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Article

Individual Urban Trees Clustering in LiDAR Data with 3-D Gestalt Measures

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Abstract: Despite the technological advancements of 3-D city models, the 3-D shape abstraction methods for urban vegetation are recent and still limited to support spatial analysis of individual or groups of trees and forest patches. In this paper, a scheme for individual urban tree abstraction, which retains the semantic complexity of the object, is proposed. Our contribution is three-fold. First, an initial tree structure based on a new 3-D aggregation operator is proposed. Second, we developed Gestalt rules for 3-D urban vegetation mapping. Third, current state-of-the-art deep learning is adapted for the abstraction of individual urban trees. Quantitative and qualitative results show the effectiveness of our proposed approach in accurately reducing the spatial density of trees and the degree of fragmentation of the total green area, which can access information about the location, size, and spatial distribution of mapped urban trees.

Keywords: urban vegetation; LiDAR; gestalt measures; deep learning; 3-D aggregation; 3-D abstraction

1. Introduction

Urban vegetation mapping is critical in many purposes, such as conservation of biodiversity [1–3], reduces the urban heat island effect [4,5], vegetation monitoring [6–9], climate change optimization and urban ecosystem services [10], and others. Usually, satellite imagery of ultra-high resolution, unmanned aerial vehicle (UAV) imagery, very-high resolution, and moderate to high resolution imagery have been effectively employed for urban vegetation mapping [11].

Since two or more images should be used for reconstruction of Earth's surface, it requires additional post-processing tasks to capture the volumetric representation of the trees. Additionally, the homogeneous regions represented in vegetation areas remain a limitation for matching algorithms. Thus, although remote sensing imagery-based data can be used to estimate some vertical tree metrics, additional 3-D data on tree condition is essentially important for mapping of urban vegetation in details [12]. Furthermore, urban vegetation cover is highly fragmented making accurate mapping more complex and challenging [13]. It is also important to note that the composition of urban vegetation and the small-scale effects of urban trees must be considered to derive high accuracy measurements [14].

Nowadays, by considering the growing application of 3D city models in urban analysis and the accurate knowledge of urban trees as basis for decision making, a comprehensive and high-resolution data on local scale are needed for urban vegetation studies. Light detection and ranging (LiDAR) sensors can directly collect very high-resolution unstructured 3-D data of urban vegetation on a city-wide scale. It can penetrate through the foliage, enabling us to measure tree heights and forest canopies. Thus, LiDAR can be further utilized as a crucial remote sensing technology for accurate urban vegetation mapping to effectively assist city councils with many tasks, such as street tree monitoring, designing strategies, air pollution, and urban noise monitoring [15,16]. In recent years, we have witnessed an increasing interest in urban vegetation mapping using LiDAR data [17–24].

Advances in technology have made LiDAR more agile and flexible in data acquisition. For example, a UAV-based LiDAR system (ULS) can obtain an amount of point density/m² much higher than an airborne-based LiDAR system (ALS). Consequently, more significant computational effort is required to process, manage, assess, and visualize urban vegetation LiDAR data [25]. However, it proved difficult to extract 3-D information from high-density LiDAR data due to the levels of detail (LoD) requirements, the complexity of work with unstructured reconstructing structures, the lack of computation power, and the available data.

Thus, the research community shifted its focus away from the LiDAR paradigm. From Cezanne's insight that an object can be conceived as composed of a set of volumetric features, recent advances in 3-D shape abstraction tasks and deep learning techniques have achieved an alternative method in mitigating the limitations of computational effort in storage, analysis, transmission, and visualization of LiDAR data.

3-D Shape abstraction represents a subjective data derivation process that can reduce visual complexity and storage requirements without losing its semantic complexity [26]. In practice, it can be a way to generate compact spatial representation models from LiDAR data with lower computational requirements for data storage, analysis, and visualization procedures [27]. Furthermore, 3-D clustering tasks reduce the geometric and semantic LoD of existing objects in 3-D city models and maintain spatial coherence with sufficient realism.

A variety of studies with different objectives can be cited based on 3-D clustering. They range from the 3-D representation of buildings [28–36] to methods for clustering complex 3D shapes [37–40]. With the growing demand for 3-D-city models, the CityGML 3.0 model has been used as a 3-D clustering based on aggregation operators [41] to obtain a standard for building representations with different LoD.

Many approaches aim to directly reduce the computational cost within deep learning based computer vision algorithms. They can further assist in LiDAR data compression for different fields [42–45]. In [46], a deep network comprised of unorganized LiDAR data using a hierarchical feature learning approach was proposed. [47] devised a tree-structured deep conditional entropy model to estimate the probability of occurrence of a given symbol for LiDAR data compression. They learn an octree structure using the sparsity and structural redundancy between points. After the learned entropy model is passed to compress the octree. Then, the point cloud is built from the same entropy model. Local feature descriptors discretize the point clouds, taking common characteristics of the real world.

In [48], a deep compression LiDAR data that avoids the voxelization process and excessive memory usage was implemented. A deep convolutional autoencoder network based on kernel points [43] was used to learn local geometric features. Furthermore, they proposed a 3-D deconvolution method to avoid discretization effects caused by voxel grids and skip connections. Nevertheless, 3-D shape abstraction methods of urban vegetation are recent and still limited in supporting spatial analysis of individual or groups of trees and forest patches.

Furthermore, none of the existing methods are sufficiently interpretable to allow for LiDAR data scene understanding as required by urban vegetation studies. Toward this goal, we adopted a scheme for individual urban tree abstraction, which retains the semantic complexity of the object (see Figure 1).

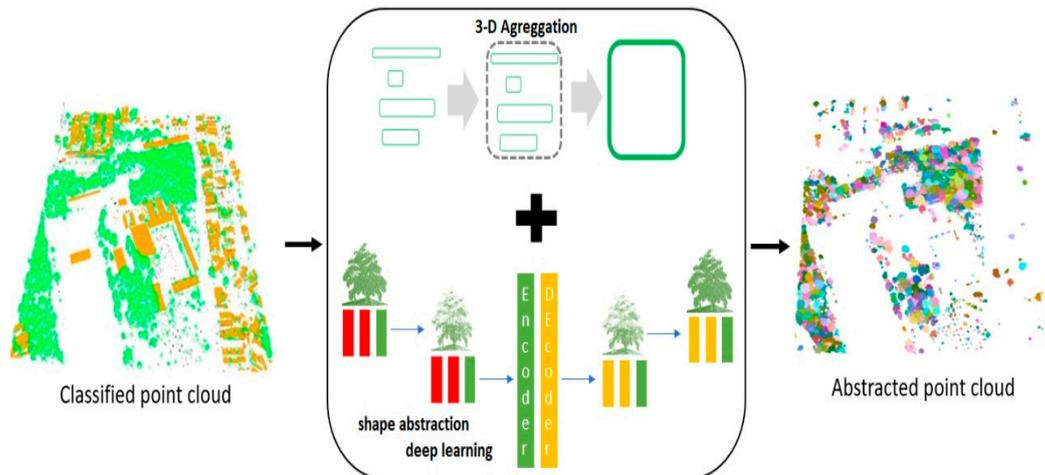


Figure 1. LiDAR data obtained by a ULS require a large amount of memory. Processing this data for storing, analyzing, transmitting, and visualization tasks requires both the aggregation and the compression of the data. A subsequent development for this synergy has allowed us to abstract 3-D shapes of urban vegetation without losing its semantic complexity.

