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Article

Optimizing the CO₂ Emission of Composite Steel-Concrete Beams with External Prestressing

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Abstract: The literature has well established prestressing in concrete beams and its calculation procedures. However, its use in composite steel-concrete beams has increased despite main normative codes lacking a specific approach for it. Designers must, in most cases, combine the available criteria to calculate the standards of steel and reinforced concrete structures. This study aimed to formulate this optimization problem and analyze CO₂ emissions for the optimal design of composite steel-concrete beams with external prestressing. The design variables for the optimization problem include cross-section of laminated or welded profiles, slab height, characteristic strength of concrete to compression, and number of tendons. We obtained a solution for the optimization problem via a genetic algorithm (GA) and a particle swarm optimization one (PSO). Comparative analysis with experimental example and with optimization problem of prestressed steel beam are performed. An parametric analysis to several spams is performed, which enabled to evaluate the factors that most impact CO₂ emissions. According to results, the chosen algorithms effectively obtained solutions for the problem, and PSO usually provided better results than GA. Regarding the final solution composition, steel contributes the most to emissions, welded profiles provided better solutions than laminated ones, and laminated spans of up to 17.5m and welded ones up to 27.5m dispensed with tendons.

Keywords: Composite steel-concrete beams; External prestressing; CO₂ emission optimization; Particle Swarm Optimization; Genetic Algorithm

1. Introduction

The industry and research have widely disseminated the use of composite steel-concrete beams over the past decades. Recent studies show advances in the use of this type of structural element. Lin et al. [1] studied the fatigue behavior of composite steel-concrete beams, finding that several residual cracks occurred when repeated loads equaled stabilized cracking ones, making the beam less rigid as load cycles increased.

Yu-Hang et al. [2] studied the fatigue in shear connectors of composite steel-concrete beams. At first, in a fatigue test conducted on seven specimens, failure occurred due to fatigue stemming from shearing the connectors in specimens with good ductility. The study also proposed a displacement calculation method, which showed effective results.

Xing et al. [3] studied the behavior of composite steel-concrete beams with elastic concrete, which can improve beam ductility and reduce the width of concrete cracks. Hassanin et al. [4] experimentally studied how composite steel-concrete beams externally stiffened by post-tensioned tendons behaved under cyclic loading. Strengthened specimens showed greater ultimate capacity and residual stiffness than unstrengthened specimens due to significant loss of composite action between concrete flanges and steel beams under cyclic load testing.

Despite the growing use of composite steel-concrete beams over the last few years, research has scarcely explored prestressing in these beams, although it has done so for reinforced concrete beams. The literature has few experimental studies, such as Ayyub, Sohn, and Saadatmanesh [5], which

explore the use of prestressed steel-concrete composite beams for their potential application in structures.

Prestressing composite steel-concrete beams can overcome larger spans with slender structures. Thus, studies must analyze the slenderness of structural elements and the environmental impacts they cause to generate more sustainable structures.

The IPCC [6] claims that reducing greenhouse gases is one of the great challenges facing humanity. Its Sixth Assessment Report [7] estimates that human activities currently cause approximately 1.1°C of global warming when compared to the pre-industrial period. The global COVID-19 pandemic reduced economic and industrial activities, but construction alone emitted 3.2 gigatons of CO₂, contributing with 10% of all greenhouse gas emissions worldwide. (UEIEA [8]).

Given this scenario, several studies have aimed at minimizing CO₂ emissions for several civil construction structures, such as Arpini et al. [9], Santoro and Kripka [10], and Tormen et al. [11]. However, research analyzing CO₂ emissions in prestressed composite steel-concrete beams are yet to be found.

Research has employed several methodologies to measure the environmental impact of buildings, among them, the life cycle assessment (LCA), a method that studies environmental inputs and outputs related to a product or their service lifecycle — i.e., since its production until the end of its service life (Khasreen, Banfill and Menzies [12]). CO₂ emission constitutes a common parameter to evaluate this impact on the structural optimization of various structures, as per Payá-Zaforteza et al. [13], García-Segura and Yépes [14], and Santoro and Kripka [10].

Among the existing optimization algorithms, the genetic algorithm (GA) proposed by Holland [15] and the particle swarm algorithm (PSO), originally proposed by Kennedy and Eberhart [16], stand out for their scope and wide use. In recent years, several structural optimization studies with GA and PSO have been developed, such as Netto, Calenzani, and Alves [17], which assessed prestressed steel beams; Breda, Pietralonga, and Alves [18], which evaluated composite beams with flat web profiles; Erdal, Doan, and Saka [19], which analyzed composite cellular steel beams; Senouci and Al-Ansari [20] and Govindaraj and Ramasamy [21], which aimed at optimizing a large range of structures; and Arpini and Alves [22] and Poitras, Lefrançois and Cormier [23], which appraised composite floor systems.

Steel structure specifications and design standards usually include composite steel-concrete beams. In turn, publications and studies on reinforced concrete structures address prestressing. Thus, the literature lacks studies directed to prestressed composite steel-concrete systems, as is the case of composite beams prestressed with straight tendons. Furthermore, optimization studies applicable to this type of structure are also scarce. Therefore, this study aims to propose a solution to the problem of optimizing the CO₂ emissions during the manufacturing of composite steel-concrete beams with doubly symmetrical steel profiles and external prestressing via straight tendons. We solved the optimization problem via the AG and PSO algorithms to evaluate their effectiveness in finding the solution for this problem.

2. Optimization problem formulation

To formulate the optimization problem, the design variables in longitudinal (Figure 1) and cross sections (Figure 2) were considered.

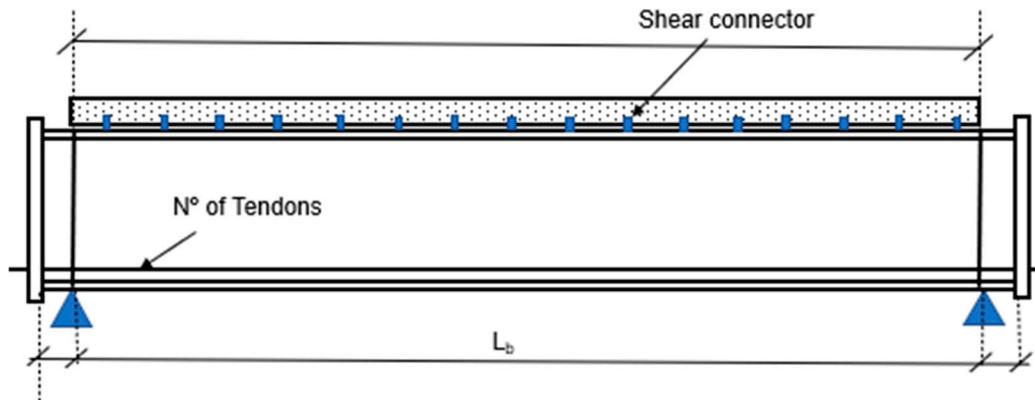


Figure 1. – Longitudinal section - design variables.

