of the assessment report, then it should be relatively easy to achieve a GOOD or better rating for A. Also, it should not be difficult for any competent technical provider performed to get a GOOD or better rating for B. The governing likely issue will be the justification for the incremental cost of getting a GOOD or better rating for A, which may require locating and reviewing the drawings and having a qualified person visit the building. This could be accomplished by managing the level of investigation prudently; for example, doing the higher level of investigations for selected buildings, particularly for those of high value or very high loss risk, and the toleration of a lower level for those buildings of low relative

Table 15: Impact on the having various A, B and C values from the qualitative value set, with one (1x) or two (2x) values set at a different variable value. Green highlighting indicates that the R qualified for a SUPERIOR rating per Table 2, blue indicates GOOD, uncolored indicates FAIR, and orange indicates POOR or BAD.

	Variable									
Fixed	1x0.1	1x0.2	1x0.35	1x0.5	1x1.0	2x0.1	2x0.2	2x0.35	2x0.5	2x1.0
0.10	0.10	0.14	0.22	0.30	0.58	0.10	0.17	0.29	0.41	0.82
0.20	0.17	0.20	0.26	0.33	0.60	0.14	0.20	0.31	0.42	0.82
0.35	0.29	0.31	0.35	0.41	0.64	0.22	0.26	0.35	0.46	0.84
0.50	0.41	0.42	0.46	0.50	0.71	0.30	0.33	0.41	0.50	0.87
1.00	0.82	0.82	0.84	0.87	1.00	0.58	0.60	0.64	0.71	1.00

value—the objective being to achieve financial feasibility. introduction of proposed ASTM level $LI_{0.5}=0.5$, Investigation Section 4.2, for Portfolio Assessments, should facilitate the focusing of added effort on those assets making the largest contribution to the uncertainty of the high, tailend loss values.

It is necessary in the author's view for the client who proposes to utilize the results of a seismic assessment to determine whether the methods used are expected to yield results that are sufficiently reliable to warrant action. The uncertainty index *R* provides a direct manner to make a decision on its reliability. Table 16 provides an example of how this uncertainty measures could be used to guide decisions. For the case of a POOR or BAD Quality evaluation, it is recommended that no decision be made based upon the evaluation, unless that decision is made to reassess risk. If action is necessary, then complete a higher level of evaluation to be its basis. This should include a preinvestigation considerations of the requirements for the assessment to be done, and a prequalifications of the performed to verify that they are capable of meeting the reliability requirements for the actions under consideration. Note that Table 15 suggests by exclusion of the orange highlights the combinations of A, B, and C assessment values likely to yield SUPERIOR, GOOD or FAIR R index values for any assessment based its characteristics. The matrix Tables 3, 8 and 13 should aid the client is setting the minimum standards for procurement of seismic assessments that are acceptable. Clearly it would be useful for clients to set the criteria for its seismic assessment at a level sufficient to be actionable before the assessments are done.

When a building or portfolio has been assessed to determine its seismic performance and uncertainty R assessment, then R provides a basis for deciding whether or not actions are warranted based on the assessment's conclusions. Table 16 provides example guidance of how the uncertainty measure could be used to guide decisions. For the case of a POOR or BAD R rating, the authors recommended that **no** decision be made based upon the evaluation, except possible to complete a more reliable assessment on which to make a decision. A FAIR rating is in the author's opinion marginally reliable depending on the decision to be made/ A GOOD or SUPERIOR rating should be adequate in most circumstances.

The Thiel-Zsutty Revised (TZR) model damage estimation for single buildings, [Thiel, Zsutty, 2017], expresses the reliability of the damage estimation process through assignment of an α multiplier factor applied to the computed standard deviation of the Beta Distribution model. The α factor can range from 0.25 to 1.5, depending on the respective quality of the estimation process. The R value, as presented in TZR Section 8 and adapted for single building damageability, can be employed to evaluate this α factor. By the tacit assumption that: α =0.4 for an R rating of Superior, 0.75 for R of Good, 1.0 for R of Fair, 1.25 for R of Poor and, 1.5 for R of Bad, then a relation can be made by the logarithmic fit of α =0.486 ln(R)+1.530, for the assigned numerical value of R that is representative of the quality of methods used; this curve fit has a squared correlation of

Table 16. Proposed decision matrix for how to act upon the assessed confidence in the reliability of assigned seismic performance level of the building R.