For this purpose, the approach comprises all processing tasks from LiDAR data classification to individual tree segmentation, aggregation, and abstraction. Such LiDAR data are acquired with airborne LiDAR systems (ALS) and unmanned vehicle LiDAR-based (ULS). Considering related works, the main contributions will be highlighted: (1) The construction of the initial tree structures based on a new 3-D aggregation operator; (2) The Gestalt rules adapted for 3-D urban vegetation studies; and (3) The abstraction of individual urban trees using a current state-of-the-art in deep learning.

The rest of this paper is organized as follows. Section 2 details the proposed method. Section 3 describes the dataset used in this study, followed by the experiments and results in Section 4. Discussions are presented in Section 5. The article ends in Section 6 with concluding remarks and suggestions for further work.

2. Methodology

The individual urban tree abstraction approach consists of three successive processing steps, as shown in Figure 2.

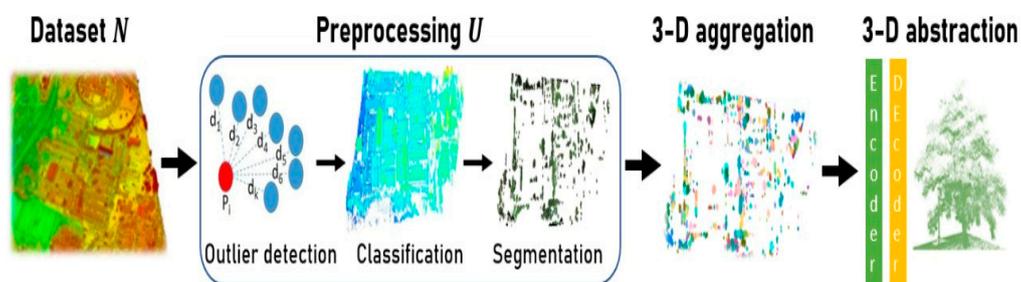


Figure 2. The framework of the proposed method.

An initial classification of urban vegetation is followed by a 3-D aggregation and an abstraction of individual tree crowns. Abstracted shapes finally enable compact information about the location, size, and spatial distribution of urban vegetation. Furthermore, we describe how each individual task has been realized.

2.1. Classification of the Urban Vegetation

The classification of urban vegetation works in two steps. Initially, outliers are detected and removed, and the remained points are separated into ground points and non-ground points. Subsequently, trees are classified by fusing the RGB components with the local maximum criteria [49].

Outliers are present in LiDAR data due to external factors such as birds, suspended particles in the atmosphere, shiny metals, surfaces with high reflective properties, and others. Removing outliers is an important task to enable a faster overall processing time. Outliers can be detected and removed by analyzing the point's neighborhood. For a given point, p_i is calculated as the distance to its closest neighbors. The aim is to estimate the average distances between it and its sample standard deviation [50].

By filtering ground points from the LiDAR data, the complexity of the urban scene is reduced. Many ground filtering approaches are available and are categorized as sloped-based methods [51,52], mathematical morphology-based methods [53–55], and surface-based methods [56–59]. The sloped-based techniques are not robust to complex terrain, while the performance of the mathematical morphology-based methods depends on the designs of elaborate local operators. Surface-based methods can approximate the ground terrain with robustness and without tedious parameters. The ground points are removed from LiDAR data N , simulating the gravitational action of a piece of cloth C that covers an inverted N [60]. The points are classified as ground points if the distance to C is less than a predefined threshold. Otherwise, it is classified as non-ground points X_i (Figure 3b,d).

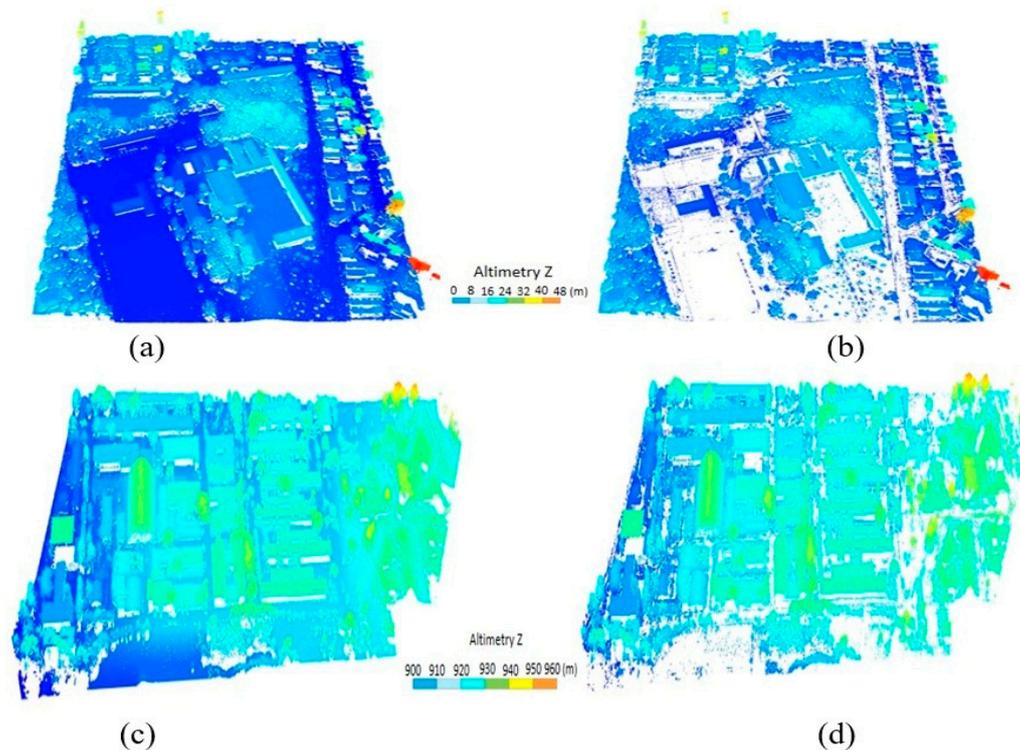


Figure 3. Filtering of the LiDAR data: (a) Original ALS data; (b) Filtered ALS data with outliers removed; (c) Original ULS data; (d) Filtered ULS data with outliers removed.