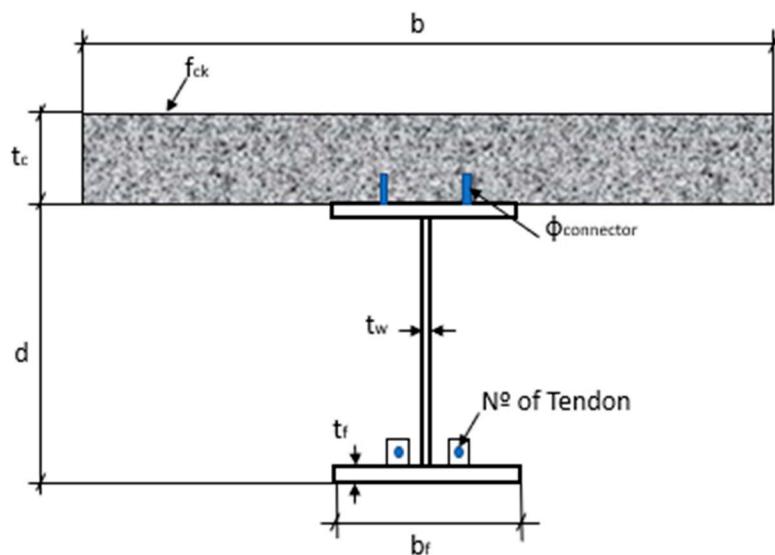


Figure 2. – Cross section - design variables.

A steel profile with its respective dimensions was directly selected from the laminated profile in the manufacturer's table (Gerdau [24]). In the case of welded profiles, each variable, i.e., profile height (d), flange width (b_f), flange thickness (t_f), and web thickness (t_w) are chosen within a practical range. Slab concrete height (t_c) was limited between 10 and 30 cm and the compressive strength of the concrete used in the slab (f_{ck}) ranges from 20 to 50 MPa, in 5 MPa steps. The number of tendons is selected by area according to the manufacturer's catalog (Protende [25]). In total, two diameter options, 19 and 22 mm, can be chosen for stud bolt connectors.

2.1. Objective Function

Our objective function – Equation (1) – seeks to minimize CO₂ emissions in the manufacturing process of prestressed steel-concrete composite beams.

$$\text{Min } CO_2 = CO_{2,s}V_s\rho_s + CO_{2,TR}V_{TR}\rho_s + CO_{2,CS}V_{CS} + L_W CO_{2,W} \quad (1)$$

The parts of Equation (1) represent the CO₂ emissions of each beam component. The first part refers to the steel profile, in which CO₂ represents the emission of CO₂ in kgCO₂ per kilogram of steel profile; V_s , the volume of the steel profile given by the product of its area A_s by the length of the beam L ; and ρ_s , the specific mass of steel. The second part represents the emission of CO₂ from the prestressing reinforcement tendons, in which CO_{2,TR} refers to the emission of CO₂ per kilogram of tendon and V_{TR} , the volume of the tendons given by the product of its area A_{TR} by the length of the bar L . The contribution of the composite slab concrete is considered by the third installment, in

which $CO_{2,CS}$ refers to the CO_2 emission of the concrete slab given in $kgCO_2$ per volume unit and V_{CS} , to the volume of concrete, in m^3 , contained within the slab width.

Furthermore, Equation (1) describes the last portion referring to the emission of CO_2 due to weld composition in welded profiles, calculated as the product of $L_w CO_{2,W}$, in which L_w represents the weld length and $CO_{2,W}$, the emission of CO_2 in $kgCO_2$ due to welding the composite steel-concrete beam. To determine the potential contribution to global warming, in $kgCO_2$ (Equation 2), a 3.3 $kgCO_2$ -Equiv./m value was adopted, adjusted by the ratio between the actual cross-section of the weld chord (A_{wl}) and the reference cross-sectional area of the weld chord for a 20-mm plate, i.e., 158 mm^2 (Sproesser et al. [26]). Figure 3 describes the variables considered to analysis weld emissions.

$$W_{CO_2} = 3.3 \times \frac{A_{wl}}{158} \quad (2)$$

in which:

$$A_{wl} = b t_w + (t_w - c)^2 \tan(\alpha/2) + [2(t_w - c) \tan(\alpha/2) + b](e/2) \quad (3)$$

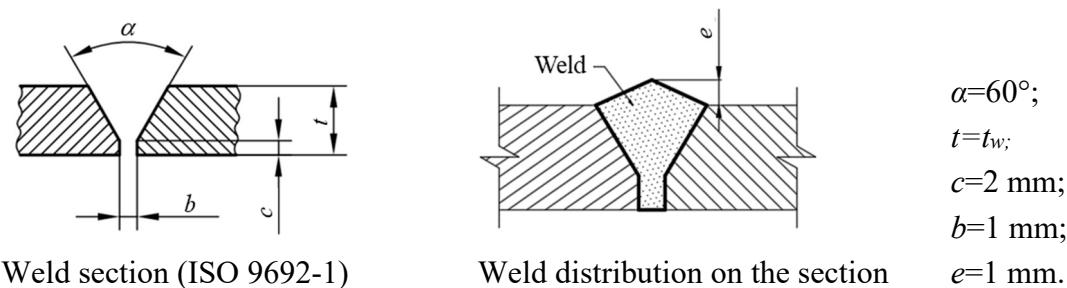


Figure 3. – Weld cross section.

The CO_2 emissions for each material considered in Equation 1 are shown in Table 1.

Table 1. – CO_2 Emissions of Materials.

Material	Unit	Emission	Source
Concrete 20 MPa		140.05	
Concrete 25 MPa		149.26	
Concrete 30 MPa		157.65	
Concrete 35 MPa	$kgCO_2/m^3$	171.74	Santoro & Kripka [10]
Concrete 40 MPa		182.14	
Concrete 45 MPa		194.70	
Concrete 50 MPa		225.78	
Steel Profile	$kgCO_2/kg$	1.116	World
Tendons		1.920	Steel Association [27]

2.1. Constraints

Constraints are used to assess the safety and performance of structures in the different stages of its useful life: (1) analysis of the steel section during pretension; (2) analysis of the steel section during concrete curing; (3) identification of the ultimate limit states of the composite section during its service phase; and (4) verification of the deflection limit state of a composite section during its service phase, considering their long-term effects. The criteria of the Brazilian standards for steel (NBR 8800:2008 [28]) and concrete (NBR 6118:2014 [29]) were used to establish the constraints in Table 2.

Table 2. Optimization Problem Constraints.