R, Seismic	Recommended for implementation actions			
assessment	based upon the reliability Quality R.			
reliability	(Acceptable or Not-Acceptable).			
CURERIOR	Very High reliability, assessment			
Superior	conclusions should be acceptable.			
GOOD	High reliability, assessment conclusions			
GOOD	should be acceptable			
	Marginal reliability. If this rating is			
	acceptable, no further action required. If			
FAIR	rating is not Acceptable then do not act on			
FAIK	the conclusions of the assessment, and/or			
	investigate actions to revise the assessment			
	to yield an Acceptable conclusion.			
POOR/RAD	Not reliable. Take no actions based on the			
Poor/Bad	assessment's conclusions.			

r²=0.993, rated as quite good. This allows the use of detailed process leading to the single building *R* rating to be employed for the standard deviation modification of the TZR model.

5.2 Influence of portfolio assessment reliability on a portfolio loss estimate

For those cases where the numerical loss values are reported in the assessment, we are now in a position to rate of the reliability of these values based on the corresponding values of the R of the portfolio assessment. However, while the value of C gives credit (better Quality) if the CV is reported for a loss value, there is, as yet, no representation of the effect of the corresponding (large or small) value of the CV. The influence of the CV cannot be included directly in the C value because the CV is different for each specific loss statistic: we need to know what loss statistic is, such as, mean, or 500-year return period, in order

to know the corresponding *CV*. As noted in Section 4.4.2 for the (Lee, 2021) Model Portfolio Example in Tables 11 and 12, the value of the *CV* increases significantly for the *high tail* loss levels having low probabilities of exceedance: these *CV* values range from less than 1% to over 66%, depending on how many Monte Carlo simulations are completed and how far out the tail loss is considered. The total uncertainty of a specific loss statistic can be determined by combining the uncertainty of the portfolio, *R*, with the uncertainty of the computations as represented by the *CV* value of the respective loss statistic as noted in Table 14. As noted in Section 5.1, if the reliability index *R* is rated as *Poor* or *Bad*, then this formula should not be used; the quality of such an assessment is not judged sufficient to recommend use of the assessment's results Table 17 presents recommendations of the reliability index for a given loss computation based on the quality index of the Portfolio assessment procedure *R* from Equation 6 and the *CV* value for the loss *S* from Table 14.

It is recognized that the individual client's needs and conditions may cause different values to be assigned for these thresholds. Referring to the values of Table 12 for the Model portfolio, the *AEL*, that is the expected or average annual portfolio loss, has *CV* values less than 5% for all the simulations completed. As a result, even if the assessment quality *R* is rated as *FAIR*, the reliability of the damage estimate will be *GOOD*. For a loss of 15% or lower, the 500K30 values are all in the *SUPERIOR*, which will yield a *GOOD* evaluation overall for an *R* value of *FAIR* evaluation, while only for losses less than about

Table 17. A qualitative rating assignment based on the aggregate reliability of CAT portfolio risk estimates based on the reliability of the CAT model computations and the Reliability value R and the S assessment for the individual numerical value for the loss being evaluation. Note that for each loss values considered, a separate Reliability Value applies. Consistent with the recommendations of Section 5.1, R values of Poor and Bad are not considered.

	S, CV						
R	SUPERIOR	Good	FAIR	Poor	Bad		
Superior	Superior	Good	Good	Fair	Poor		
Good	Good	Good	Good	Fair	Poor		
Fair	Good	Fair	Fair	Poor	Bad		

6% will the 20K30 values be *GOOD*. The message is that having enough simulations completed can have an important influence on the reliability of the values computed and subsequently used in the financial decision. The advantage of obtaining an increase in simulations is that it does not require an increase in the analysts' time, but only computer time. If small adjustments are made to some building investigations using the Lee approach of Section 2.2 to identifying the buildings that contribute the most to the tail-loss contribution values, then it may be easy to achieve a CV less the 5%, (Lee, 2021).