Complementary to the filtering task, an initial classification is executed in the point cloud to address the problem of false positives and false negatives of the vegetation objects. After filtering LiDAR data, the point cloud mainly contains trees, buildings, and smaller humanmade objects (Figure 4a,c). Triangulated irregular networks (TIN) can be used to search for points with height values below 5 m and 30 m [61]. It can also help assign values for non-ground points and null values for points erroneously filtered as non-ground (Figure 4b,d).

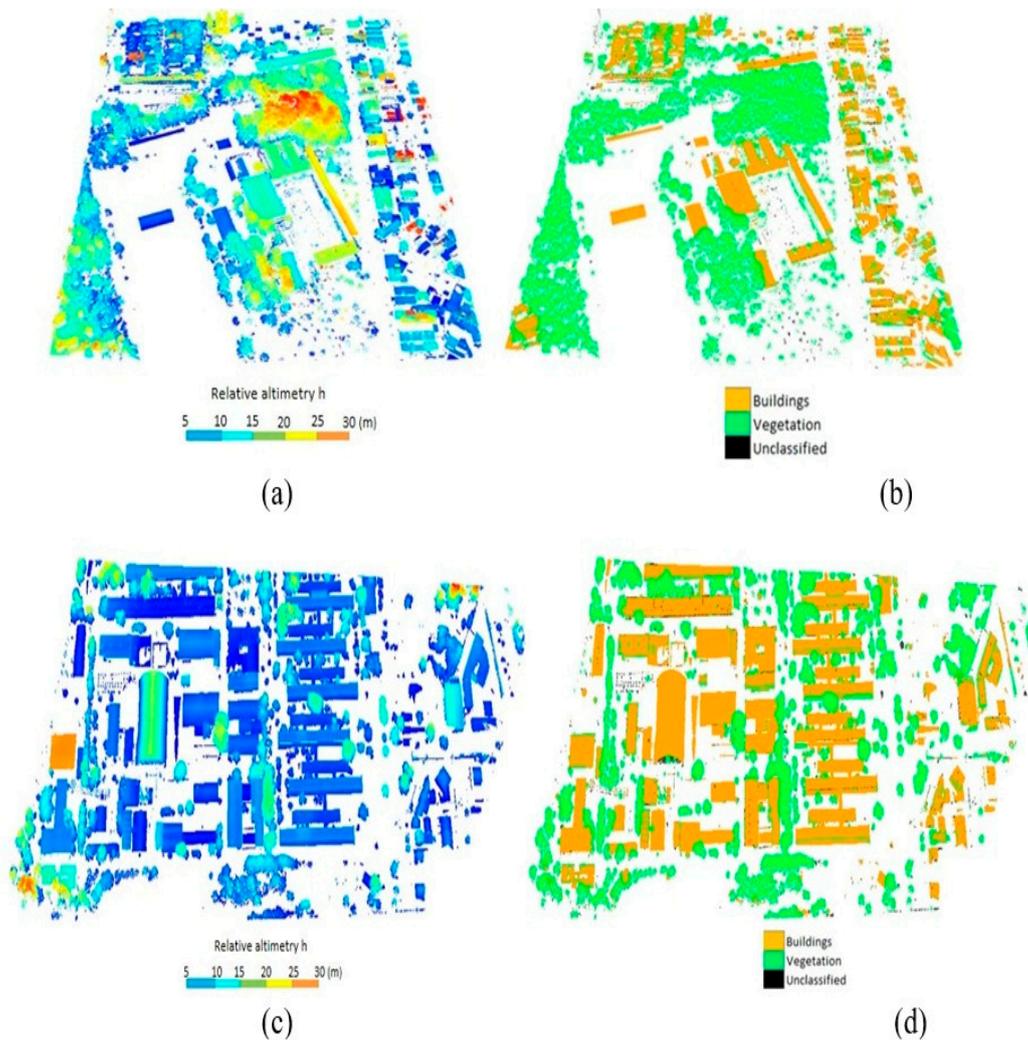


Figure 4. Results of the initial classification: (a) Filtered ALS data; (b) Results of the initial classification of ALS data; (c) Filtered ULS data; (d) Results of the initial classification of ULS data.

The flatness and ruggedness of the objects are estimated using tolerance measures of 0.1 and 0.3, respectively. Vegetation objects are associated with higher reflectance values in the green G component, while higher reflectance values in the red R component are associated with building objects. Points labeled as vegetation, for which higher values are in the R and blue B components, can be considered false negatives of buildings and false positives of vegetation. The radiometric resolution of the corresponding RGB image enables important information to distinguish trees from buildings.

In this work, the ALS data was texturized using the orthoimage available. A prior radiometric transformation of the corresponding RGB orthoimage from 8 to 16 bits was done. Consequently, the range for the RGB coordinates was extended from $\{0; \dots; 255\}$ to $\{0; \dots; 65,535\}$, corresponding to 216 levels. Therefore, points with low height variations concerning their neighbors were discarded as vegetation points by checking the existence of points with maximum height in all local neighborhoods using a search window of size 0.5 m [62].

All local maximums are validated as vegetation; otherwise, they are treated as building false negatives. The criteria used for each labeled point X_i are summarized in Table 1. In Table 1, X_iR , X_iB , X_iG represent the R, G, and B reflectance values for the point X_i , and b denotes the radiometric resolution of the image.

Table 1. The spectral and local maximum criterion to analyze a labeled point X_i .

Label	RGB criteria	Local max. criterion
Vegetation	$X_{iG} \geq 2^{b-1}; X_{iG} > X_{iR}; X_{iG} > X_{iB}$	X_i is local max.
	$X_{iG} < 2^{b-1}; X_{iG} > X_{iR}; X_{iG} > X_{iB}$	
	$X_{iR} < 2^{b-1}; X_{iR} < X_{iG}; X_{iR} \approx X_{iB}$	
	$X_{iR} \geq 2^{b-1}; X_{iR} < X_{iG}; X_{iR} \approx X_{iB}$	
Buildings	$X_{iR} \geq 2^{b-1}; X_{iR} > X_{iG}; X_{iR} > X_{iB}$	X_i is not local max.
	$X_{iR} < 2^{b-1}; X_{iR} > X_{iG}; X_{iR} > X_{iB}$	
	$X_{iG} \geq 2^{b-1}; X_{iG} < X_{iR}$ or $X_{iG} < X_{iB}$	
	$X_{iG} < 2^{b-1}; X_{iG} < X_{iR}$ or $X_{iG} < X_{iB}$	

At the end of the process, a resulting point cloud $U = \{u_1, u_2, \dots, u_n\}$ is obtained containing only true positives and false negatives of vegetation (Figure 5b,d).

