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*Article*

# Development of a Multi-Motor Asynchronous Electric Drive with Changes in the Coordinated Rotation of the Supply Voltages of the Motors

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**Abstract:** In the proposed article, the issues of increasing the synchronizing ability of the system of coordinated rotation of asynchronous motors are considered. Based on the *T*-shaped equivalent circuit, electromechanical relationships were obtained with changes in the value of the total rotor resistance and the supply voltage of individual motors. An algorithm for calculating the torques, stator and rotor currents of the motors of the system has been compiled. Based on the calculations obtained, the mechanical characteristics of the system asynchronous motors are constructed for various values of total resistance, supply voltages and rotor positions. The obtained data and graphs confirm the adequacy of the theory obtained in an analytical way. Functional and structural diagrams in small scales have been compiled, which allow simulating transient operation modes of multi-motor asynchronous electric drives in the Matlab application package. Multi-motor asynchronous electric drives with adjustable supply voltages, as well as with preliminary synchronization and synchronous braking, have been developed. Compilation of a program for the stability of a nonlinear system of a multi-motor asynchronous electric drive (MAEDs) with a thyristor voltage converter (TVC) in Matlab. Also, the modes of soft start, load shedding and surge on the motor shaft are simulated, confirming the stability of the system.

**Keywords:** multi-motor asynchronous electric drive; coordinated rotation; thyristor voltage converters; synchronizing torques

## 1. Introduction

In a number of production mechanisms, machines and units of various industries, the synchronous rotation of several motors, interconnected mechanically, electrically or technologically, is required. Such mechanisms include carding machines, belt and chain conveyors, unified building vibration platforms, cold rolling mills, paper machines, etc. In most drives of technological processes, the drive motors are not kinematically rigidly connected to each other. Synchronization of rotation of asynchronous motors of these mechanisms is achieved through the use of a relay-contact or control system for motors connected electrically and according to the classical “electric shaft” scheme. Systems of the “energy shaft”, in turn, are divided into an electric operating shaft (EOS), an electric equalizing shaft (EES). Their distinctive features are discussed in detail in the monograph. Such systems have significant disadvantages: low synchronizing capacity, tendency to self-oscillations, as a result - a narrow stability region, large losses of electrical energy in common rotor circuits, etc. The modern development of elements of power electronics, converter and microprocessor technology

allows, on the basis of cheap, reliable asynchronous electric motors, to create a wide variety of control systems for multi-motor asynchronous electric drives and expand the possibilities of their synchronous rotation even with significant differences in load torques. Thus, the creation and widespread implementation of control systems for multi-motor asynchronous electric drives of synchronous, synchronous-in-phase rotation, which make it possible to improve the quality of output products and the productivity of technological processes, is an urgent task. The development and optimization of multi-motor asynchronous electric drives (MAEDs) represent a pivotal area in modern electromechanical engineering. These systems play a crucial role in various industrial applications where precise synchronization and efficient operation are paramount. This study focuses on advancing the understanding and capabilities of MAEDs through the development of a method for calculating mechanical characteristics and exploring their behavior under variable supply voltages. Asynchronous motors, with their robustness and adaptability, are widely employed in industrial settings due to their ability to handle diverse loads and operational conditions. However, achieving optimal synchronization among multiple motors, especially when subjected to fluctuations in supply voltages, remains a challenging yet essential objective. This article addresses this challenge by proposing a systematic approach to analyze and optimize the performance of MAEDs under varying electrical inputs. The methodology leverages a *T*-shaped equivalent circuit to derive essential parameters such as torque, stator, and rotor currents, while considering angular deviations and electrical phase shifts. Practical validation and simulation in Matlab provide insights into transient behaviors and stability under different operational scenarios, thereby offering a comprehensive understanding of the system's dynamic response. By examining the impact of supply voltage variations on mechanical characteristics and synchronization efficiency, this study aims to contribute valuable insights into enhancing the reliability, efficiency, and adaptability of MAEDs in industrial applications. The results and discussions presented herein underscore the importance of tailored control strategies and optimal voltage management for achieving seamless operation and maximizing energy efficiency in multi-motor asynchronous electric drives.

## 2. Materials and Methods

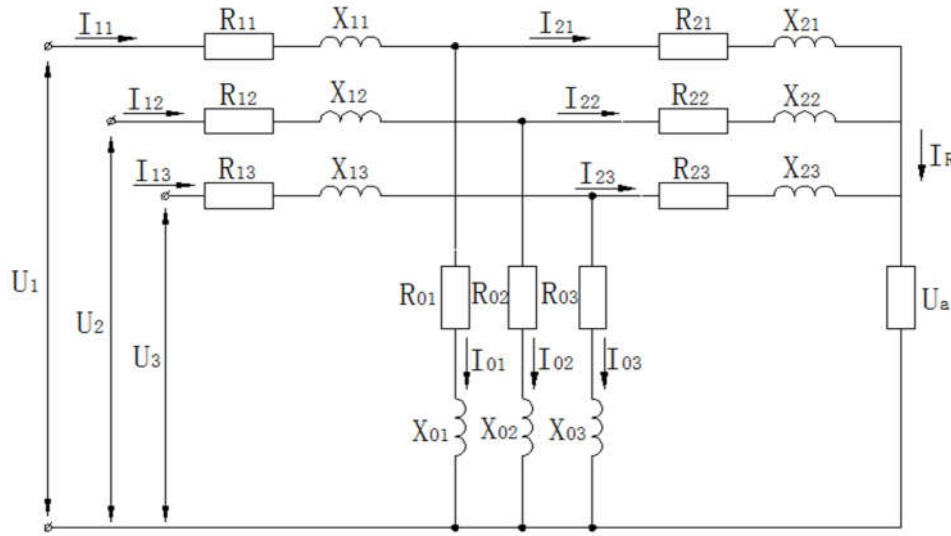
The main electromechanical ratios of the EOS three-engine system are found from the *T*-shaped equivalent circuit. The angular mismatches of the rotors of differently loaded motors are denoted by  $\varphi_1, \varphi_2, \varphi_3$  relative to some imaginary axis rotating in coordination with the motor rotors. According to the theory of the electric shaft, mechanical angles of rotation can be taken into account in electrical degrees relative to the applied voltages along the stator circuits, i.e., by multiplying the voltages by  $e^{j\varphi_1}, e^{j\varphi_2}, e^{j\varphi_3}$ . Phase shifts of all motor currents are taken into account by multiplying by the same multipliers. This approach is necessary to make the formulas more symmetrical. Further calculations are carried out according to the principle of the overlay method.

For an analytical study of multi-motor electric drives with electrical communication through rotary circuits, when the supply voltage of individual motors changes, we accept the following generally accepted assumptions in the electric drive:

- the parameters of the system engines are identical;
- the magnetic field along the circumference of the air gap of each engine is distributed evenly, only the main harmonic field is taken into account;
- losses in the steel of the stator and rotor are not taken into account, the magnetic circuits of the motors are unsaturated;
- voltage applied to the stator windings, symmetrical three-phase;
- superposition principle is used to determine currents and torques;
- the resistance of the connecting cables is not taken into account;
- in the study of stability, deviations "in the small" are taken into account.

To determine the currents and moments of the MAEDs synchronous rotation (SR) system with electrical communication through common rotor circuits, which includes three asynchronous motors, we use its *T*-shaped equivalent circuit, which is shown in Figure 1, where respectively marked (see Figure 1):

$U_1, U_2, U_3$  – is the mains voltages for each motor;  
 $I_{11}, I_{12}, I_{13}, I_{21}, I_{22}, I_{23}$  – is the stator and rotor currents of the machines, respectively;  
 $r_{11}, r_{12}, r_{13}$  and  $x_{11}, x_{12}, x_{13}$  – is the active and inductive resistances of the stator windings of the corresponding motors of the system with electrical connection through rotor circuits;  
 $r_{21}, r_{22}, r_{23}$  and  $x_{21}, x_{22}, x_{23}$  – is the active and inductive resistances of the rotor windings;  
 $x_{01}, x_{02}, x_{03}$  – is the inductive resistances of the magnetization circuits;  
 $R_a$  – is the additional resistance in the rotor circuit;  
 $S$  – is the slip;  
 $\varphi_1, \varphi_2, \varphi_3$  – is the angular shifts of the rotors in electrical degrees relative to the accepted reference axis.



**Figure 1.** T-shaped equivalent circuit of three asynchronous motors with electrical connection through rotor circuits.

Denoting the complex resistances of the stators and rotors during sliding  $S$  through  $Z_1, Z_2$ , taking into account the identity of the motor parameters and reduction of rotor resistances, we obtain:

$$Z_1 = r_1 + j(x_0 + x_1) \quad (1)$$

$$Z_2 = \frac{r'_2}{S} + j(x_0 + x'_2) \quad (2)$$

where  $\frac{r'_2}{S}, x'_2$  – is the active and inductive resistance of the rotors, respectively, reduced to the stator.