$C(1) = \frac{M_{Sd}^+(Step\ 1)}{M_{Rd}^+(Step\ 1)} - 1 \leq 0$ (t=0)	(4)	$C(9) = \frac{M_{Sd}^-(Step\ 3)}{M_{Rd}^-(Step\ 3)} - 1 \leq 0$ (t=∞)	(15)
$C(2) = \frac{M_{Sd}^-(Step\ 1)}{M_{Rd}^-(Step\ 1)} - 1 \leq 0$ (t=0)	(5)	$C(10) = \frac{V_{Sd}(Step\ 3)}{V_{Rd}(Step\ 3)} - 1 \leq 0$ (t=∞)	(16)
$C(3) = \frac{V_{Sd}(Step\ 1)}{V_{Rd}(Step\ 1)} - 1 \leq 0$ (t=0)	(6)	$C(11) = \left(\frac{N_{Sd}}{N_{Rd}} + \frac{8}{9} \right) \left(\frac{M_{Sd}^+(Step\ 3)}{M_{Rd}^+(Step\ 3)} \right) - 1 \leq 0$ (t=∞)	(17)
$C(4) = \left(\frac{N_{Sd}}{N_{Rd}} + \frac{8}{9} \right) \left(\frac{M_{Sd}^+(Step\ 1)}{M_{Rd}^+(Step\ 1)} \right) - 1 \leq 0$ (t=0)	(7)	$C(11) = \left(\frac{N_{Sd}}{N_{Rd}} + \frac{8}{9} \right) \left(\frac{M_{Sd}^-(Step\ 3)}{M_{Rd}^-(Step\ 3)} \right) - 1 \leq 0$ (t=∞)	(18)
$C(4) = \left(\frac{N_{Sd}}{N_{Rd}} + \frac{8}{9} \right) \left(\frac{M_{Sd}^-(Step\ 1)}{M_{Rd}^-(Step\ 1)} \right) - 1 \leq 0$ (t=0)	(8)	$C(11) = \left(\frac{N_{Sd}}{2N_{Rd}} \right) + \left(\frac{M_{Sd}^+(Step\ 3)}{M_{Rd}^+(Step\ 3)} \right) - 1 \leq 0$ (t=∞)	(19)
$C(4) = \left(\frac{N_{Sd}}{2N_{Rd}} \right) + \left(\frac{M_{Sd}^+(Step\ 1)}{M_{Rd}^+(Step\ 1)} \right) - 1 \leq 0$ (t=0)	(9)	$C(11) = \left(\frac{N_{Sd}}{2N_{Rd}} \right) + \left(\frac{M_{Sd}^-(Step\ 3)}{M_{Rd}^-(Step\ 3)} \right) - 1 \leq 0$ (t=∞)	(20)
$C(4) = \left(\frac{N_{Sd}}{2N_{Rd}} \right) + \left(\frac{M_{Sd}^-(Step\ 1)}{M_{Rd}^-(Step\ 1)} \right) - 1 \leq 0$ (t=0)	(10)	$C(12) = \frac{\delta_{total}}{\delta_{max}} - 1 \leq 0$	(21)
$C(5) = \frac{M_{Sd}^+(Step\ 2)}{M_{Rd}^+(Step\ 2)} - 1 \leq 0$ (t=0)	(11)	$C(13) = \frac{\frac{b_f}{2t_f}}{0.38 \sqrt{\frac{E}{f_y}}} - 1 \leq 0$	(22)
$C(6) = \frac{M_{Sd}^-(Step\ 2)}{M_{Rd}^-(Step\ 2)} - 1 \leq 0$ (t=0)	(12)	$C(14) = \frac{\frac{t_w}{\hbar}}{3.76 \sqrt{\frac{E}{f_y}}} - 1 \leq 0$	(23)
$C(7) = \frac{V_{Sd}(Step\ 2)}{V_{Rd}(Step\ 2)} - 1 \leq 0$ (t=0)	(13)	$C(15) = \frac{\sigma_t}{f_y} - 1 \leq 0$	(24)
$C(8) = \frac{M_{Sd}^+(Step\ 3)}{M_{Rd}^+(Step\ 3)} - 1 \leq 0$ (t=∞)	(14)		

Constraints C(1), C(2), C(3), and C(4) are used to assess positive bending moment, negative bending moment, shear force, and combined bending, respectively, in step 1. Constraints C(5), C(6), and C(7) are related to the evaluation of the positive bending moment, negative bending moment, and shear, respectively, in step 2. Constraints C(8), C(9), C(10), and C(11) are related to the verification of the positive bending moment, negative bending moment, shear force, and combined bending, respectively, in step 3. Constraint C(12) is related to the verification of the deflection in step 4. Constraints C(13) and C(14) impose the use of compact profiles, a requirement of NBR 8800:2008 [28] for beams subject to negative moments. Finally, constraint C(15) refers to the limitation of the tensile stress in the steel profile since the tension in the lower fiber of the steel profile lower flange must be lower than the yield strength of steel for the use of elastic analysis to determine deflections.

This study considers composite beams with external prestressing by pretension. therefore, to calculate the required structure, in step 1 of pretension, the considered loads refer to the weight of the beam itself and its construction loads and the resistant section, a section of the steel profile. In

step 2, after tendon pretension and slab execution, the resistant cross-section includes that of the steel profile and its loads refer the weight of the beam and the slab in addition to construction loads. In step 3, after the concrete is cured, the resistant cross-section includes the composite section and its loads refer to the weight of the composite beam and of the construction and utilization loads. Finally, in step 4, long-term effects are added to estimate deflection.

Our optimization problem solution was obtained via the Matlab [30] native genetic algorithm and PSO implemented within Matlab [30] with the adaptive penalties method (APM) proposed by Barbosa and Lemonge [31] to analyze the constraints of the problem. A population of 100 individuals was considered for the PSO, along with 75 iteration steps and a tolerance of 10^{-6} as a stopping criterion and solution convergence. The initial GA population contained 120 individuals, a 0.05 and 0.8 rate of elite individuals and crossing of intermediate types, respectively, and a random mutation rate.

3. Numerical Results

Numerical analysis was carried out in three stages. The first one aimed to evaluate the proposed design formulation by relating it to the experimental results in the literature and compare the deviations in our formulation to the real behavior of a structure regarding its resistance and rigidity. For this, the experiment in Ayyub, Sohn, and Saadatmanesh [5], which tested a full-scale pre-stressed composite beam, was selected and numerically implemented. The second stage aimed to analyze our optimization technique. As in Netto, Calenzani, and Alves [17], prestressed steel beams were used as reference to compare optimizations by analyzing their CO₂ emissions. Although the selected example is not a prestressed composite beam, we managed to validate the selected optimization technique.

Finally, in the third stage, a parametric analysis was developed to evaluate the impacts of using external prestressing on prestressed composite beams for spans of varying lengths and fixed loading. The span ranged from 5 to 40 m in 2.5-m steps. For each span, the optimized solution is shown with its CO₂ emission percentage for each component and material of the evaluated composite beam.

3.1. Example 1 – The Composite Stressed Beam in Ayyub, Sohn, and Saadatmanesh [5]

The example we chose to validate our design formulation refers to a prestressed composite beam with straight tendons, which was tested by Ayyub, Sohn, and Saadatmanesh [5] as shown in Figure 4.

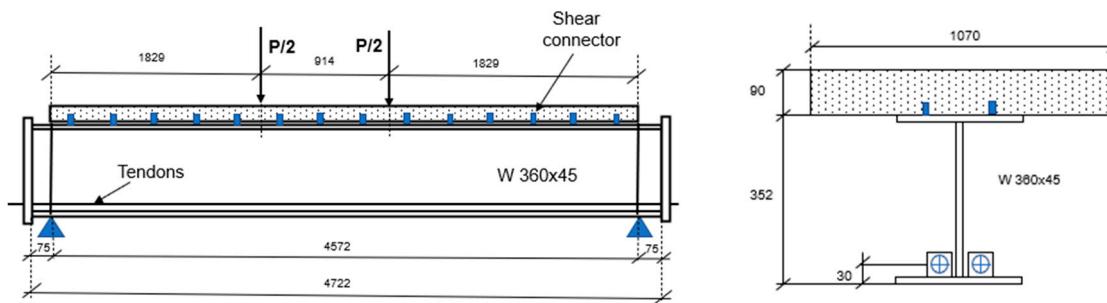


Figure 4. – Composite Prestressed Beam in Ayyub, Sohn, and Saadatmanesh [5] (Dimensions in mm).