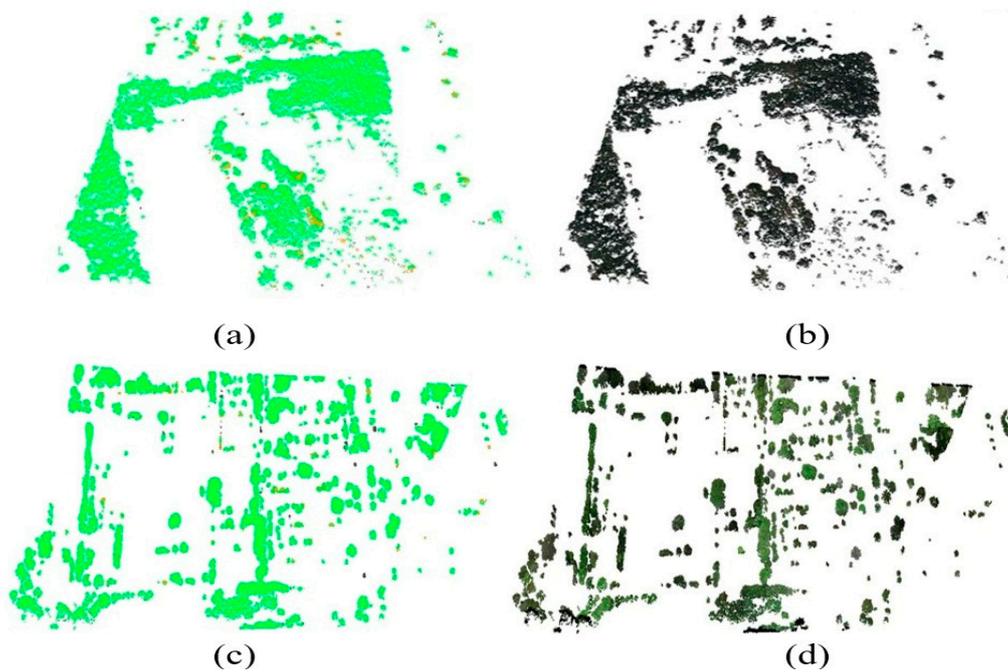


Figure 5. Labeled vegetation points: (a) Initial classification of ALS data; (b) Results of the refined classification of ALS data; (c) Initial classification of ULS data; (d) Results of the refined classification of ULS data.

2.2. Segmentation of Individual Trees

Once individual trees are accurately segmented, tree structural attributes can be extracted for urban vegetation studies. A frequently used and efficient individual tree segmentation is offered by the local maximum filtering approach and its variants [63–65]. However, since local maximum filtering is a raster-based approach, such strategies are prone to interpolation uncertainties. Cluster-based methods [66,67] depend on seed points extracted from a local maximum of a rasterized point cloud, and they are time-consuming.

A promising compromise for tree segmentation uses global maximum algorithms, clustering trees from the relative spacing between them [49]. However, a normalization task is needed to guarantee that the elevation of a point correctly indicates its height from the ground. To avoid this additional task, we adapted the global maximum algorithm, where trees are individually segmented (see Figure 6) from the tallest tree to the shortest and also from the center to the edges using few parameters.

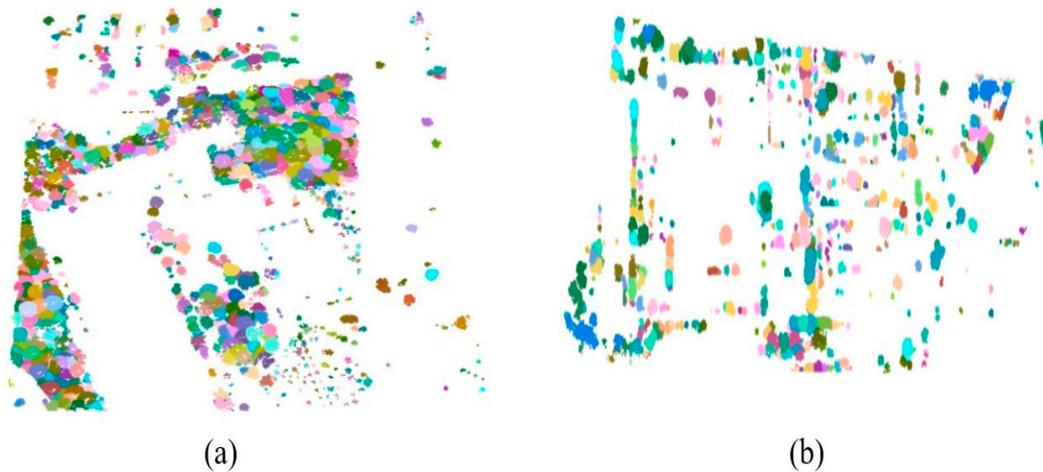


Figure 6. Segmented individual trees: (a) Results of the segmentation of ALS data; (b) Results of the segmentation of ULS data.

The set of parameters used in individual tree segmentation tasks for the ALS data and the ULS data are summarized in Table 2. Our adapted algorithm segments individual trees using the detected global maximum m by analyzing the neighboring. Since m is a local maximum within a search radius R , it can be the top of a tree belonging to the target tree of the segmentation into iteration i or belong to the top of another tree. Since m is a local non-maximum, it is only analyzed based on the minimum spacing rule.

Table 2. Summary of the parameters defined for tree crown segmentation (ALS and ULS data).

Parameter	Description	Values (m)
dt1	bottom limits	5
dt2	upper limits	7
Zu	bottom limits	15
Speed up	upper limits	10
hmin	Minimum height for a detected tree	5
R	Search radius for the local maximum	5

2.3. Proposed 3D Aggregation with Abstraction Purposes

The aim of our 3-D aggregation approach is to decrease the spatial density of the trees, maintaining their original structure with high computational efficiency. It corresponds to a 3-D aggregation approach based on Gestalt measures, such as the spatial relation of proximity and similarity, which, combined with a shape abstraction deep learning method, enables us to compact information about urban vegetation's location, size, and spatial distribution. The goal was to optimize the merge between pairs of adjacent trees. It enables properly decreasing trees' spatial density using our proposed Gestalt measures.

In this paper, the proposed 3-D aggregation operation was executed in two steps. Initially, we calculated the distances for all $\frac{n!}{(n-2)!2!}$ pairs of trees. Subsequently, the thresholds (i.e., height, length, and approximate area) were analyzed for the pairs that attend the proximity conditions. Thus, we computed a matrix in which the rows correspond to the trees resulting from the 3-D aggregation, and the columns are the recalculated attributes. Given an input V_i and V_j (e.g., pair of trees), the horizontal distance between their centroids $d(V_i, V_j)$, the predefined threshold for the distance value between V_i and V_j (t_d), our goal is to estimate the cluster of the trees G_p that best describe the proximity criterion [$d(V_i, V_j) \leq t_d, (V_i, V_j) \in G_p$].