Then the voltage equations for the stator and rotor circuits are:

$$\dot{U} = I_{1n}Z_1 - I_{2n}jX_0 \quad (3)$$

$$(I_{1n}jX_0 - I_{2n}Z_2)e^{j\varphi_n} = \frac{R'}{S} \sum_{L=1}^n I_{2n}e^{j\varphi_n} \quad (4)$$

In our case, the parameters of all three motors are strictly identical ( $P_{1n} = P_{2n} = P_{3n}, n_{1n} = n_{2n} = n_{3n}, I_{11n} = I_{12n} = I_{13n} = I_{21n} = I_{22n} = I_{23n}$ ) and the voltage equation systems will take the form:

$$U = I_{11}Z_1 - I_{21}jX_0$$

$$U = I_{12}Z_2 - I_{22}jX_0 \quad (5)$$

$$U = I_{13}Z_3 - I_{23}jX_0$$

$$(I_{11}jX_0 - I_{21}Z_2)e^{j\varphi_1} = \frac{R'}{S} (I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3})$$

$$(I_{12}jx_0 - I_{22}Z_2)e^{j\varphi_2} = \frac{R'}{S}(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \quad (6)$$

$$(I_{13}jx_0 - I_{23}Z_2)e^{j\varphi_3} = \frac{R'}{S}(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3})$$

Having determined the values of the stator currents from Eq. (5) substituting into the system of Eq. (6). After transformation we get:

$$\begin{aligned} Ujx_0e^{j\varphi_1} - (x_0^2 + Z_1Z_2)I_{21}e^{j\varphi_1} &= \frac{R'}{S}Z_1(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \\ Ujx_0e^{j\varphi_2} - (x_0^2 + Z_1Z_2)I_{22}e^{j\varphi_2} &= \frac{R'}{S}Z_1(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \quad (7) \\ Ujx_0e^{j\varphi_3} - (x_0^2 + Z_1Z_2)I_{23}e^{j\varphi_3} &= \frac{R'}{S}Z_1(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \end{aligned}$$

Summing up these equalities:

$$U(e^{j\varphi_1} + e^{j\varphi_2} + e^{j\varphi_3})jx_0 - (x_0^2 + Z_1Z_2)(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) = \frac{3R'}{S}Z_1(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \quad (8)$$

Determine the current in the common rotor circuit:

$$I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3} = \frac{Ujx_0(e^{j\varphi_1} + e^{j\varphi_2} + e^{j\varphi_3})}{\frac{3R'}{S}Z_1 + (x_0^2 + Z_1Z_2)} \quad (9)$$

Substituting the values of the total currents of the currents into the system of Eq. (7) we obtain:

$$\begin{aligned} Ujx_0e^{j\varphi_1} - (x_0^2 + Z_1Z_2)I_{21}e^{j\varphi_1} &= \frac{3R'}{S}Z_1 \frac{Ujx_0(e^{j\varphi_1} + e^{j\varphi_2} + e^{j\varphi_3})}{\frac{3R'}{S}Z_1 + (x_0^2 + Z_1Z_2)} \\ Ujx_0e^{j\varphi_2} - (x_0^2 + Z_1Z_2)I_{22}e^{j\varphi_2} &= \frac{3R'}{S}Z_1 \frac{Ujx_0(e^{j\varphi_1} + e^{j\varphi_2} + e^{j\varphi_3})}{\frac{3R'}{S}Z_1 + (x_0^2 + Z_1Z_2)} \quad (10) \\ Ujx_0e^{j\varphi_3} - (x_0^2 + Z_1Z_2)I_{23}e^{j\varphi_3} &= \frac{3R'}{S}Z_1 \frac{Ujx_0(e^{j\varphi_1} + e^{j\varphi_2} + e^{j\varphi_3})}{\frac{3R'}{S}Z_1 + (x_0^2 + Z_1Z_2)} \end{aligned}$$

From the 10th equation we find the rotor currents:

$$\begin{aligned} I_{21} &= \frac{jx_0 \left\{ x_0^2 + z_1 \left[ Z_2 + \frac{R'}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)} \right) \right] \right\}}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1Z_2)} \cdot U \\ I_{22} &= \frac{jx_0 \left\{ x_0^2 + z_1 \left[ Z_2 + \frac{R'}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_2)} \right) \right] \right\}}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1Z_2)} \cdot U \\ I_{23} &= \frac{jx_0 \left\{ x_0^2 + z_1 \left[ Z_2 + \frac{R'}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_3)} \right) \right] \right\}}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1Z_2)} \cdot U \end{aligned}$$

Stator currents are defined as:

$$\begin{aligned}
I_{21} &= \frac{U}{Z_1} + \frac{jx_0}{Z_1} I_{21} = \frac{U}{Z_1} + \frac{jx_0}{Z_1} \cdot \frac{jx_0 \left\{ x_0^2 + z_1 \left[ Z_2 + \frac{R'}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)} \right) \right] \right\}}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)} \cdot U = \\
&= \frac{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{R'}{S} \right) \right] (x_0^2 + Z_1 Z_2) - x_0^2 \left\{ x_0^2 + z_1 \left[ Z_2 + \frac{R'}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)} \right) \right] \right\}}{Z_1 \left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)} = \\
&= \frac{x_0^2 Z_1 Z_2 + Z_1^2 Z_2 \left( Z_2 + \frac{3R'}{S} \right) + \frac{x_0^2 R'}{S} \cdot Z_1 \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)}}{Z_1 \left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)} \cdot U = \\
&= U \cdot \frac{x_0^2 \left[ Z_2 + \frac{R'}{S} \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)} \right] + Z_1 Z_2 \left( Z_2 + \frac{3R'}{S} \right)}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)}
\end{aligned} \tag{11}$$

For the 2nd, 3rd engine are equal:

$$\begin{aligned}
I_{22} &= U \cdot \frac{x_0^2 \left[ Z_2 + \frac{R'}{S} \sum_{L=1}^3 e^{j(\varphi_L - \varphi_2)} \right] + Z_1 Z_2 \left( Z_2 + \frac{3R'}{S} \right)}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)} \\
I_{23} &= U \cdot \frac{x_0^2 \left[ Z_2 + \frac{R'}{S} \sum_{L=1}^3 e^{j(\varphi_L - \varphi_3)} \right] + Z_1 Z_2 \left( Z_2 + \frac{3R'}{S} \right)}{\left[ x_0^2 + Z_1 \left( Z_2 + \frac{3R'}{S} \right) \right] (x_0^2 + Z_1 Z_2)} \tag{12}
\end{aligned}$$

Neglecting the active resistance  $r_1$  and designating  $Z$ ,  $x$  through  $Z_2 \approx jx_0 \sigma_1$ ,  $x = x_1 + x_0 \sigma_1$ ,

where  $\sigma_1 = \frac{x_1 + x_0}{x_0}$  is the primary dissipation factor, the rotor currents are defined as:

$$\begin{aligned}
I_{21} &= \frac{Z + \frac{\sigma_1 R}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)} \right)}{Z \left( Z + \frac{3R' \sigma_1}{S} \right)} \cdot U \\
I_{22} &= \frac{Z + \frac{\sigma_1 R}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_2)} \right)}{Z \left( Z + \frac{3R' \sigma_1}{S} \right)} \cdot U \tag{13} \\
I_{23} &= \frac{Z + \frac{\sigma_1 R}{S} \left( 3 - \sum_{L=1}^3 e^{j(\varphi_L - \varphi_3)} \right)}{Z \left( Z + \frac{3R' \sigma_1}{S} \right)} \cdot U
\end{aligned}$$

Developed engine moments:



$$M_n = \frac{I_{1n} + I'_{1n}}{2} \cdot U = \frac{U}{2\sigma_1} (I_{2R} + I'_{2R})$$

$$M_1 = \frac{U}{2\sigma_1} (I_{21} + I'_{21})$$

$$M_2 = \frac{U}{2\sigma_1} (I_{22} + I'_{22})$$

$$M_3 = \frac{U}{2\sigma_1} (I_{23} + I'_{23})$$

where  $I'_{21}$ ,  $I'_{22}$ ,  $I'_{23}$  are complex quantities.