6 Conclusions

The essential purpose of this paper is to understand that Seismic Loss assessment conclusions are, at their base, uncertain. It is important to recognize that there is inherent

uncertainty in the results of all professional seismic performance assessments; this condition was well stated by Justice Roger J. Traynor in 1954: Those who hire (professionals) are not justified in expecting infallibility, but only reasonable care and competence. They purchase the service, not insurance, Another applicable warning is where the consultant is providing probability estimates of loss values important to financial decisions: The main point to keep in mind is that an estimate of fn without some sense of the confidence set is usually not useful. (Wasserman, 2006, page 57). And lastly the authors wish to emphasize that statistical sampling error and possible bias, herein characterized as uncertainty, is a feature of any statistical technique or of its results. The expected value of the results differs from the true underlying quantitative parameter being estimated. As a general conclusion, when a client considers the use of a seismic loss assessment result as a basis for a decision and they do not want to be a victim of a decision gone wrong, then there should be a careful consideration and specification of the scope of services for their seismic loss studies. These are needed in order to provide an acceptable reliability/uncertainty of the results. Also, in order to detect possible sources of uncertainty, there should be a reasonably descriptive presentation of the CAT Model procedures by the performer so as to allow review by the client who will be using the results. Further when results are reported, there should be an evaluation of the reliability of the results, e.g., quality and or confidence limits. This follows the legal definition of *being prudent*, a term that means to obtain reliable data, use good judgment, be wise, sensible and reasonably cautious.

A key recommendation is that if the ASTM 2026 definitions of level of investigation of 0, 1, 2, and 3 are to be useful in Portfolio Seismic Loss Assessment, it is advisable for an intermediate Level 0.5 to be added, as discussed in Section 4.2 and as Lee, 2021,

(2021). This allows less intense, but financially feasible investigations of the seismic performance characteristics to be both prescribed and performed, that have a better chance of yielding acceptable reliable conclusions.

This paper has provided an approach to the evaluation of the uncertainties in the process of performing an assessment, and the expression of the confidence that a decision maker should have in making decisions relying on the results of the assessment, including:

- 1. For a Single Building:
 - Quality measures of the results of a specific seismic evaluation (SUPERIOR to BAD) that recognizes all of the sources of uncertainty of the assessment procedure and its execution by the consultant/provider. These include the decisions made in the approach selected for the engineering evaluation and the execution of the assessment. These measures provide an effective tool to describe the degree of uncertainty of damage values for individual buildings, whether ASTM E2026 Scenario Loss or Probable Loss values.
 - Quantitative confidence limits for the loss values where these limits represent
 uncertainties due to both those of the computations, and impacts of the quality
 measures for the assessment performed. The recommended Coefficient of
 Variation (CV) and Confidence Limits (CL) for numerical results includes both
 the *aleatory* damage prediction model uncertainty and the *epistolic* sample
 estimation uncertainty.
 - Quality of earthquake performance rating levels when used for non-numerical evaluations, including safe or not-safe for use, and assigned CEBC related performance ratings assignment I to VII.
- 2. For a or portfolio of buildings located in one or more independent seismic hazard regions:
 - Quality measures (SUPERIOR to BAD) of assessed portfolio loss statistics including SML, SEL, SUL and for ASTM 2026 loss values, and for portfolio loss values PL. The Quality measures include all of the sources of uncertainty of the assessment procedure and its execution by the providing consultant, including decisions made in the approach, the use/or not of engineering evaluation, and the execution of the assessment. The quality of the description of the task required for the evaluation of the necessary components, and the quality of the investigator performing the task are both represented in the component quality assignment matrices.
 - Introduction of the *Bootstrap* sampling method for estimation of Portfolio Loss Statistics for a set of Monte Carlo simulations of the aggregated loss, together with a method for evaluation of appropriate *CV* for the estimated values.
 - Introduction of total reliability assessments for portfolio loss estimate to represent both the aleatory *Bootstrap* sampling error of estimates based the Monte Carlo simulations and with the epistemic uncertainty of the assumptions of the CAT Model application. This leads to different characterizations of the reliability of different loss results from Monte Carlo simulations.

<u>Setting Criteria for Seismic Assessments Before they are Completed:</u> Clearly it would be useful for a client to set the criteria for its seismic assessment at a level sufficient to be actionable before they are done. The Matrix Tables 3, 8 and 14 should aid the client is setting the minimum standards for procurement of seismic assessments and Tables 15 and 16 measures indicate whether or not they are likely to meet the client's needs.

<u>Concerning Portfolio Loss Assessment</u>: For the case where Quality, and/or Confidence Limits have been found to be not acceptable for *prudent* decisions, the probability distribution function and statistics for the entire portfolio loss assessment can be examined and

modified to reflect not only the computational uncertainty, but also the modeling uncertainty and how an improved assessment can be performed. It is immediately obvious that increasing the number of properties, when possible, in the portfolio can be more influential to achieve a stated reliability goal, that would be an improvement in way in which the seismic losses of the individual properties are determined. However, for the most common case of given specific portfolio, it is likely that the only way to improve its reliability is to improve the total reliability of the assessment procedures for selected buildings-principally, those of high value and proximity to major event sources. Again, the specification of the intermediate Level 0.5 of investigation as discussed in Section 4.2, can be very effective in decreasing uncertainty.