We also used a similarity criterion for 3-D aggregation of the pairs of adjacent trees $(V_i, V_j) \in G_s$:

$$t_{h_{\min}} < \frac{h_{r_i}}{h_{r_j}} \leq t_{h_{\max}} \quad (1)$$

$$t_{C_{x_{\min}}} < \frac{C_{x_i}}{C_{x_j}} \leq t_{C_{x_{\max}}} \quad (2)$$

$$t_{C_{y_{\min}}} < \frac{C_{y_i}}{C_{y_j}} \leq t_{C_{y_{\max}}} \quad (3)$$

$$t_{S_{apr_{\min}}} < \frac{S_{apr_i}}{S_{apr_j}} \leq t_{S_{apr_{\max}}} \quad (4)$$

where: - $t_{hr_{\min}}$ and $t_{hr_{\max}}$ are the minimum and maximum threshold values, respectively, for the ratio between the relative tree heights (h_{r_i} , h_{r_j});

- $t_{C_{x_{\min}}}$ and $t_{C_{x_{\max}}}$, $t_{C_{y_{\min}}}$ e $t_{C_{y_{\max}}}$ are the minimum and maximum threshold values for the ratio between the lengths of the trees in X coordinates (C_{x_i} , C_{x_j}) and in Y coordinates (C_{y_i} , C_{y_j});

- $t_{S_{apr_{\min}}}$ e $t_{S_{apr_{\max}}}$ are the minimum and maximum threshold values for the ratio between the approximate areas of the trees (S_{apr_i} , S_{apr_j}).

Note that G_s is a cluster obtained from the similarity criterion. It is composed by pairs of adjacent trees with similar heights and approximate surface area, such that $G_s \subset G_p$. Interestingly, when all neighbors' trees are identical, we have a particular case $G_s \subseteq G_p$. One of the key challenges when aggregating such objects is related to the vegetation cover area limits in the range of values between 5 m x 5 m (upper limit for LoD 3) and 50 m x 50 m (lower limit for LoD 1). Furthermore, wrong aggregations can occur derived from the preliminary suppression of the existing buildings.

To overcome this problem, we used different threshold values by assuming the LoD 2 point cloud CityGML 3.0 specifications. We have used two strategies to assign threshold values for Cx, Cy, and S_{apr} components. First, we considered the similarity between the two horizontal spacing limits adopted for previous segmentation (e.g., 5 m and 7 m). Second, we used the value of 1.5 m as the upper limit for the ratio of superficial areas like [42], whose approach focused on footprint areas of buildings to be aggregated. Once the LoD 2 has no specifications for height dimensions from point cloud objects, we adopted the following values: $\frac{5}{6}$ e $\frac{6}{5}$ for the ratio of relative heights. The minimum and maximum threshold values used for all parameters are presented in Figure 7.

		Proximity	Similarity							
		Euclidean horizontal distance	Height		Length in X		Length in Y		Approximate area	
		t_d (m)	$t_{h_{min}}$	$t_{h_{max}}$	$t_{c_{x_{min}}}$	$t_{c_{x_{max}}}$	$t_{c_{y_{min}}}$	$t_{c_{y_{max}}}$	$t_{s_{apr_{min}}}$	$t_{s_{apr_{max}}}$
Threshold	A	35	$\frac{5}{6}$	$\frac{6}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{25}{49}$	$\frac{49}{25}$
	B				$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{1,5}$	1,5
	C	30			$\frac{5}{7}$	$\frac{7}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{25}{49}$	$\frac{49}{25}$
	D				$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{1,5}$	1,5
	E	25			$\frac{5}{7}$	$\frac{7}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{25}{49}$	$\frac{49}{25}$
	F				$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{1,5}$	1,5
	G	20			$\frac{5}{7}$	$\frac{7}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{25}{49}$	$\frac{49}{25}$
	H				$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{1,5}$	1,5
	I	15			$\frac{5}{7}$	$\frac{7}{5}$	$\frac{5}{7}$	$\frac{7}{5}$	$\frac{25}{49}$	$\frac{49}{25}$
	J				$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{\sqrt{1,5}}$	$\sqrt{1,5}$	$\frac{1}{1,5}$	1,5

Figure 7. Proposed 3-D aggregation threshold values.

As results, we have a set of aggregated trees and a set of non-aggregated trees. Finding the structural attributes of each tree, we calculated important metrics to quantify the degree of segmentation of the existing tree set GF and the average internal distance GD between them, as follows:

$$GF = \frac{AD}{\sum S_{apr_i}} \quad (5)$$

$$GD = \frac{\sum d_{v_i, v_j}}{\sum (v_i, v_j)} \quad (6)$$

where: - AD represents the number of trees delimited into area of study;

- $\sum S_{apr_i}$ is the total surface area of an existing tree canopy;
- $\sum d_{v_i, v_j}$ denotes the sum of all horizontal distances between adjacent trees;
- $\sum (v_i, v_j)$ is the total number of existing pair of adjacent trees.

Note that, GF is measured in trees/square meter of green area, and GD is measured in meters. The 3-D data aggregation reduces fragmentation RF due to the clustering and increases tree spreading ADA, as the smallest internal distances are suppressed in the clustering operation. Therefore, we calculated the variation of GF and GD using the expressions:

$$RF = 100x \left(1 - \frac{GF_g}{GF_o} \right) \% \quad (7)$$

$$ADA = 100x \left(\frac{GD_g}{GD_o} - 1 \right) \% \quad (8)$$

Where:

- GF_g denotes the degree of fragmentation of the set of trees resulting from the 3-D aggregation;
- GF_o is the degree of fragmentation of the set of trees before the 3-D aggregation;
- GD_g represents the degree of dispersion of the set of trees resulting from the 3-D aggregation;
- GD_o denotes the degree of dispersion of the set of trees before the 3-D aggregation;
- RF is the percent reduction in degree of fragmentation obtained after the 3-D aggregation, and ADA denotes the percentage increase in the degree of dispersion obtained after the 3-D aggregation.

Other challenges when storing, analyzing, and visualizing LiDAR data are related to memory requirements. However, without powered computers, one can still abstract the aggregated trees into a compact, structured point cloud. An abstraction task is needed to reduce memory requirements and computing times. Toward this goal, we adopted the deep leaning compression method [48].

Learning a set of local feature descriptors [43] and reconstructing the original aggregated trees from the embedding provides an abstracted point cloud, as shown in Figure 8.