We represent the current  $I_{21}$  as:

$$I_{21} = \frac{Z + \frac{\sigma_1 R}{S} - \frac{1}{3} \left[ \left( Z + \frac{3R'\sigma_1}{S} \right) - Z \right] \sum_{L=1}^3 e^{j(\varphi_L - \varphi_1)}}{Z \left( Z + \frac{3R'\sigma_1}{S} \right)} \cdot U \quad (14)$$

$$\text{given that } Z = \frac{r_2 \sigma_1}{S} + jx, \quad Z' = \frac{r_2 \sigma_1}{S} + jx, \quad \frac{e^{j\varphi} + e^{-j\varphi}}{2} = \cos \frac{e^{j\varphi} - e^{-j\varphi}}{2} = \sin \varphi$$

We determine the developed moments of the engines:

$$M_1 = \frac{U^2}{3\sigma_1} \left[ \frac{r_2 \frac{r_2 \sigma_1}{S} \left[ 3 - \sum_{L=1}^3 \cos(\varphi_L - \varphi_1) \right] - x \sum_{L=1}^3 \sin(\varphi_L - \varphi_1)}{\left( \frac{r_2 \sigma_1}{S} \right)^2 + x^2} + \frac{\frac{(r_2 + 3R)\sigma_1}{S} \sum_{L=1}^3 \cos(\varphi_L - \varphi_1) + x \sum_{L=1}^3 \sin(\varphi_L - \varphi_1)}{\left[ \frac{(r_2 + 3R\sigma_1)}{S} \right]^2 + x^2} \right] \quad (15)$$

$$M_2 = \frac{U^2}{3\sigma_1} \left[ \frac{r_2 \frac{r_2 \sigma_1}{S} \left[ 3 - \sum_{L=1}^3 \cos(\varphi_L - \varphi_2) \right] - x \sum_{L=1}^3 \sin(\varphi_L - \varphi_2)}{\left( \frac{r_2 \sigma_1}{S} \right)^2 + x^2} + \frac{\frac{(r_2 + 3R)\sigma_1}{S} \sum_{L=1}^3 \cos(\varphi_L - \varphi_2) + x \sum_{L=1}^3 \sin(\varphi_L - \varphi_2)}{\left[ \frac{(r_2 + 3R\sigma_1)}{S} \right]^2 + x^2} \right] \quad (16)$$

$$M_3 = \frac{U^2}{3\sigma_1} \left[ \frac{r_2 \frac{r_2 \sigma_1}{S} \left[ 3 - \sum_{L=1}^3 \cos(\varphi_L - \varphi_3) \right] - x \sum_{L=1}^3 \sin(\varphi_L - \varphi_3)}{\left( \frac{r_2 \sigma_1}{S} \right)^2 + x^2} + \right.$$

$$+ \frac{\frac{(r_2 + 3R)\sigma_1}{S} \sum_{L=1}^3 \cos(\varphi_L - \varphi_3) + x \sum_{L=1}^3 \sin(\varphi_L - \varphi_3)}{\left[ \frac{(r_2 + 3R\sigma_1)}{S} \right]^2 + x^2} \quad (17)$$

Changes in the supply voltage of the motors were indicated by the coefficients:

$$\frac{U_1}{U_{nom}} = k_1, \quad \frac{U_2}{U_{nom}} = k_2, \quad \frac{U_3}{U_{nom}} = k_3.$$

Further, taking into account the previously accepted assumptions, and introducing the coefficients of voltage change  $k_1 = \frac{U_1}{U_{nom}}$ ,  $k_2 = \frac{U_2}{U_{nom}}$ ,  $k_3 = \frac{U_3}{U_{nom}}$ , we will find the equations for the currents and moments of the motors in the system, taking into account the identity of the parameters of the motors included in the system. Assuming that  $U_1 \neq U_2 \neq U_3$  and  $\varphi_1 \neq \varphi_2 \neq \varphi_3$ , we write the stator and rotor voltage equations for each motor of a three-motor system of synchronous rotation with electrical connection through rotor circuits in the form:

$$\begin{aligned} U_1 &= I_{11}Z_1 - I_{21}jx_0 \\ U_2 &= I_{12}Z_1 - I_{22}jx_0 \quad (18) \\ U_3 &= I_{13}Z_1 - I_{23}jx_0 \\ (I_{11}jx_0 - I_{21}Z_2)e^{j\varphi_1} &= \frac{R}{S}(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \\ (I_{12}jx_0 - I_{22}Z_2)e^{j\varphi_2} &= \frac{R}{S}(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \quad (19) \\ (I_{13}jx_0 - I_{23}Z_2)e^{j\varphi_3} &= \frac{R}{S}(I_{21}e^{j\varphi_1} + I_{22}e^{j\varphi_2} + I_{23}e^{j\varphi_3}) \end{aligned}$$

Taking into account the possible changes in voltages  $U_1$ ,  $U_2$ ,  $U_3$  using the coefficients  $k_1$ ,  $k_2$ ,  $k_3$  and substituting the value of the stator currents from Eq. (18) into Eq. (19), we obtain the expressions for rotor currents Eq. (20). Since the engines of the coordinated rotation system are assumed to be identical, we will write the expressions for rotor currents and moments only for the first engine:

$$\begin{aligned} I_{21} &= \frac{\left[ \left( Z + \frac{3R\sigma_1}{S} \right) k_n - \frac{R\sigma_1}{S} \sum_{L=1}^3 k_L e^{j(\varphi_L - \varphi_1)} \right]}{Z \left( Z + \frac{3R\sigma_1}{S} \right)} U = Uk_1 \frac{\left( Z + \frac{3R\sigma_1}{S} \right) - \frac{1}{3} \left[ \left( Z + \frac{3R\sigma_1}{S} \right) - Z \right] \sum_{L=1}^3 \frac{k_L}{k_1} e^{j(\varphi_L - \varphi_1)}}{Z \left( Z + \frac{3R\sigma_1}{S} \right)} = \\ &= \frac{Uk_1}{3} \left[ \frac{3 - \sum_{L=1}^3 \frac{k_L}{k_n} e^{j(\varphi_L - \varphi_1)}}{Z} + \frac{\sum_{L=1}^3 \frac{k_L}{k_n} e^{j(\varphi_L - \varphi_1)}}{Z + \frac{3R\sigma_1}{S}} \right] \quad (20) \\ M_1 &= \frac{2}{3} M_{1\max} \left\{ \frac{3 - \sum_{L=1}^3 \frac{k_L}{k_1} \left[ \cos(\varphi_L - \varphi_1) + \frac{S}{S_{\max}} \sin(\varphi_L - \varphi_1) \right]}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} + \frac{\sum_{L=1}^3 \frac{k_L}{k_1} \left[ \cos(\varphi_L - \varphi_1) + \frac{S}{S'_{\max}} \sin(\varphi_L - \varphi_1) \right]}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \right\} \end{aligned}$$

(21)

where  $M_{1\max} = \frac{U^2 k_1^2}{2\sigma_1 x}$ ,  $S_{\max} = \frac{r_2' \sigma_1}{x_1 + x_2' + \sigma_1}$ ,  $S'_{\max} = S_{\max} \left( 1 + \frac{3R'}{2r_2'} \right)$ .  $M_{1\max(2,3)}$  respectively, are the maximum moments of the engines.



We write expressions for the moment of the first engine, dividing them into asynchronous and synchronizing components:

$$M_1 = \frac{U^2 k_1^2}{2\sigma_1 x} \left\{ \frac{3 - \sum_{L=1}^3 \frac{k_L}{k_1} \cos(\varphi_L - \varphi_1)}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} + \frac{\sum_{L=1}^3 \frac{k_L}{k_1} \cos(\varphi_L - \varphi_1)}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \right\} + \frac{U^2 k_1^2}{2\sigma_1 x} \left\{ \frac{\sum_{L=1}^3 \frac{k_L}{k_1} \frac{S'_{\max}}{S} \sin(\varphi_L - \varphi_1)}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} - \frac{\sum_{L=1}^3 \frac{k_L}{k_1} \frac{S}{S_{\max}} \sin(\varphi_L - \varphi_1)}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} \right\} \quad (22)$$