For this test, seven low-relaxation steel wire strands with a 15 mm diameter and yield strength (f_{pyk}) and ultimate tensile strength (f_{ptk}) equal to 1620 and 2017 MPa, respectively, were considered. The beam is formed by a W 360x45 steel profile with a yield strength equal to 411 MPa, a 9-cm thick solid concrete slab, and concrete with an average compressive strength equal to 40 MPa with a standard deviation of 0.63 MPa. Using ABNT NBR 12655:2015 [32], the characteristic compressive strength of concrete equal to 36.7 MPa is obtained. The modulus of elasticity of steel equals 200 GPa and that of concrete, 30.25 MPa.

As shown by Ayyub, Sohn, and Saadatmanesh [5], the collapse load for the beam equaled 780kN, corresponding to a bending moment of 713.31kNm.

Using the proposed design methodology, the resistant moment determined for the beam totals 679.19kNm, 5.02% lower than the experimentally obtained one, suggesting that the proposed methodology favors safety. Figure 5 shows the load versus displacement graph with test curves and the proposed methodology.

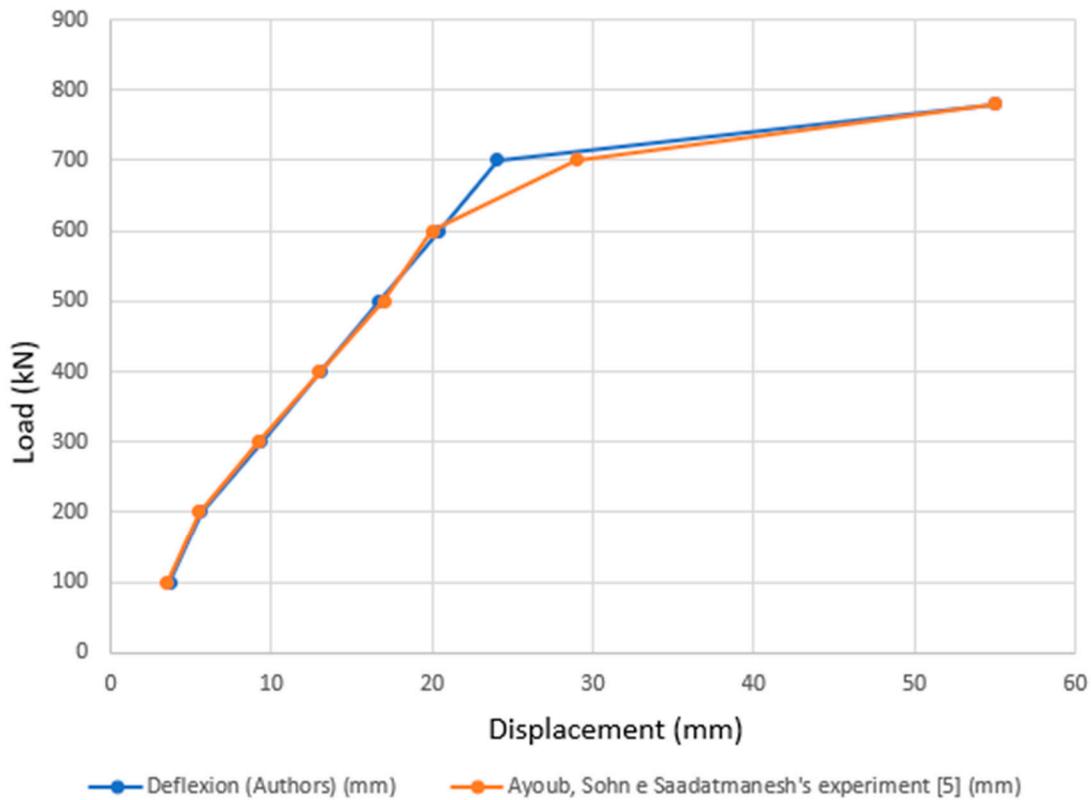


Figure 5. – Analysis Load x Displacement.

Regarding stiffness, since the dimensioning methodology considers elastic linear analysis to estimate maximum displacements, it was observed, as expected, that experimental and analytical deflection values in the elastic phase agree with each other, corroborating the validation of our proposed methodology. The maximum deflection obtained by Ayyub, Sohn, and Saadatmanesh [5] was 5.29 cm whereas, with our proposed formulation, we obtained a maximum deflection equal to 5.52 cm, resulting in a difference of 4.2% between studies.

Figure 6 offers an analysis of the collapse modes that govern designs according to the proposed methodology: resistant moments and shears in relation to the loads and the stresses generated in the beam for different load stages up to the collapse of the load.

Figure 6 describes the bending due to the positive moment in the middle of the span, which is the mode that governs the problem for a 780-kN failure load, followed by the shear in the beam.



Figure 6. – Analysis of collapse modes.

3.2. Example 2 – Optimization Comparative Analysis

For a comparative analysis of the optimization process, the prestressed steel beam (Figure 7) optimized by Netto, Calenzani, and Alves [17] was analyzed as a prestressed steel-concrete composite beam; In this study, we re-optimized the steel beam. The input data considered were 150-kN 3-point loads applied at 11, 12.5, and 14 meters from the left support; with a 3-kN/m overload; a 12.86-kN/ permanent load m; a 15-kN/m serviceability overload; a 25-m L ; 15.2-mm tendons set 100 mm below the inferior flange bottom; a 345-MPa f_y ; and a 205000-MPa E . The analysis in this study considered that the load corresponding to the weight of the slab would be included in the 12.86-kN/m value of the permanent load. Moreover, both a shored and unbolted structure were analyzed; in which the abbreviations of the models were identified as AG and PSO, i.e., the genetic algorithm and particle swarm algorithm, respectively; and ESC and NESC, referring to shored and unshored structures, respectively.

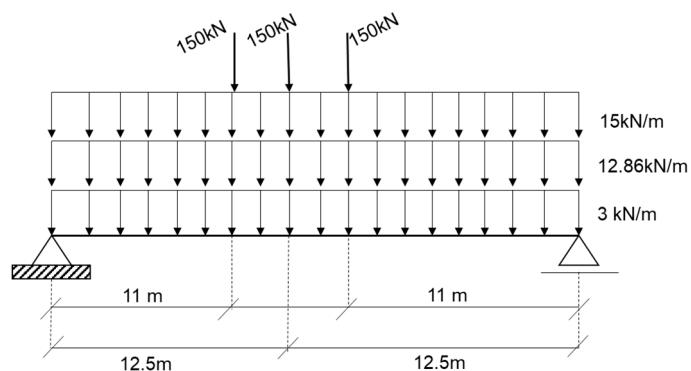


Figure 7. – Optimized Prestressed Steel Beam – Netto, Calenzani, and Alves [17].