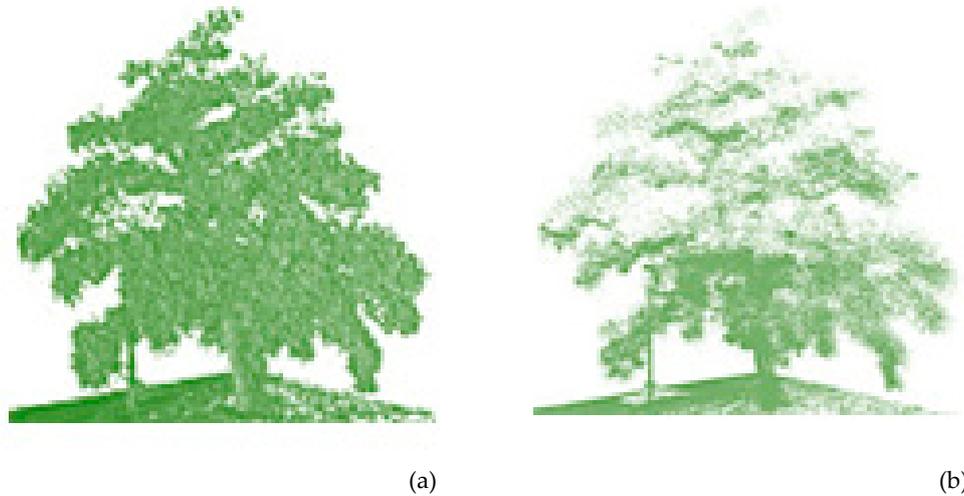


Figure 8. 3-D abstraction task: (a) Original individual tree; (b) Results of the abstraction task.

3. Study Area and Materials

3.1. Study Area

For evaluation, two reference areas are selected (Figure 9a,c). The reference area A corresponds to Salvador, a city in northeastern Brazil with around 640 km². Salvador is known for its Portuguese colonial architecture, afro-brazilian culture, and tropical coastline, making it one of Brazil's most tree-rich cities. Area A presents an average altitude of less than 12 meters, composed of vegetation, roads, and different building structures. The local flora is highly heterogeneous and composed of trees and shrub species of varying plant structures found in public squares, gardens, and private and restricted access properties. Ground vegetation (grasses) is also found in the region, mainly in flowerbeds of streets and avenues. The reference area B corresponds to Curitiba, a city in south Brazil with around 430 km² (Figure 9c). Curitiba is the largest tree-rich city in Brazil. The study area comprises 0.26 km² of vegetation, streets, and different types of buildings (Figure 9d). The local flora includes different tree structures, especially Ipe and Parana pine trees.

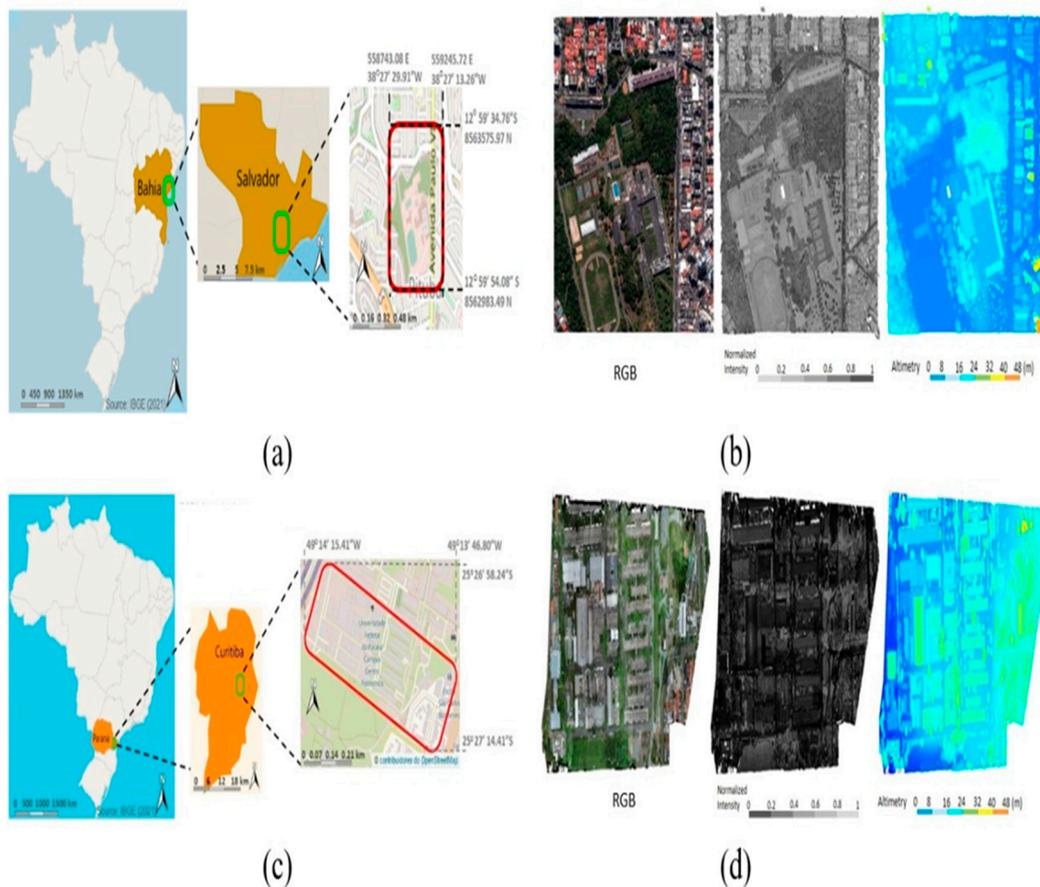


Figure 9. Overview of reference areas: (a) Study area 1 (Salvador); (b) Orthoimage, intensity image, and Hypsometric image of the area 1; (c) Study area 2 (Curitiba); (d) Orthoimage, intensity image, and Hypsometric image of the area 2.

3.2. Data

The flights for Salvador were carried out between August 2016 and February 2017 with an airborne laser scanning system (ALS). This reference area was acquired by a RIEGL VQ480-II laser sensor integrated with a global navigation satellite system (GNSS) in conjunction with an inertial navigation system (INS) and one UltraCam Lprime metric camera from Vexcel. The specified point density is 8 pts/m². The RGB orthoimage (**Figure 9b**) was added to texturize the urban trees. The ALS data covers an area of 0.3 km². LiDAR data from Curitiba originates from the unmanned laser scanning system (ULS) surveys in October 2021. The reference area B was acquired by a Zenmuse L1 laser sensor rigidly fixed within the DJI platform [68] with a mean flight altitude of 80 m and a footprint of 1 cm. The specified point density is 280 pts/m². Note that, for this area test, the ULS data is not texturized with an RGB orthoimage.

4. Results

This section provides detailed insights into the proposed method's results applied to areas 1 and 2. It is structured according to the individual processing tasks.

4.1. Classification and Segmentation of the Individual Urban Vegetation

By analyzing and refining the classification procedure using the local maximum criteria and the RGB criteria, we found the confusion matrix for the ALS data and for ULS data classification, as shown in Table 3. The truth reference data (initial classification) was generated using the LAsTools software, and it is used as a reference to assess the global accuracy of our method.