As can be seen from equation (22), the magnitude of the torque and, accordingly, the equalizing torque of a given motor are interrelated affected by changes in the supply voltages of other machines. Similarly, one can write an expression for currents, moments, and synchronizing moments of a multi-motor system with adjustable voltage, from which, as a special case, currents, moments for two, three, etc. can be found. motor controlled and unregulated system of synchronous rotation with electrical connection through rotary circuits. Turquoises for a synchronous rotation system with electrical connection through rotary circuits with the  $n^{\text{th}}$  motor are defined as:

$$M_n = \frac{U^2 k_n^2}{n\sigma_1 x} \left[ \frac{n - \sum_{L=1}^n \frac{k_L}{k_n} \left[ \cos(\varphi_L - \varphi_n) - \frac{S}{S_{\max}} \sin(\varphi_L - \varphi_n) \right]}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} \right] + \frac{U^2 k_n^2}{n\sigma_1 x} \left[ \frac{\sum_{L=1}^n \frac{k_L}{k_n} \left[ \cos(\varphi_L - \varphi_n) + \frac{S}{S'_{\max}} \sin(\varphi_L - \varphi_n) \right]}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \right] \quad (23)$$

where the first term is the asynchronous component, the second is the synchronizing component. The general equalizing moment in the  $n$  motor system of synchronous rotation between the  $n^{\text{th}}$  and  $m^{\text{th}}$  motor has the expression:

$$M_{\text{general syn nm}} = \frac{U^2}{n\sigma_1 x} \left[ \frac{k_n^2 \left[ n - \sum_{L=1}^n \frac{k_L}{k_n} \cos(\varphi_L - \varphi_n) \right] - k_m^2 \left[ n - \sum_{L=1}^m \frac{k_L}{k_n} \cos(\varphi_L - \varphi_m) \right]}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} + \right. \\ \left. + \frac{K_n^2 \sum_{L=1}^n \frac{K_L}{K_n} \cos(\varphi_L - \varphi_n) - K_m^2 \sum_{L=1}^m \frac{K_L}{K_m} \cos(\varphi_L - \varphi_m)}{\frac{S}{S'_m} + \frac{S'_m}{S}} - \frac{U^2}{n\sigma_1 x} \left[ \frac{K_n^2 \sum_{L=1}^n \frac{K_L}{K_n} \frac{S}{S'_m} \sin(\varphi_L - \varphi_n) - K_m^2 \sum_{L=1}^m \frac{K_L}{K_m} \frac{S}{S'_m} \sin(\varphi_L - \varphi_m)}{\frac{S}{S'_m} + \frac{S'_m}{S}} - \right. \right. \\ \left. \left. - \frac{K_n^2 \sum_{L=1}^n \frac{K_L}{K_n} \frac{S}{S'_m} \sin(\varphi_L - \varphi_n) + K_m^2 \sum_{L=1}^m \frac{K_L}{K_m} \frac{S}{S'_m} \sin(\varphi_L - \varphi_m)}{\frac{S}{S'_m} + \frac{S'_m}{S}} \right] \right] \quad (24)$$

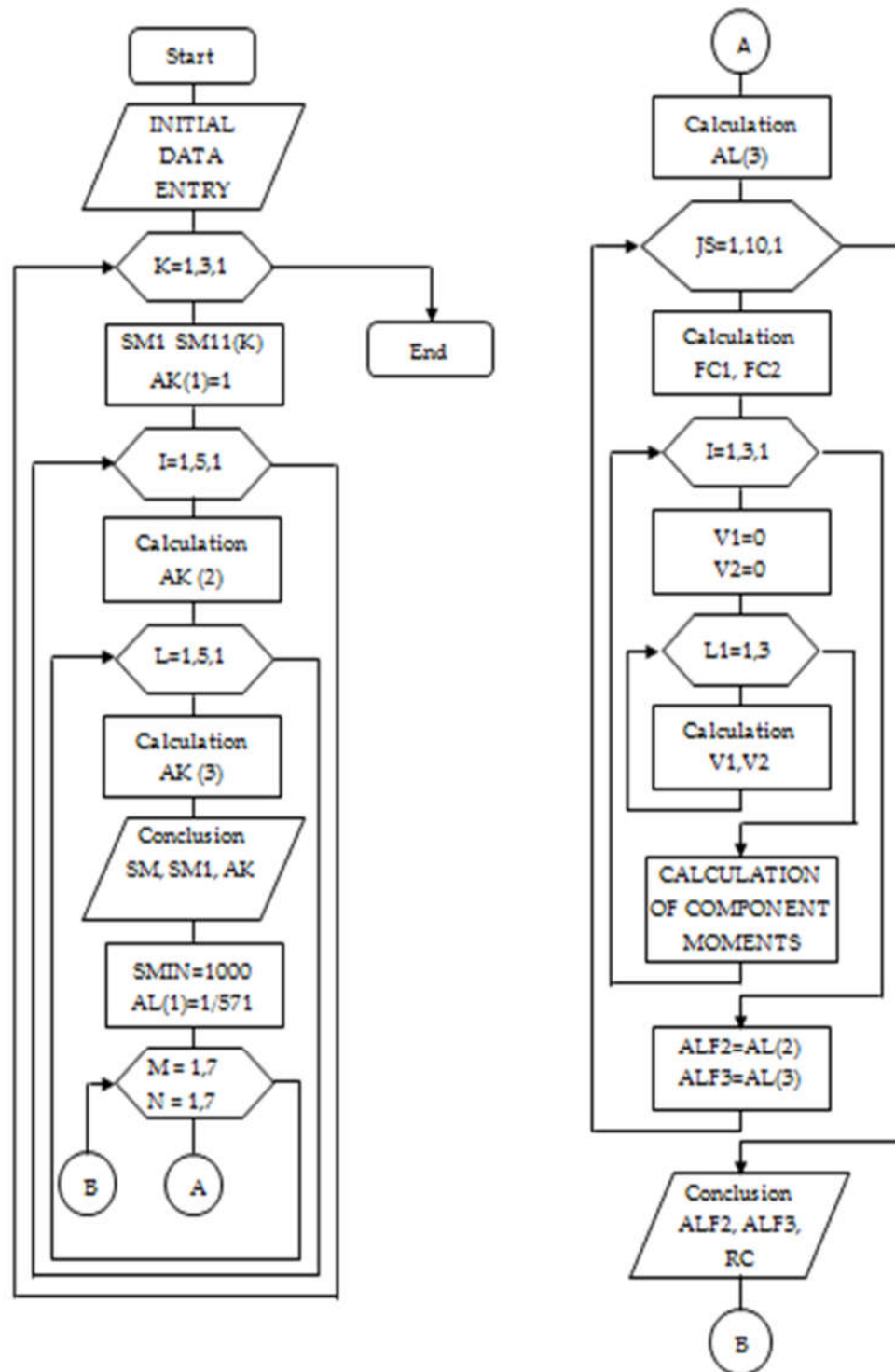
To calculate the mechanical characteristics, we use Eq. (8), while giving different values to the mismatch angles, changing the magnitude of the supply voltage, and also changing the total rotor resistance. According to the above expressions, a calculation was carried out for motors of the type *Ue, 56a, 154W, IP44* of the electric drive carding machine (CM) CR-24 with the following parameters:

$$U_n = \frac{220}{380} \text{ W}; U_2 = 153 \text{ W}; \omega_n = 960 \text{ rpm}; I_1 = \frac{21,4}{12,4} \text{ A}; I_2 = \frac{12}{22,5} \text{ A}; f_c = 50 \text{ Hz}.$$

### 3. Algorithm for Calculating the Electromechanical Ratio of a Multi-Motor Asynchronous Electric Drive

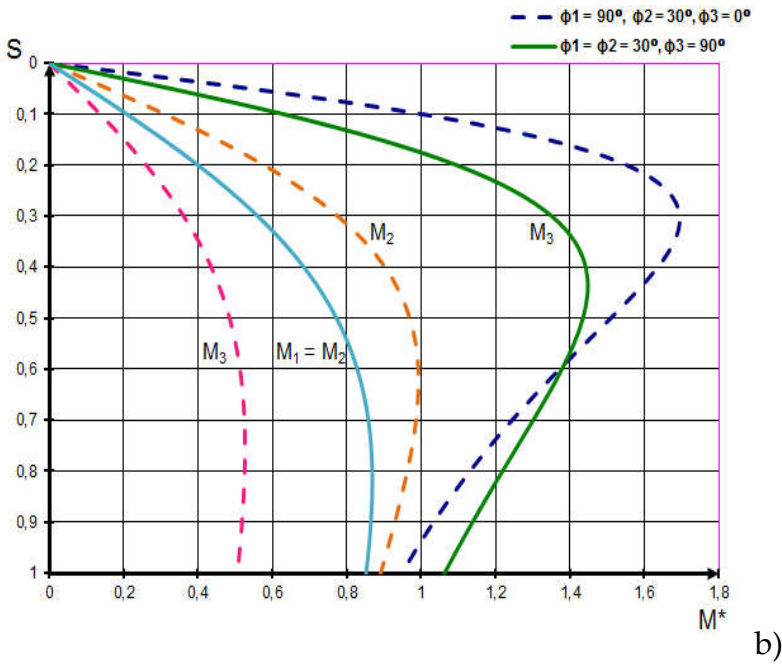
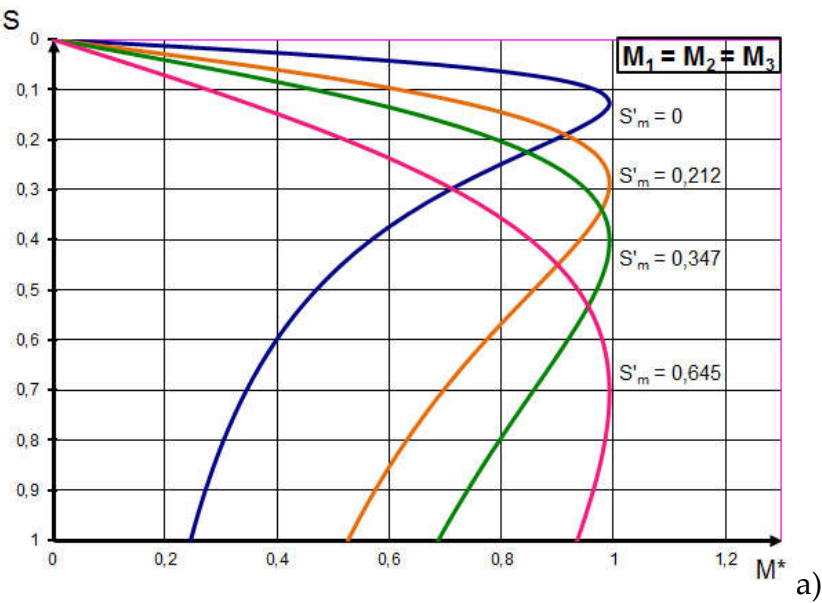
The algorithm for calculating the mechanical characteristics of the three-engine MAEDs system, taking into account the change and the angular positions of the rotor, is shown in Figure 2, and the mechanical characteristics are plotted when changing various parameters. By changing the values of