To solve the optimization problem, Netto, Calenzani, and Alves [17] used the native GA of Matlab and obtained results for doubly symmetrical and monosymmetric welded steel profiles.

The best result for the doubly symmetric profile consisted of a profile with a 1580-mm height, 410-mm upper and lower flanges, whose thickness and web equaled 22.4mm and 12.5mm, respectively, and nine 15-mm diameter tendons. Table 3 shows a comparative analysis of the optimization result of the prestressed composite beam in relation to the result by Netto, Calenzani, and Alves [17] for a pure steel beam. Table 4 shows the obtained emission, displacement, compression, and traction stresses values.

Table 3. – Optimum design of prestressed steel beam.

Model	d (mm)	b _f (mm)	t _w (mm)	t _f (mm)	Slab height (mm)	Φ _{studbolt} (mm)	f _{ck} (MPa)	No. of tendons
Netto, Calenzani, and Alves [17]	1580	410	33.5	22.4	-	-	-	9
PSO - ESC	1156	240	17	18	110	22	35	9
GA - ESC	1231	222	17	14	110	22	35	8
PSO - NES	1182	253	17	15	110	22	35	9
GA - NES	1318	237	17	13	130	19	30	5

Table 4. – Optimization Results.

Model	δ (mm)	s _c (MPa)	s _t (MPa)	Emissions				
				Profile (kgCO ₂)	Tendons (kgCO ₂)	Weld (kgCO ₂)	Concrete (kgCO ₂)	Total (kgCO ₂)
Netto, Calenzani, and Alves [17]	68.26	-282.45	199.72	15834.54	535.68	1343.49	-	17713.72
PSO - ESC	57.06	-127.02	101.30	6062.34	535.68	325.96	944.57	7868.54
GA - ESC	56.87	-122.53	96.34	5840.47	476.16	325.96	944.57	7587.16
PSO - NES	39.17	-125.73	99.79	5951.51	535.68	325.96	944.57	7757.72
GA - NES	44.46	-107.71	83.94	6160.02	297.60	325.96	1024.73	7808.30

The use of a prestressed composite beam reduced 63.1% of CO₂ emissions from the steel profile. It also reduced the sag by 16.7%, the maximum compressive stress by 56.6%, and tensile stress by 51.8%, increasing the safety of the structure.

Figure 8 shows the total emission normalized in relation to the result by Netto, Calenzani, and Alves [17]. The genetic algorithm with an unshored structure was the model that generated the best solution, reducing total emissions by 57.2%.

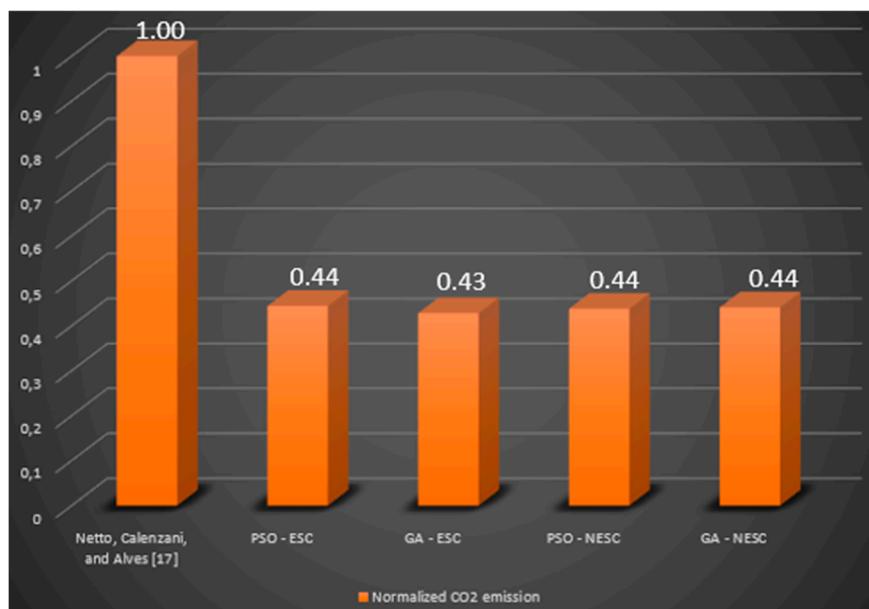
**Figure 8.** Normalized total CO₂ emission.

Figure 9 shows the constraints used to analyze the models, in which the governing constraints were the positive moment constraints in all three phases and deflection and combined bending in step 3.

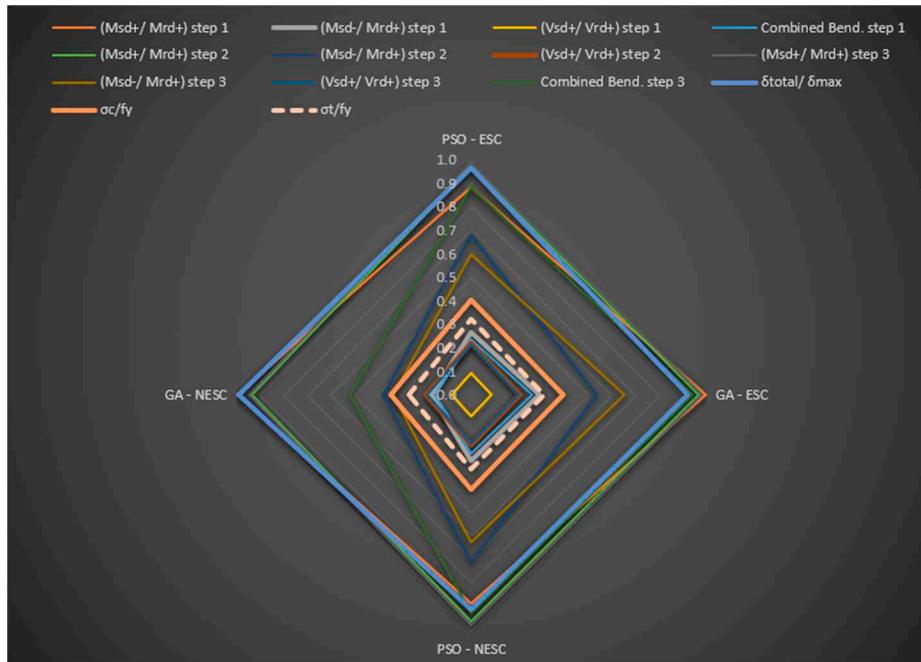


Figure 9. – Constraints Analysis.

3.3. Example 3 – Parametric Analysis

With the aim of analyzing the impacts of CO₂ emissions on prestressed composite beams and evaluate which composition and factors most influence emissions, a parametric analysis of the prestressed composite beam was performed, varying the span from 5 to 40 m in 2.5-m steps. Our analysis considered several factors, including a 3-m distance between beams, a 345-Mpa steel yield strength, and, as optimization variables, the section of the steel profile, its number of tendons, the thickness of the concrete slab, and the compressive strength of the used concrete. For loading, in addition to the weight of the beam, 2kN/m² were considered for the dead load; 5kN/m², for the live load; and 1kN/m², for the construction load. Optimization problem solutions were evaluated via both GA and PSO. Figure 10 shows the ratio of the solution obtained via GA and PSO.