Table 3. Confusion matrix of the point cloud classification.

ALS		Truth reference		
		Vegetation	Non-vegetation	Total of points
Label	Vegetation	500.164	94.225	594.389
	Non-vegetation	18.569	408.114	426.683
	Total	518.733	502.339	1.021.072
ULS				
Label	Vegetation	6.455.452	1.089.707	7.454.159
	Non-vegetation	169.953	14.944.094	15.114.047
	Total	6.625.405	16.083.801	22.659.206

Table 3 reveals that the global accuracy of the ALS data was higher than 88% (908.278 correctly labeled points/1.021.072 truth reference points). Thus, the classification accuracy can be improved in highly densified vegetation areas when flatness and ruggedness criteria are incorporated. We noted that few false positives were detected, and it implied a decrease in the difference between the quantities of points initially labeled as vegetation and building from 179.017 points to 16.394 points. The results are more compatible when the errors of omission (3.75%) and inclusion (15.85%) are added to the vegetation label.

For the ULS data, the global accuracy achieved was higher than 94% (21.399.546 correctly labeled points/22.659.206 truth reference points). Unlike the ALS data, the difference between the points initially labeled as vegetation and building has increased from 7.568.888 points to 9.548.396 points when the errors of omission (14.44%) and inclusion (2.56%) are added to the vegetation label. This difference has shown that the performance of the proposed classification method is more efficient for areas with a sparse number of concentrated trees (area A). Notably, the volumetric spread has performed as an essential metric to avoid false positives.

In terms of the segmentation, more than 851 trees were segmented in ALS data, representing a spatial density around 29 trees/hectare. For the ULS data, more than 518 trees were segmented, resulting in a spatial density of 20 trees/hectare. From the quantitative result of tree delimitation (AD), we have calculated the degree of fragmentation (GF) and dispersion (GD) of the set of segmented trees as well as the spatial density of trees (DA), as shown in Table 4.

Table 4. Landscape metrics obtained with our segmentation method.

Data	AD	DA (tree/hectare)	GF (tree/green area)	GD (m)
ALS	851	28.65	67.33	9.73
ULS	518	19.9	78.96	10.45

Note that our segmentation method depends on the chosen parameters, whose thresholds can change the number of delimited trees and the values of their extracted metric attributes.

4.2. 3D Aggregation with Abstraction of Individual Trees

Our 3-D aggregation approach includes spatial relation of proximity and similarity measures to optimize the merge between pairs of adjacent trees (V_i and V_j), decreasing objects' spatial density without losing their original structure. These spatial relations were quantified using the following Gestalt measures depicted in section 2. As a result, we have obtained a diversity of metrics from the predefined thresholds (see **Figure 10**). In a close look at the 3-D aggregation results (Table 5), it is noticeable that the simultaneous decrease in the proximity and relative size thresholds has implied a reduction in the number of merged trees (AM). Consequently, the number of non-aggregated trees (ANA) increased (see set J in Table 5).

Table 5. Metrics for ALS and ULS data.

Data	Threshold	GF(*)	GD (m)	ANA	AM
ALS	A	64.31	12.56	431	382
	B	65.26	13.37	554	271
	C	64.16	14.48	457	354
	D	65.58	13.94	580	249
	E	61.70	14.17	496	284
	F	63.29	14.11	625	175
	G	62.65	14.64	552	240
	H	62.34	14.12	670	118
	I	60.68	14.81	625	142
	J	62.57	14.07	722	69
ULS	A	75.31	17.58	311	181
	B	75.3	16.84	397	97
	C	73.93	17.63	341	144
	D	74.39	16	409	79
	E	72.68	17.81	373	105
	F	74.39	17.31	430	58
	G	73.17	17.35	405	75
	H	74.84	16.79	449	42
	I	74.39	16.91	446	42
	J	76.52	16.41	482	20

* GF in tree/square meter of green area.

These results may lead us to infer that the set J is the least prone to shape abstraction by 3-D aggregation. For all sets of thresholds, the number of ANA is higher than the number of AM. The set I has achieved the highest 3-D aggregation by using the proposed method. In this case, it was quantified by the highest RNA value (see Figure 10), due to the lower number of resulting trees (merged and non-aggregated).

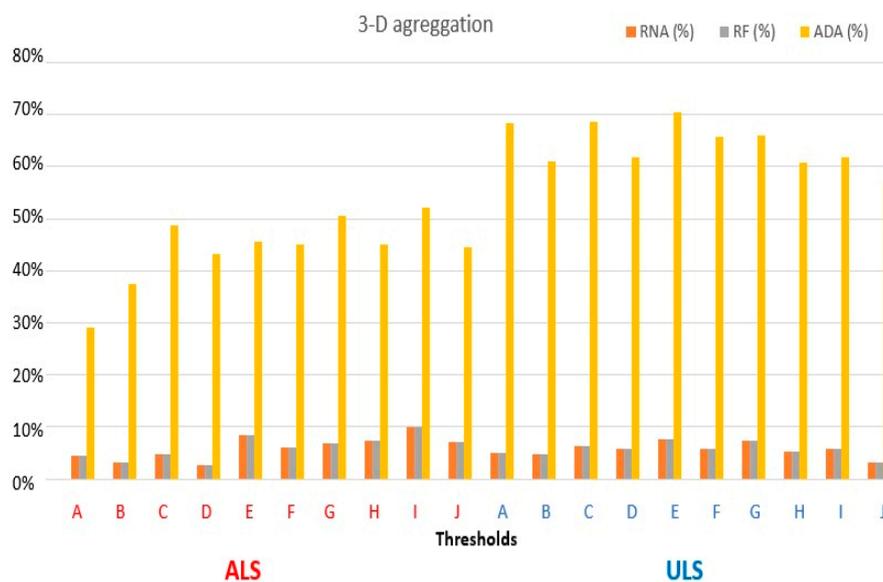


Figure 10. 3-D Aggregation results for the ALS and the ULS data after the 3-D aggregation procedure.

The highest values of the two calculated indexes are associated with the same set I. A direct relationship between the RF and ADA metrics was obtained. This means the reduced fragmentation of the tree set made them more dispersed. In the case of set B, the fragmentation reduction obtained

was smaller than for set A, and a smaller dispersion reduction value was also expected. However, a higher ADA value was obtained for set B than for set A. Note also that the lowest values obtained for RF and ADA are not associated with the same set. The set D generated the lowest RF and set A the highest ADA. The 72.65% and 98.47% storage space for ALS and ULS data, respectively, indicate good 3-D abstraction (Table 6). The computational storage space of the point clouds is consistently smaller than their original data.

Table 6. 3-D abstraction results for ALS and ULS data.