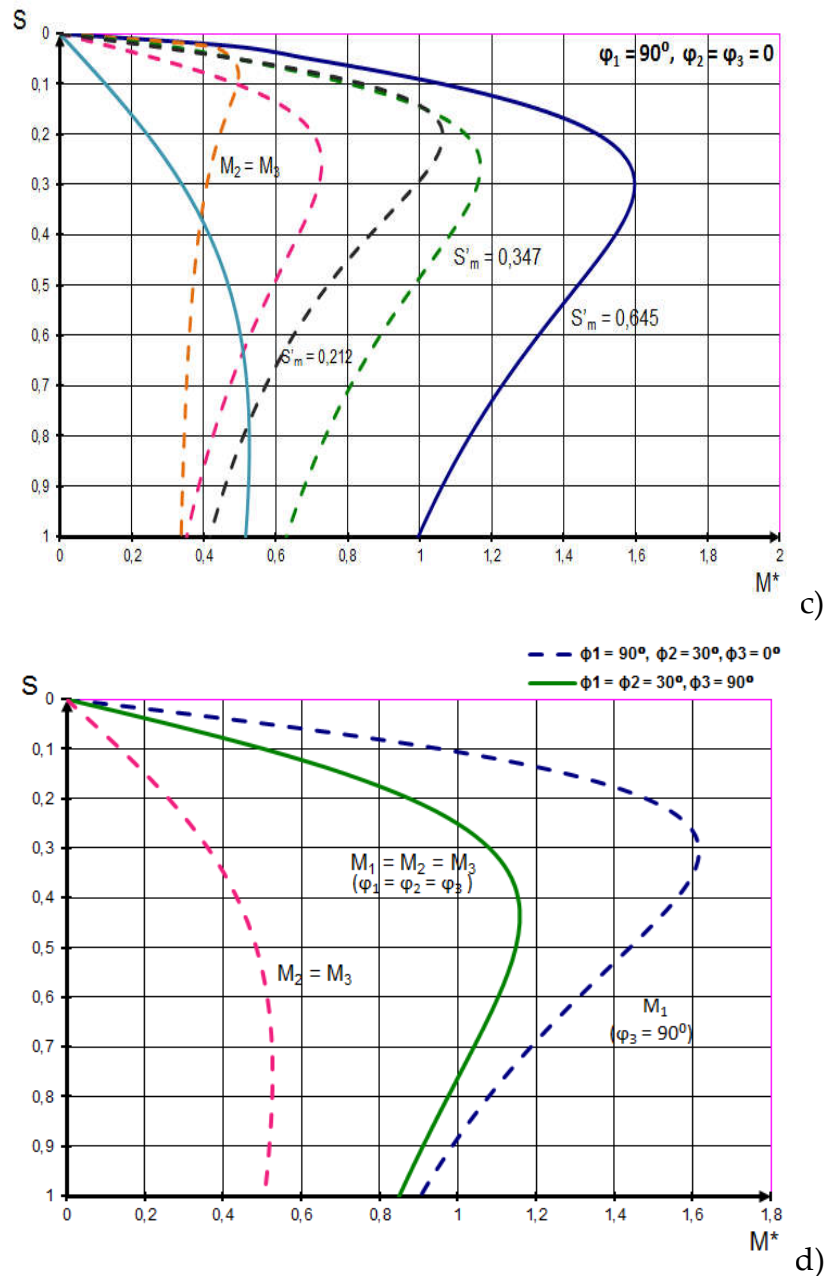
these coefficients and angles, you can obtain a large number of graphs of mechanical characteristics shown in Figure 2.



**Figure 2.** Algorithm for calculating the mechanical characteristics of a three-engine MAEDs system.

The results of the calculation are shown in Figure 3. The calculated curves of mechanical characteristics are built for three values of additional resistances corresponding to three stages and critical slips:  $S'_m = 0,212; 0,347; 0,645$  (see Figure 3a) and mismatch angles  $\Delta\varphi_{21} = \Delta\varphi_{23} = 90^\circ$  (see Figure 3b),  $\Delta\varphi_{12} = 60^\circ$ ,  $\Delta\varphi_{13} = 90^\circ$  (see Figure 3c) of the engine rotors.

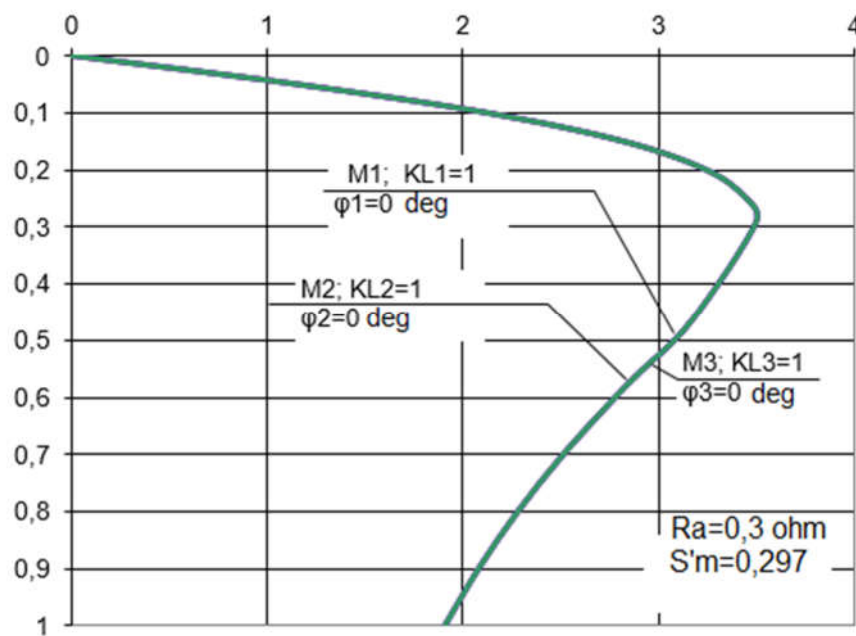




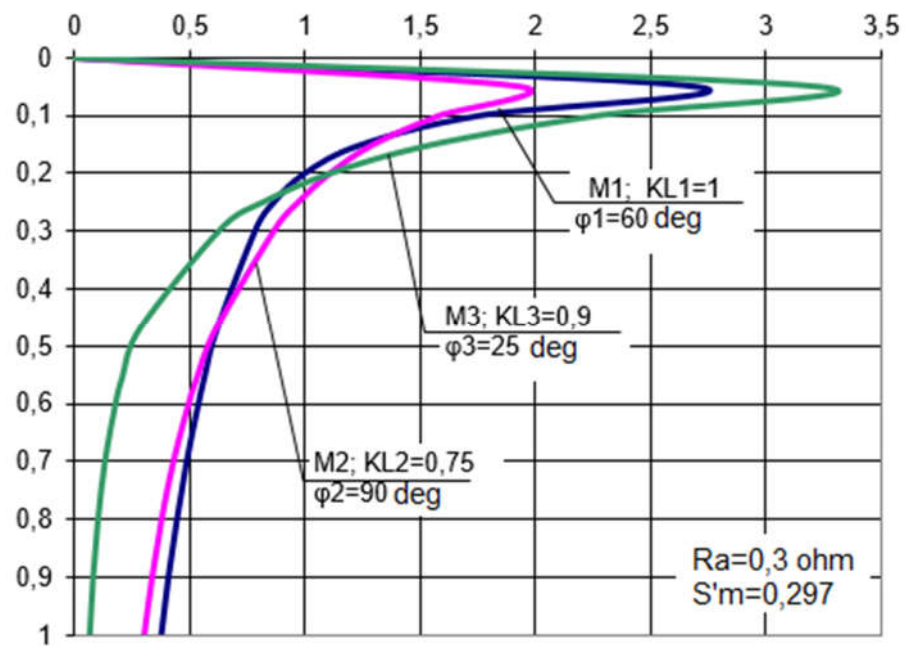
**Figure 3.** Mechanical characteristics of a three-motor electric drive carding machine (CM) at different angles of mismatch and total rotor resistance.