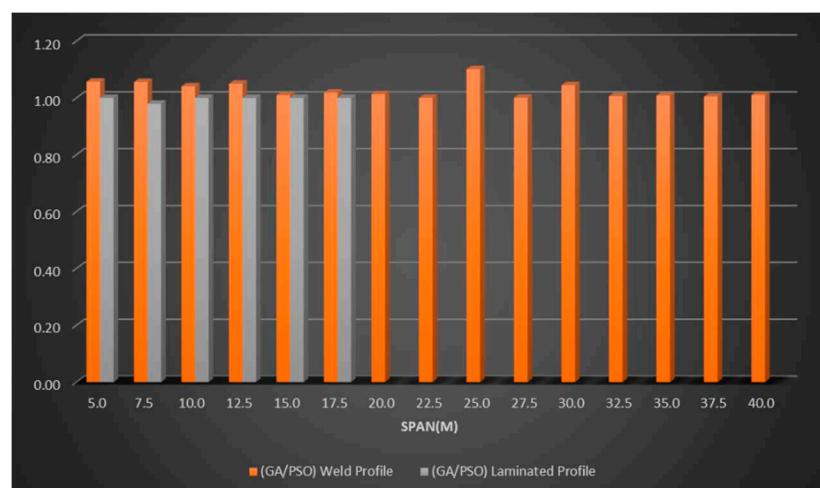


Figure 10. – Relation between GA/PSO Total Emissions.

Figure 10 shows that PSO provided better or equal solutions to GA for both laminated profiles and welded profiles. Regarding welded profiles, the biggest difference totaled 11% for the 5-m span, whereas for laminated profiles, the biggest difference was around 2%. For the 20-m span, GA was unable to find a solution to the problem when adopting the laminated profile. Considering the GA

limitations and that the best solutions were obtained via PSO, our analyses will refer to the solutions via PSO.

Regarding the PSO solutions for both laminated and welded profiles, Figure 11 shows the relation between the best solutions for total emissions, which we limited to a maximum span of 25 m.

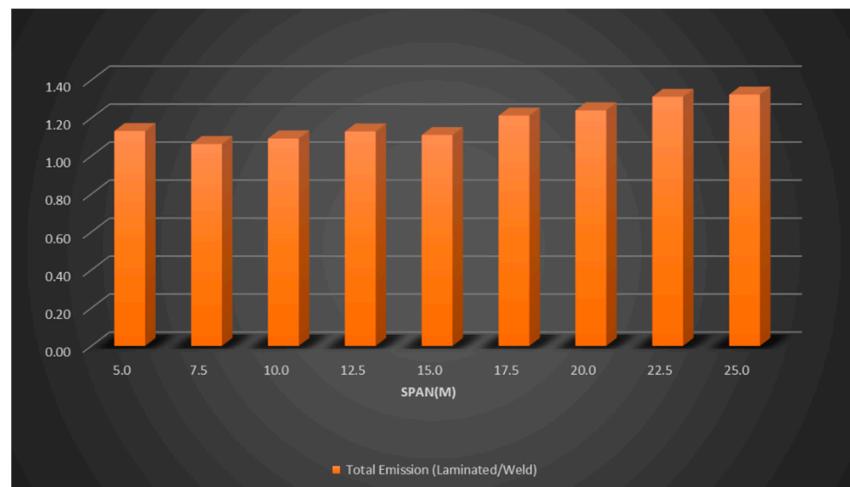


Figure 11. –Laminated/Welded Profile PSO Ratios.

Figure 11 shows that when comparing the solutions obtained for laminated and welded profiles, the best solutions were for the welded profile regarding CO₂ emissions, even considering the emission of the weld in the profile manufacturing process. Tables 5 and 6 show the dimensions obtained for both laminated and welded profiles after optimization, respectively.

Table 5. – Final solution for laminated profiles.

Span(m)	b _f (mm)	d(mm)	t _w (mm)	t _f (mm)	t _c (cm)	f stud(mm)	f _{ck} (MPa)	No. of Tendons
5.0	102	153	5.8	7.1	110	19	20	0
7.5	101	305	5.6	6.7	110	19	20	0
10.0	165	310	5.8	9.7	110	22	20	0
12.5	153	455	8	13.3	110	19	20	0
15.0	166	529	9.7	13.6	110	19	20	0
17.5	210	537	10.9	17.4	110	19	25	0
20.0	228	608	11.2	17.3	110	22	35	4
22.5	324	611	12.7	19	110	22	20	6
25.0	325	616	14	21.6	110	19	35	8

Table 6. – Final solution for welded profile.

Span(m)	b _f (mm)	d(mm)	t _w (mm)	t _f (mm)	t _c (cm)	f stud(mm)	f _{ck} (MPa)	No. of Tendons
5.0	90	129	4	5	110	19	20	0
7.5	109	309	4	6	110	19	20	0
10.0	129	381	4	10	110	22	20	0
12.5	151	560	6	9	110	22	20	0
15.0	153	655	7	11	110	22	20	0
17.5	153	749	8	13	110	19	20	0
20.0	200	755	8	16	110	19	25	0
22.5	167	856	9	21	110	19	25	0
25.0	131	888	9	37	110	19	30	0
27.5	325	854	9	20	110	22	40	0

30.0	319	900	15	18	110	19	40	7
32.5	317	900	15	28	110	22	30	9
35.0	281	900	22	28	110	19	40	12
37.5	298	900	21	40	110	22	35	14
40.0	404	900	18	39	110	22	45	16

Table 5 shows that laminated profiles faced limitations in their dimensions and, thus, tendons were required to solve the problem for spans of 20 m or more. On the other hand, for welded profiles, tendons were only necessary for spans exceeding 30 m. It can also be observed that for all beams, the solutions obtained were for an 11-cm concrete slab. The compressive strength of concrete starts to increase from the 17.5-m span for laminated profiles and the 20-m one for welded ones. Although the highest strength concrete has the higher their CO₂ emission, this value is compensated in the composition of the final resistance capacity of the prestressed composite steel-concrete beam. Figure 12 shows our analysis of the span/height ratio (L/h) of laminated and welded profiles for the obtained solutions.