Data	Storage space (%)	
	$\mu = 1$	$\mu = 2$
ALS	72.65	45.32
ULS	98.47	96.94

In Figure 11, a comparison between the landscape metrics (fragmentation and dispersion) reveals that the abstraction performed by deep learning implied the most significant variations in relative height and crown surface area and the greatest number of trees eliminated. All calculated indexes with the highest values are associated with the deep learning architecture ($\mu = 1$). We also detected that the compression performed by deep learning implied the highest variations in the structural attributes of the trees as well as the highest number of eliminated trees. All ΔP and Δh calculated values are less than 1 m, and the ΔS values are less than 50 m². The abstractions did not entail enough loss of information to make the tree representation applied to the point clouds incompatible with LoD2.

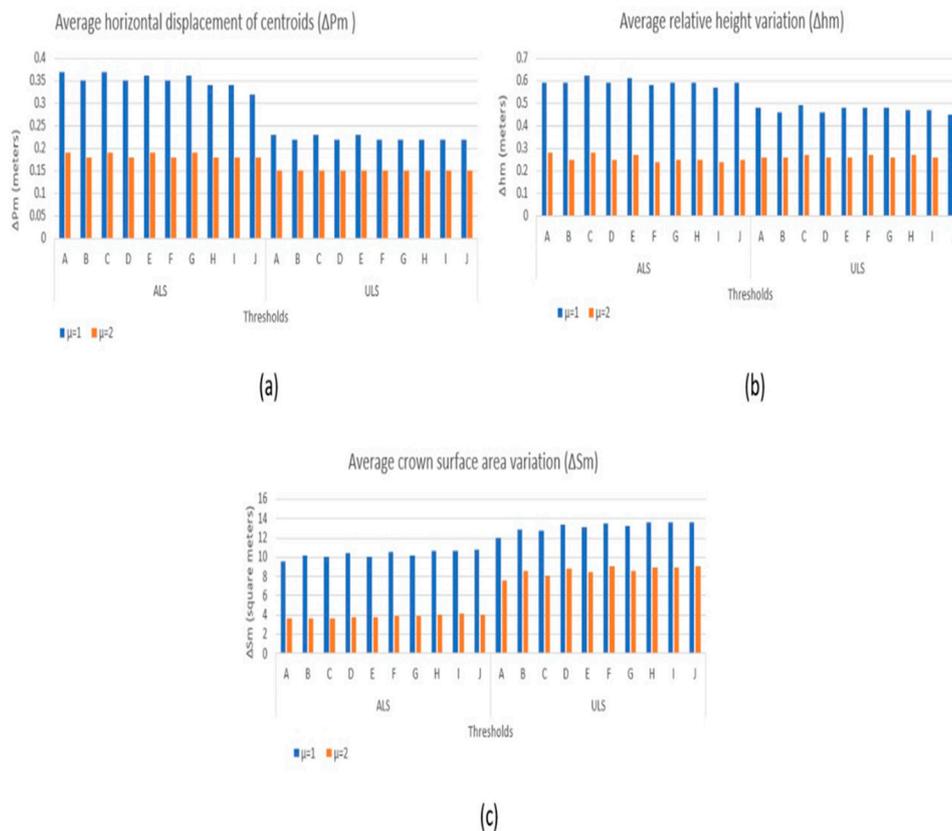


Figure 11. Correspondence of the abstracted individual trees with the original point clouds: (a) Average horizontal displacement of centroids; (b) Average relative height variation; (c) Average crown surface area variation.

5. Discussion

5.1. Classification and Segmentation of Urban Vegetation

An extensive approach has been developed, allowing the classification and segmentation of individual trees in ALS and ULS point clouds. To reduce noise in the point clouds and the complexity of the urban scene, buildings, powerlines, and ground objects are filtered. Filtering is proved to be essential for the classification procedure. It removes spurious points, avoiding oversampling in the estimation of the flatness and volumetric scattering attributes.

Individual trees in ALS and ULS data with high point density cannot be classified using only geometric features [69]. Our approach that combines both the spectral and geometric criteria solves the limitation. Combining these metrics leads to a high classification accuracy of 85% and 95% for ALS and ULS data, respectively. The segmentation algorithm has achieved good performance and guaranteed the extraction of the desired structural attributes of the individual trees. Therefore, special attention to the thresholds is crucial, which may lead to erroneous segmentation. A high segmentation accuracy of 75% is observed for LiDAR data containing substantially more compact urban trees. The goal of an efficient and complete segmentation of the individual urban trees in the ALS and ULS point clouds is fulfilled.

5.2. 3D Aggregation and Abstraction Tasks

LiDAR point clouds have become the base for a variety of tasks related to vegetation urban planning studies. However, the high computational effort required for storage, analysis, and visualization of LiDAR data remains often challenging due to its high point density. A 3-D aggregation combined with a deep learning LiDAR abstraction task is chosen as it offers the advantages of maintaining spatial coherence and sufficient data realism.

Erroneous segmentation and distance between individual trees are detected from ALS and ULS data using the fragmentation and dispersion of total green area metrics. Our method can also be used to calculate other attributes such as the localization, height, canopy area, and spatial distribution information of individual urban trees. The degree of fragmentation is minimal (10%), while the average degree of dispersion is around 70%. This observation does not fully hold for all thresholds used in this study.

The results from the aggregation task are highly influenced by the point density of LiDAR data. For example, the ULS data presented several reduced points, and the percentage of storage space was significantly more significant than the ALS data. However, a linear relationship between the reduction of the number of points and the storage space is not perceptible, although they are directly proportional. Furthermore, area B presented a higher impact on more minor degrees of fragmentation and initial tree dispersion than area A. This suggests that point density has a significant influence.

The fragmentation reductions and dispersion increases calculated after 3-D aggregation showed a noticeable direct relationship for the ULS data, which was not observed for the ALS data. Notably, exploiting spatial measures associated with Gestalt measures of proximity and similarity showed a dominant effect in reducing the spatial density of trees and the degree of fragmentation of the total green area. The mixture of trees relies on the criteria of proximity and similarity that can increase the degree of dispersion. Regarding the correspondence with the original point cloud, the best abstraction results mainly were obtained with the autoencoder $\mu = 2$. From each database created, we can access information about mapped urban trees' location, size, and spatial distribution.

6. Conclusions

This paper presents a 3-D aggregation task combined with a deep learning method for abstracting individual urban trees in ALS and ULS LiDAR data. As the 3-D shape abstraction approaches for urban vegetation studies are still limited to support spatial analyses of non-vegetation urban elements, such as buildings, thus lacking the realization of studies that contemplate its specific application, the present work proved innovative. Although it is not possible to discriminate which

LiDAR data performed the best abstraction task, the approach fulfills the objective of reducing the storage space of the LiDAR data. In contrast to only considering the individual trees, further works will consider the information that might be learned from the trees context. The geometric and topological relations between trees parts could be learned to constrain the model reconstruction. An obvious further way for improvement is the inclusion of hyperspectral images.

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