The curves with slip  $S'_m = 0,645$ , shown in Figure 3a, are typical for the operating CM of the CR-24 type, the value of the resistance not switched off from the common rotor circuit is taken equal to  $0.19 \Omega$  from the point of view of the parameters that are optimal according to technological requirements. At the same time, the rigidity of the mechanical characteristic is much lower than that of the characteristics with  $S'_m = 0,347$  (dashed line with a dot) and  $S'_m = 0,212$  (dashed line) in Figure 3a. At  $S'_m = 0,645$ , the EOS system tends to self-oscillate at static moments higher than  $M_{st.nom}$ . The system at critical angles of mismatch  $\Delta\varphi = 90^\circ$  develops an equalizing maximum moment equal to  $M_{eq12} = M_{eq13} = 1,29M_{max}$ , i.e., it can work stably at values of static moments that satisfy the condition:  $M_{st1,2,3} = 1,20M_{max}$ . Figure 3b shows the dependences of  $M_{syn} = f(S)$  for several slip values in the presence of resistance  $R_a = 0,05; 0,08; 0,19\Omega$ . Obviously, approaching the

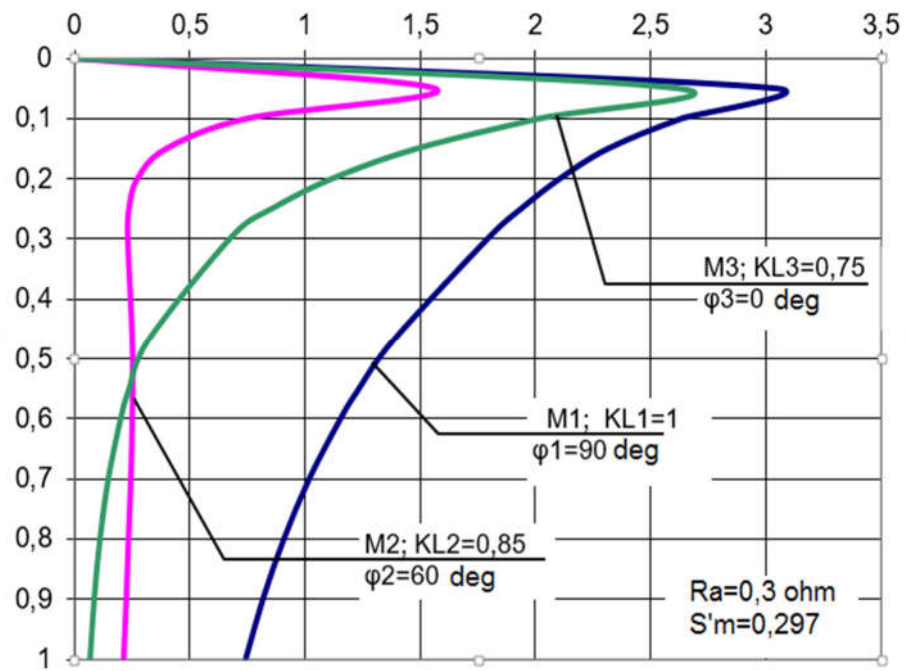
synchronous speed greatly reduces the magnitude of the synchronizing components of the motor torques. An increase in the value of active resistances in the common rotor circuit simultaneously with a decrease in the speed of the entire system increases its synchronizing capacity. The negative values of the synchronizing components of the moments are due to the difference in the loads on the shafts. In this case, the synchronizing torques maintains consistent rotation. The difference between these moments determines the action of the entire system. For example, in the variant under consideration, the first engine is assumed to be the most loaded, and its synchronizing component of the torque is equalized by the sum of the moments of the other two engines, i.e.,  $M_{syn1} + M_{syn2} + M_{syn3} = 0$ . Figure 3a shows the synchronizing torques of the system engines at mismatch angles of the position of the rotors  $\Delta\varphi_{1,2} = 90^\circ$  const. Equalizing moments between the first and third, second and third engines of the system at angle  $\Delta\varphi_{1,3} = 0$  take maximum values, gradually decreasing with increasing  $\Delta\varphi_{1,3}$ . The synchronizing component of the torque of the third machine at  $\Delta\varphi_{1,3} = 180^\circ$  is equal to zero, and the other machines are equal to each other, but have opposite signs. Equalizing moments reach their maximum at  $\Delta\varphi \pm 90^\circ$ , equal to zero at  $\Delta\varphi = 180^\circ$  and  $\Delta\varphi = 0$  (see Figure 3b). With small slips, the motors of the system develop only very limited moments; therefore, their synchronizing components are small. Therefore, we can conclude that the EOS system in the CM drive works satisfactorily with a slip of at least 0.15-0.3 (see Figure 3c and Figure 3d). The above calculations have shown that in systems with large additional resistances, the torques of certain motors become negative, i.e., the system can only work when mechanical energy is supplied to these motors from the load side. As can be seen from expression Eq. (26), the total equalizing moment between the motors consists of the sum of the asynchronous and synchronizing components of the motors. Equalizing moments are also formed due to the difference in drive torques. Graphs based on the calculation results when the supply voltage of the motors changes is shown in Figure 4.



a)

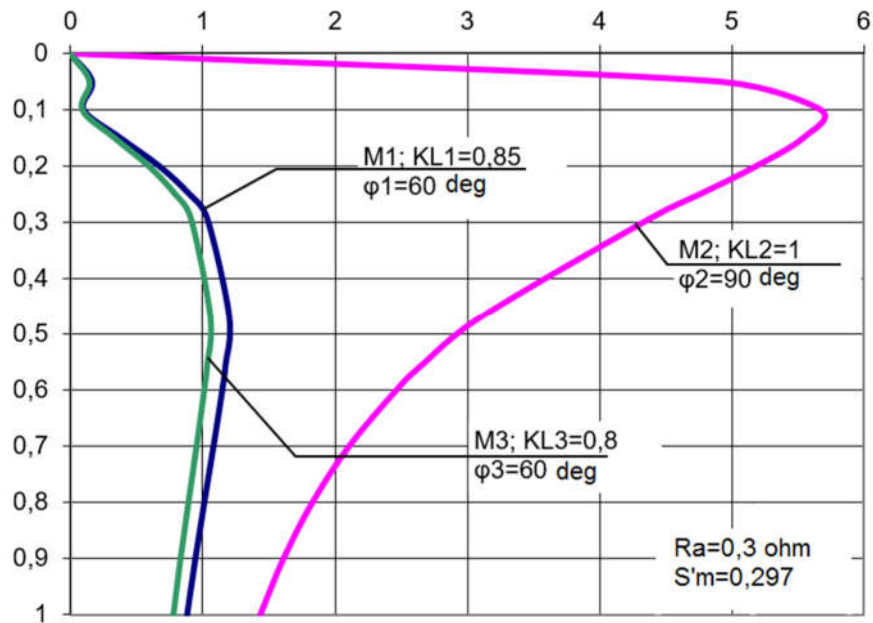


b)

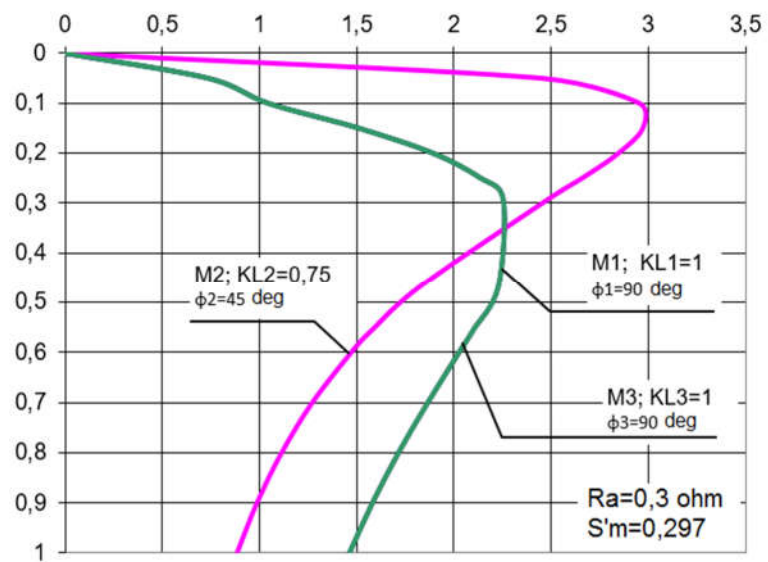


c)