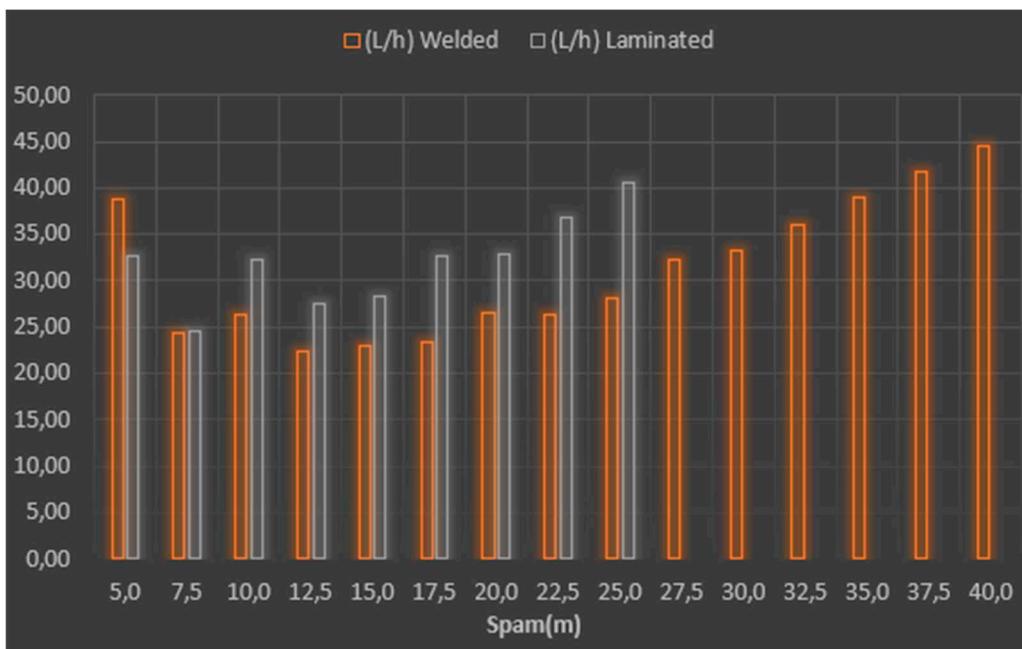


Figure 12. – Ration L/h.

Figure 12 shows that the L/h ratio for laminated profiles was higher than that for welded ones in the same analyzed spans. Laminated profiles averaged a 32 ratio, whereas welded ones, 31. These ratios indicate that a ratio between 30 and 35 L/h can be adopted for prestressed steel-concrete beams for pre-dimensioning purposes.

Figures 13 and 14 show the composition of the final emission of beams optimized with both the laminated and welded profiles.

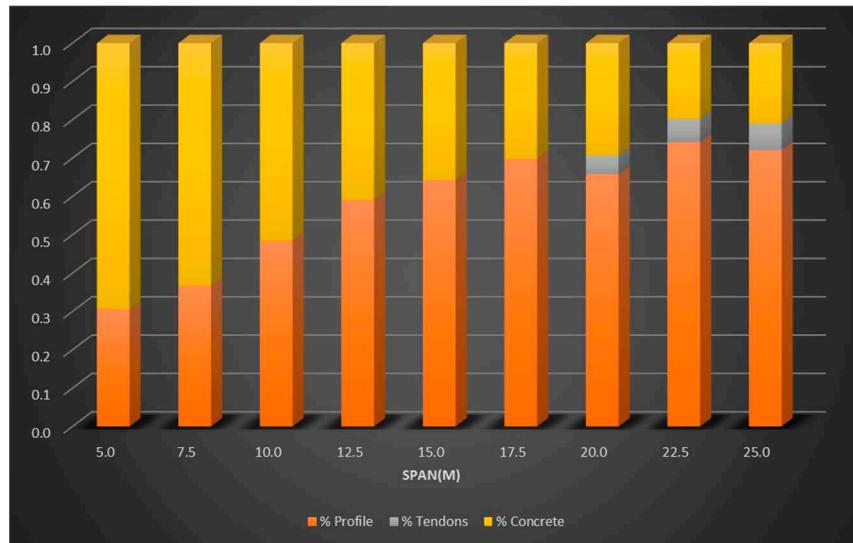


Figure 13. – Composition of the total emission from laminated profiles.

For laminated profiles, as shown in Figure 13, the steel profile is responsible for around 50% of the emission for 5-, 7.5-, and 10-m spans. For the largest spans, the emission related to the steel profile represents a value above 60%. On the other hand, for a 20-m span, emissions related to concrete revolved around 29%, whereas for tendons, around 5%. For the 22.5- and 25-m spans, emissions related to prestressing tendons and concrete were around 10% and 20%, respectively.

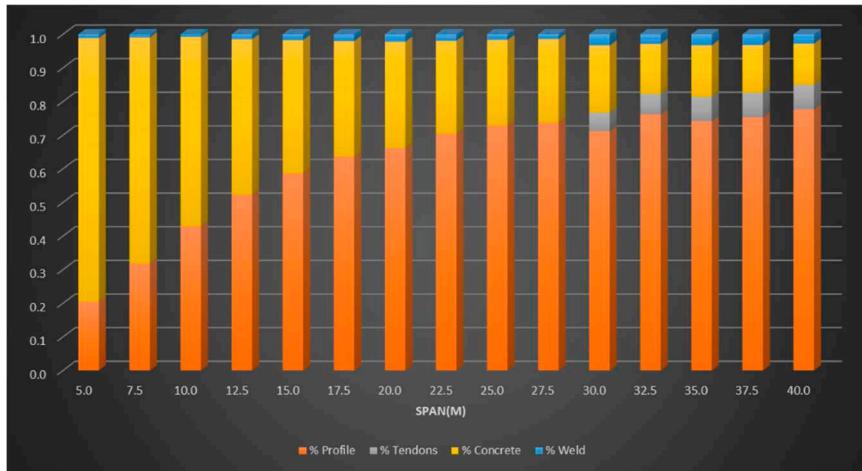


Figure 14. – Composition of total emission from welded profiles.

Welded profiles showed an emission distribution ratio similar to that for laminated profiles. Weld emission for these problems ranged from 1% for the 10-m span to a maximum value of 3.3% for the 30-, 35-, and 37.5-m spans. Note that weld emissions are proportional to the thickness of the web adopted for the welded profile, as shown in Figure 15.

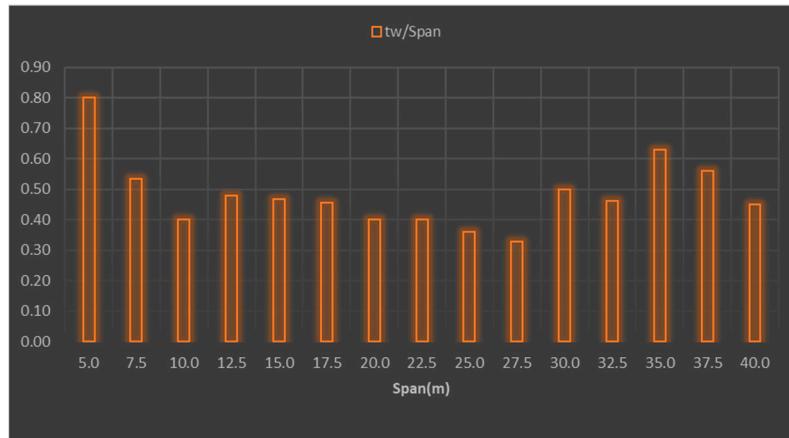


Figure 15. – Ratio t_w/span .

Emissions from tendons ranged from 5.5% for the 30-m span to 7.4% for the 37.5-m one, generating a low impact on the total emission of the beams.

Figures 16 and 17 show an analysis of the factors that stood out for rolled and welded profiles, respectively, regarding the modes that governed the optimization problem.

According to Figure 16, for spans ranging from 5 to 17.5 m, laminated profiles, show no need for tendons, the constraints that governed the problem referred to the maximum tensile stress generated in the profile, followed by the positive moment in the act of construction (assembly of the beam), in which only the profile resists the efforts of the structure due to the weight of the slab and construction loads. For cases that needed prestressing tendons, the constraints that governed the problem included the combined flexion at time $t=\infty$ and the positive moment in the act of pretension $t=0$.