Where Can the Reliability Assessments be Useful? At any time that the analysis is intended to inform a decision, either a priori to set the criteria such that the quality of the results will meet the user's needs, or a posteriori to determine if reported assessments are considering to be of adequate reliability to warrant their use. There are a wide variety of decision-making applications, not all of which require a numerical evaluation of the risk of damage likely, for example:

- Whenever a technical assessment has been done of a building's seismic performance. This includes decisions concerning:
 - When a building may be used, leased, or purchased and there is a prudent or required necessity that the occupants, contents, and/or functions performed in the building warrant protection and the assessed result is intended to inform this decision.
 - When insurance is in question as to whether or not it is necessary and if the premiums are acceptable.
 - Whether a building provides adequate seismic performance, e.g., PML report, in order to be considered as a surety for a loan, mortgage or other financial instrument.
- Whenever a technical assessment has been done for the seismic loss risk for a
 portfolio of buildings seismic performance, and/or whether the buildings are
 located at site subject to the same seismic hazard, or at a number of sites, subject
 to differing seismic hazards. The decisions include:
- Whether insurance policies provide appropriate risk coverage consistent with client's needs.
 - Whether Real Estate Portfolio's seismic loss risk is acceptable to investors or financers, and the degree of risk posed by the portfolio to asset protection including the in-place insurance, particularly to evaluate whether the risk of loss to the tranche is commensurate to the premium. *Tranche* is a French word meaning "slice" or "portion." In the world of investing and insurance, it is used to describe a security that can be split up into smaller pieces with varying risk and return and subsequently sold to investors.
- Whenever a technical assessment has been done to support policy decisions, public or private, where these policy decisions:
- Limit or allow use of a specific buildings that are subject to seismic hazards after
 the event. Examples include assessment of emergency services buildings for
 continuity of service after the event. Note that this may become more prevalent, as
 the State of California is encouraging post-event functionality for retrofits and new
 building design.

The uncertainty evaluation method as developed in this paper can be applied for many other technical risk management procedures where complex models are developed to provide critical results for decisions, and the third-party *decision makers* need a measure to determine the reliability of these results. The method is particularly applicable where the evaluation requires the processing of both quantitative (numerical) and qualitative (expert opinion) measures of uncertainty.

Cost control is usually a paramount consideration in the investment decision-making process. When the stakes are high, investors may be willing to pay more to have seismic

loss assessment done well, and will most likely focus on high-end effort for the high relative value buildings. Common acceptable standards for reliability would be: at a minimum of the *GOOD* level, and for those properties expected to be large contributors to the loss, probably want a *SUPERIOR* reliability is advisable. This paper provides a basis for prescribing the requirements of the assessment, before the work is done, such that the results will have a desired quality.

Quality issues are possibly more important for insurance applications than for equity investment. For insurance, there are often some *tranches* of the risk for very low probability of occurrence losses. It is the values at these *right tail* limits of the risk curve that can have the greatest influence on the likelihood of payments being required. However, at these *tail* limits, there is the highest potential for uncertainty (high CV). Therefore, setting the premium for providing such insurance depends on understanding the degree to which these computed *tail* losses can be relied upon. This includes the possible upper and lower bounds of the estimated risk that has the most influence on the actual total loss risk. As seen in Table 12 for the model portfolio, the CV can be quite large and the probability of occurrence very low at the tail of the distribution. These influences are so large, and have such profound implications for the risk levels, that it would be prudent for the insurer to set the quality limits required for the high-risk *tranche* before the loss investigations are performed This action is necessary to reduce the likelihood of a financial mistake to an acceptably low level. The message is clear.

Lastly: This paper, with its proposed method (parallel to that of FEMA P695) of describing and evaluating uncertainty, can serve as an organized model for future improvements in seismic loss assessments, and the method can be applied to many other professional processes where the reliability of results is required. We expect that actual applications in seismic loss assessment will result in improvements when users find that there are better ways of specifying the *Measure* and *Implementation* descriptions of the quality matrices. These future applications may show the need for other components to supplement or replace the matrix elements in this procedure.

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