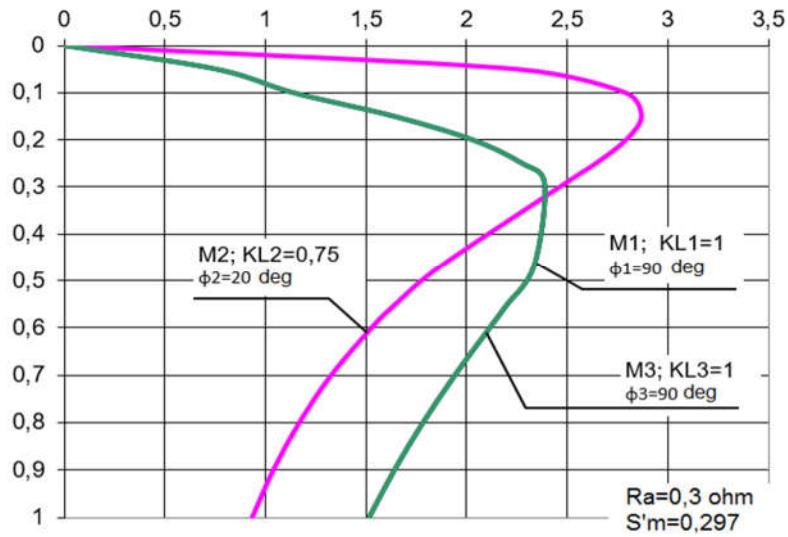




d)



e)



f)

**Figure 4.** Graphs of the mechanical characteristics of MAEDs with a change in the supply voltages of the motors.

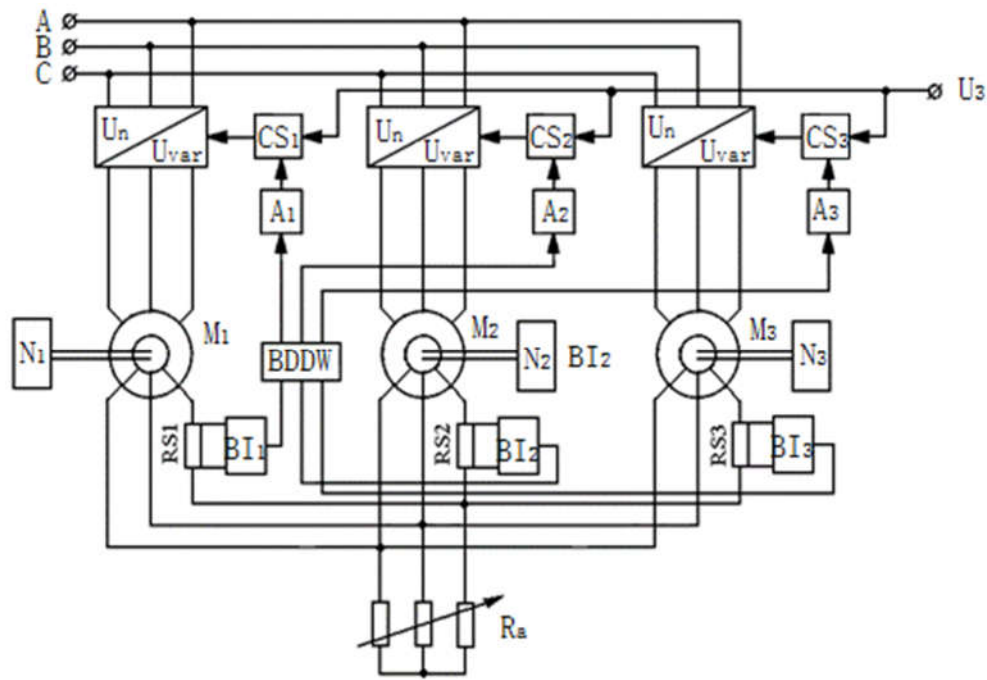
In a MAEDs system with TVC, the synchronizing capacity of the system is determined by equalizing torques consisting of the difference in the torques of the motors of the system with changes in the magnitude of the supply voltage. The mechanical characteristics of the system engines (in Figure 4a) were obtained with  $U_1=U_2=U_3$  and  $\varphi_1=\varphi_2=\varphi_3=0$  i.e., all characteristics are identical from the accepted condition of the identity of engines  $M_1, M_2, M_3$ . All characteristics are obtained with the minimum residual resistance in the common circuit of the rotors. In the characteristics (b, c, d), the supply voltages are changed within 75% -90% of the nominal value, and the angular positions of individual rotors are in the range from  $0^\circ$  to  $90^\circ$ . In Figures 4 (e, c), the mechanical characteristics are similar, but differ at the same total voltages for the first and third engines, and the value of the second engine is reduced by 25% and differ in the angular positions of the rotors ( $20^\circ$  and  $45^\circ$ ). The results of the study reveal that the difference in angular positions does not exceed  $45^\circ$  и  $70^\circ$ , and the value of the supply voltage is from 0.75 to 1.0 of the nominal value. With such AM with TVC changes, the system works stably. Equalizing moments are also formed due to the difference in drive moments. From the obtained expressions of the moments it follows that with the in-phase rotation of three machines, that is, with  $U_1 = U_2 = U_3 = U_{1n}$  and  $\varphi_1 = \varphi_2 = \varphi_3$ :

$$M_{1,2,3} = \frac{2M_{\max}}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \quad (25)$$

In this case, all three machines operate on rheostatic characteristics with tripled additional resistance  $3R_a$ , and the equalizing moments are equal to zero.

#### 4. Development of an Adjustable Multi-Motor Asynchronous Electric Drive

Many variants of a multi-motor asynchronous electric drive (MAEDs) with thyristor voltage converters (TVC) have been proposed, showing a significant improvement in the synchronizing capacity of such systems compared to the classical system of asynchronous electric drive of matched rotation [7–9]. One of the areas of such developments is multi-motor asynchronous electric drives with adjustable supply voltages [4]. The principle of this system is to increase the synchronizing capacity of MAEDs by regulating the supply voltages according to the load of the motors, i.e., the maximum loaded motor is supplied with maximum energy, and the less loaded motor is supplied with voltage according to the load. Figure 5 shows MAEDs with TVC, made on thyristors (a) [11] and on transistors (b) [12]. MAEDs with TVC works like this:



**Figure 5.** Functional diagram of MAEDs with TVC with determination of the motor load difference.

In practical implementation, the power circuit of the TVC-AM system contains six thyristors connected in pairs in anti-parallel to the stator circuits of a three-phase asynchronous motor [13–15]. Such a converter is designed to regulate the 1st, or fundamental, harmonic that feeds the voltage motor by changing the thyristor opening angle  $\alpha$  in the range from  $\alpha=\varphi$  to  $\alpha=180^\circ$ . In this case, the effective phase voltage of the first harmonic changes from  $U_1=U_{1nom}$  (where  $U_1=U_{1nom}$  is the effective phase rated voltage of the supply network;  $\varphi$  is the phase angle of the load, determined from the design parameters of the motors  $\varphi = \arctg\left(\frac{\omega_{L_0}}{R}\right)$  to  $U_1=0$ ).