Similar to what occurred for laminated profiles, for spans ranging from 5 to 27.5 m, which showed no need for prestressing tendons, the constraints that governed the problem included the maximum tensile stress generated in the profile and the positive moment in the act of construction (assembly of the beam). For cases that needed prestressing tendons, the constraints that governed the problem referred to the combined flexion at time $t=\infty$ and the positive moment in the act of pretension $t=0$. For both cases, note that the service limit state due to excessive sag was the constraint that least impacted the problem. This solution points to the importance of prestressing to control excessive deformations in structures.

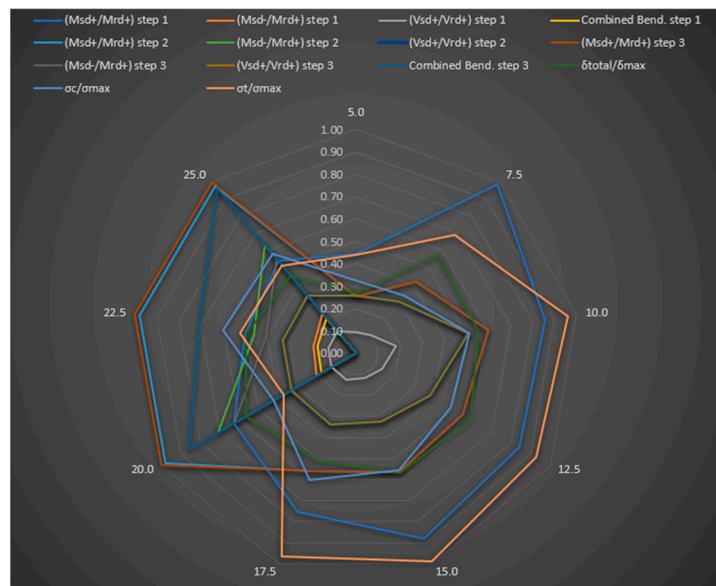


Figure 16. – Constraints Analysis of Laminated Profiles.

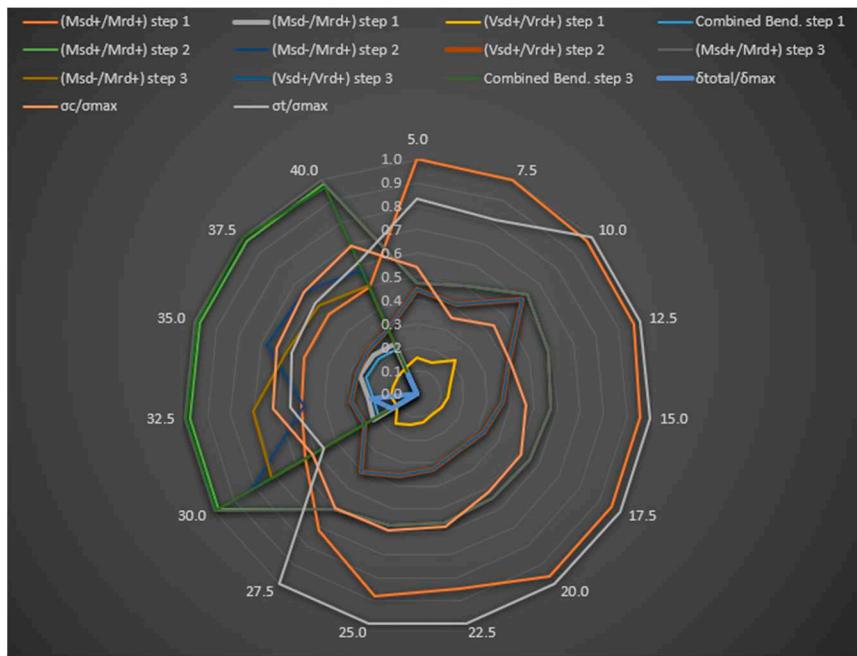


Figure 17. – Constraints Analysis of Weld Profiles.

4. Conclusion

This study aimed to propose an optimization of CO₂ emissions from prestressed composite beams using doubly symmetrical laminated and welded profiles with external prestressing and straight tendons. For this, three examples were analyzed, the first of which to validate our algorithms, comparing our results to experimental ones. The second example optimized a prestressed composite beam compared it to the optimization of a prestressed metallic beam. The third example conducted a parametric analysis of the factors influencing the solution for the CO₂ emission optimization problem.

Regarding the first validation example, results indicate that the methodology can reliably formulate the optimization problem considering the low difference in displacements and final moments in the structures when compared to experimental result.

Regarding the second example, in which a comparative analysis of the optimization was conducted following the proposed methodology with a prestressed steel beam, results were more than satisfactory. In this analysis, the best solution was found using GA and an unshored structure, obtaining a 63.1% reduction in CO₂ emissions of the steel profile and a 57.2% reduction in total CO₂ emissions. We also found a 16.7% reduction in its sag, 56.6% in its maximum compressive stress, and 51.8% in its tensile stress, increasing the safety of the structure. In this example the constraints that governed optimization referred to positive moments, bending, and combined bending in step 3.

With the conducted parametric analysis in the third example, we concluded that PSO generated better results than GA. GA found the best solutions for laminated spam profiles up to 17.5m while PSO found the best solutions for laminated profiles up to 25m. For welded profiles, solutions without prestressing tendons were used for spans up to 27.5 m.

Another observed point was that welded profiles generated the best results. Even with the use of welding in the manufacturing process, welded profiles generated lower emissions than laminated ones.

Regarding the final solution for the optimization problem, we observed that the thickness of the slab was the same for all examples. However, the compressive strength of the concrete increased from the span of 17.5 m for laminated profiles and 20 m for welded profiles, a positive contribution to the final solution as it decreased emissions. Thus, we found that the pre-dimensioning of a prestressed composite beam can adopt a *L/h* ratio between 30 and 35.

Steel profiles were the main responsible for emitting CO₂. For laminated profiles, whose total CO₂ emission value revolved around 50% for spans ranging from 5 to 10 m. For larger spans, this

emission reaches 60%. Emissions related to the welding process had very little influence on the final solution and welded profiles showed better solutions than laminated ones. Concrete showed 29% of the total CO₂ emission in beams with spans above 20 m, whereas the CO₂ emission of tendons revolved around 5%. For 22.5- and 25-m spans, the emissions related to prestressing tendons revolved around 10% and 20% respectively.

On the other hand, welded profiles showed similar emission values, differing in the increase in weld emissions, around 1% for beams with up to 10-m spans and reaching a maximum value of 3.3% for 30-, 35-, and 37.5-m spans. Emissions from prestressing tendons was around 5.5% for a 30-m span and 7.4% for a 37.5-m one. In the absence of the need for prestressing tendons, maximum traction generated in the profile and the positive moment in the act of construction were the modes governing the third example. For cases that needed prestressing tendons, the constraints that governed included flexion combined with t=∞ and positive moment during prestressing.

Therefore, we suggest that our formulation to optimize prestressed composite steel-concrete beams proved to be reliable due to the satisfactory results in our analyses.

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