The frequency of the alternating voltage of the fundamental harmonic remains unchanged and is equal to the mains frequency, i.e.,  $f_1=f_{1nom}$ . With this control, the synchronous speed of the asynchronous motor and the critical slip do not change, but the motor torque  $M=f(U_1^2)$  is controlled. The degree of loading of the motors is determined: in the sensors of the phase of the rotor currents, signals are selected that are proportional to the phases of the rotor currents and converted into a control signal proportional to the angles of mismatch of the rotor currents of each motor relative to the total rotor current. Therefore, a signal equal to:

$$\begin{aligned} U_{y1} &= U_3 - U_{21} \\ U_{y2} &= U_3 - U_{22} \\ U_{y3} &= U_3 - U_{23} \end{aligned} \quad (26)$$

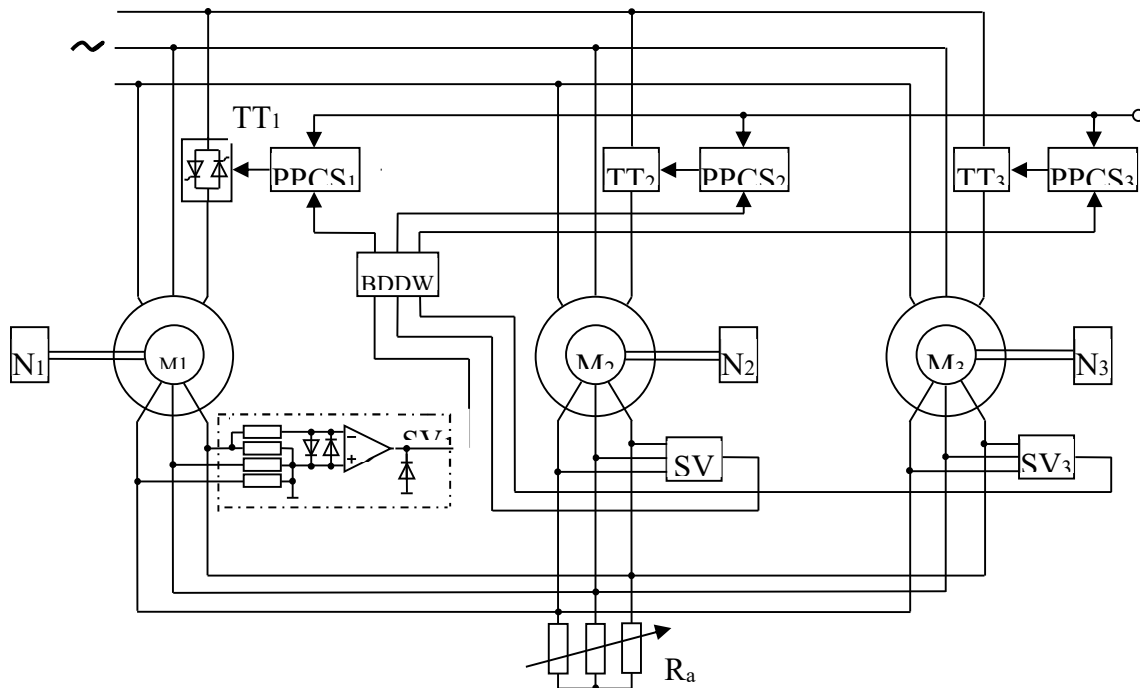
The control signals  $U_{y1}$ ,  $U_{y2}$ ,  $U_{y3}$  contribute, by changing the energy flow supplied to each motor, to equalize the phases of the rotor currents, that is, the synchronism of the rotation of the speeds of all the motors of the MAEDs system with TVC. The equalizing moment of the system with a common rotor resistance is subject to a synchronizing effect caused by the difference in the voltages supplying the motors. In this case, the leading motor, which has a lower load, is supplied with less voltage, and the lagging one is supplied with more voltage in accordance with the magnitude and sign of the mismatch angle. The thyristor groups of the most loaded motor open completely.

Here, the mismatch angles are determined by the load difference, therefore, the control accuracy of a multi-motor asynchronous electric drive of synchronous rotation is determined by the accuracy

and measurement limits of the mismatch angle of the position of the rotors, due to the difference in load moments on the shafts of electric motors that are not kinematically connected to each other.

The rest of the engines receive power in accordance with the load. The general speed control of the MAEDs system with TVC in accordance with the technological requirements in small ranges can be made by changing the signal  $U_3$  or the total resistance  $R_a$ , which in this scheme can be minimal. A multi-motor asynchronous electric drive has been developed that allows for synchronous torque control using asymmetric voltage regulators and synchronous braking by asymmetric power supply of stator windings of asynchronous electric motors. This circuit solution provides preliminary synchronization of the rotors of all motors by closing back-to-back thyristors in one phase, as well as synchronous braking of motors or operating mechanisms after turning on the thyristors and connecting the windings of the third phase to the second.

If an asymmetric voltage is applied to the stator windings of identical asynchronous motors in accordance with the diagram shown in Figure 6, then when analyzing the mechanical characteristics of an asynchronous motor, the given system of asymmetric voltages can be replaced by two symmetrical voltage systems of positive and negative sequences. Both voltage systems create positive and negative sequence rotating fields, respectively. In the direction of the positive sequence field, the rotor moves, which has slip  $1 + (1 - S) = 2 - S$  with respect to the negative sequence field, where  $S$  - is the slip relative to the positive sequence field.



**Figure 6.** Three-motor electric drive with asymmetric thyristor voltage converters.

where marked:

$M_1, M_2, M_3$  – is the asynchronous motors with a phase rotor;

$N_1, N_2, N_3$  – is the motor shaft loads;

$SV_1, SV_2, SV_3$  – is the rotary voltage sensors EMF;

$TT_1, TT_2, TT_3$  – is the back-to-back thyristors;

$BDDW$  – is the block for determining the degree of workload;

$PPCS_1, PPCS_2, PPCS_3$  – is the pulse-phase control systems;

$R_a$  – is the total rotor resistance EOS.

Expressions for the moments of three induction motors from the positive and negative sequence fields in the MAEDs SR system can be found based on the  $T$ -shaped equivalent circuit shown in Figure 6. In this case, the torques of the engines will have the form: direct sequence:

$$M_{1,2,3}^F = \frac{2M_{\max}}{3} \left[ \frac{3 - \sum_{L=1}^3 \cos(\theta_L - \theta_{1,2,3})}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} + \frac{\sum_{L=1}^3 \cos(\theta_L - \theta_{1,2,3})}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \right] + \frac{2M_{\max}}{3} \left[ \frac{\frac{S}{S_{\max}} \sum_{L=1}^3 \sin(\theta_L - \theta_{1,2,3})}{\frac{S}{S_{\max}} + \frac{S_{\max}}{S}} - \frac{\frac{S}{S'_{\max}} \sum_{L=1}^3 \sin(\theta_L - \theta_{1,2,3})}{\frac{S}{S'_{\max}} + \frac{S'_{\max}}{S}} \right] \quad (27)$$

Reverse sequence:

$$M_{1,2,3}^I = \frac{2M_{\max}}{3} \left[ \frac{3 - \sum_{L=1}^3 \cos(\theta_L - \theta_{1,2,3})}{\frac{2-S}{S_{\max}} + \frac{S_{\max}}{2-S}} + \frac{\sum_{L=1}^3 \cos(\theta_L - \theta_{1,2,3})}{\frac{2-S}{S'_{\max}} + \frac{S'_{\max}}{2-S}} \right] + \frac{2M_{\max}}{3} \left[ \frac{\frac{2-S}{S_{\max}} \sum_{L=1}^3 \sin(\theta_L - \theta_{1,2,3})}{\frac{2-S}{S_{\max}} + \frac{S_{\max}}{2-S}} - \frac{\frac{2-S}{S'_{\max}} \sum_{L=1}^3 \sin(\theta_L - \theta_{1,2,3})}{\frac{2-S}{S'_{\max}} + \frac{S'_{\max}}{2-S}} \right] \quad (28)$$

where  $M_{1,2,3}$  - is the torques of the first, second and third engines;  $M_{\max}$  - is the maximum torque of the motors;  $S$  - slip of asynchronous motors;  $S_{\max}, S'_{\max}$  - is the maximum slip of the engine separately and in the system of the electric working shaft;  $\theta_{1,2,3}$  - is the angular displacements of motor rotors;  $\theta_L$  - is the angular position of the rotor of the corresponding motor.

Total moments, i.e., The torques of each motor in the MAEDs SR system with unbalanced connection of the stator windings are defined as:

$$\begin{aligned} M_1 &= M_1^D - M_1^R \\ M_2 &= M_2^D - M_2^R \\ M_3 &= M_3^D - M_3^R \end{aligned} \quad (29)$$

As can be seen from the expression of the moments of asynchronous motors in MAEDs SR, the moments of the motors consist of asynchronous and synchronizing components (the second terms are proportional to the sine of the angular position of the rotors). As the graphs of mechanical characteristics during synchronous braking have shown, they coincide and overlap each other as rectilinear curves with a multi-motor version and prove the correctness of the theory as asymmetric braking in a single-motor version.

## 5. Conclusions

Based on the  $T$  - figurative equivalent circuit:

1. Analytical expressions for torques, stator and rotor currents of asynchronous motors of a coordinated rotation system are obtained.
2. An algorithm for calculating the main electromechanical ratios has been compiled, mechanical characteristics have been constructed for various values of rotor resistance, supply voltages and angular positions of the rotors of asynchronous motors of a coordinated rotation system.
3. Multi-motor asynchronous electric drives with thyristor converters with increased synchronizing capabilities have been developed.
4. A multi-motor asynchronous electric drive with preliminary synchronization, synchronous starting and braking has been developed.

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